Lock-and-Key Mechanisms of Cerebellar Memory Recall Based on Rebound Currents

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Wetmore DZ, Mukamel EA, Schnitzer MJ. Lock-and-key mechanisms of cerebellar memory recall based on rebound currents. J Neurophysiol 100: 2328–2347, 2008. First published August 1, 2007; doi:10.1152/jn.00344.2007. A basic question for theories of learning and memory is whether neuronal plasticity suffices to guide proper memory recall. Alternatively, information processing that is additional to readout of stored memories might occur during recall. We formulate a “lock-and-key” hypothesis regarding cerebellum-dependent motor memory in which successful learning shapes neural activity to match a temporal filter that prevents expression of stored but inappropriate motor responses. Thus, neuronal plasticity by itself is necessary but not sufficient to modify motor behavior. We explored this idea through computational studies of two cerebellar behaviors and examined whether deep cerebellar and vestibular nuclei neurons can filter signals from Purkinje cells that would otherwise drive inappropriate motor responses. In eyeblink conditioning, reflex acquisition requires the conditioned stimulus (CS) to precede the unconditioned stimulus (US) by >100 ms. In our biophysical models of cerebellar nuclei neurons this requirement arises through the phenomenon of postinhibitory rebound depolarization and matches longstanding behavioral data on conditioned reflex timing and reliability. Although CS–US intervals <100 ms may induce Purkinje cell plasticity, cerebellar nuclei neurons drive conditioned responses only if the CS–US training interval was >100 ms. This bound reflects the minimum time for deinactivation of rebound currents such as T-type Ca2+. In vestibulo-ocular reflex adaptation, hyperpolarization-activated currents in vestibular nuclei neurons may underlie analogous dependence of adaptation magnitude on the timing of visual and vestibular stimuli. Thus, the proposed lock-and-key mechanisms link channel kinetics to recall performance and yield specific predictions of how perturbations to rebound depolarization affect motor expression.

INTRODUCTION

Research to date on the biological mechanisms of long-term memory has focused primarily on candidate mechanisms for memory formation, such as neuronal plasticity. But to what degree are the phenomenological properties of memory determined by biological mechanisms of memory recall? Studies on recall mechanisms have concerned reconsolidation processes that accompany retrieval (Debiec et al. 2006; Doyere et al. 2007), network attractor theories of associative memory (Hopfield 1982; Wills et al. 2005), and expression of learned reflexes (du Lac et al. 1995; Mauk and Donegan 1997; Medina and Mauk 2000; Medina et al. 2000). However, the electrophysiological dynamics that occur during recall might have an important role in shaping qualities such as memory reliability and generalization. Thus, a basic question is whether these dynamics function primarily as a readout mechanism for retrieving stored memories or also perform additional processing of the stored information. Pattern completion is one aspect of associative memory recall for which candidate biological mechanisms have been identified (Nakazawa et al. 2002). Nonetheless, the existing literature on recall has generally assumed that the electrophysiological dynamics of recall should facilitate effective readout, i.e., retrieving the appropriate memory in response to a stimulus. The possibility that some constraints on memory expression might also be enacted at recall has not been widely considered.

Recent work on cerebellar memory systems indicates there are multiple loci of neuronal plasticity and at least two different brain areas of memory storage with distinct induction kinetics (Boyd en et al. 2004; De Zeeuw and Yeo 2005; Hansel et al. 2001; Lang et al. 1999; Ohyama and Mauk 2001; Ohyama et al. 2003a). According to two-stage models of cerebellar learning, the numerous synapses in cerebellar cortex support flexible and rapid acquisition of new associations, whereas subsequent plasticity in the deep cerebellar or vestibular nuclei allows long-lasting memory storage (Boyd en et al. 2004; du Lac et al. 1995; Mauk 1997; Mauk and Donegan 1997; Miles and Lisberger 1981). Purkinje cells in the cerebellar cortex receive inputs from approximately 10⁵ parallel fibers and project outputs to the deep cerebellar and vestibular nuclei in a highly convergent manner, with each nuclear cell influenced indirectly by 10⁵–10⁶ parallel fibers (Mauk 1997; Napper and Harvey 1988). Given the vast number of potential network states in the cerebellar cortex, a rich set of training experiences might lead to network states that encode undesirable or inappropriate movements. The plausibility of this occurring is indicated by behavioral and computational studies that suggest the distribution of synaptic plasticity levels might evolve in a complex manner throughout learning experience, rather than purely reversing course during extinction or relearning (Kimpo et al. 2005; Mauk and Ohyama 2004). An example of an undesirable motor response is one executed in response to sensory cues that are reliably associated with rewarding or aversive stimuli but that arrive too late to be predictive of an appropriate motor action. Are there memory recall mechanisms that selectively prevent the expression of inappropriate motor responses, despite significant induction of synaptic plasticity? Or does plasticity induction always suffice to modify cerebellar-mediated motor behavior? At least for some forms of...
associative motor learning mediated by noncerebellar memory systems, it has been shown that associative memory storage by itself can be insufficient to modify behavior (Barnet et al. 1997).

To explore these issues, we formulated a “lock-and-key” hypothesis stating that the induction of plasticity is necessary but not sufficient to modify motor behavior. There is the additional requirement that plasticity must shape the dynamics of neural activity (the “key”) to match a temporal filter (the “lock”) that selectively precludes inappropriate motor responses to sensory stimuli. We examined this hypothesis in the context of two cerebellum-dependent behaviors, classical eyeblink conditioning (Christian and Thompson 2003) and adaptation of the vestibulo-ocular reflex (VOR) (Ito 1982; Miles and Lisberger 1981), for which there exist longstanding, rich behavioral data sets (Gormezano et al. 1962; Raymond and Lisberger 1996). If our hypothesis is true, what biological mechanisms might serve as the lock for these two behaviors?

This paper focuses on rebound currents in the deep cerebellar nuclei (DCN) and medial vestibular nuclei (MVN) neurons as candidate lock mechanisms, because it is well established that these currents perform significant temporal transformations of hyperpolarizing inputs, such as those from cerebellar Purkinje cells believed to trigger learned movements. Rebound channels, such as low voltage-activated (T-type) and hyperpolarization-activated cation (h) channels, are expressed at sufficient density to generate robust postinhibitory rebound depolarizations in DCN and MVN neurons, the output neurons of cerebellar circuits (Aizenman and Linden 1999; Aizenman et al. 1998; Jahnson 1986a; Linilás and Muhlethaler 1988; Sekirnjak and du Lac 2002). For both behaviors studied, rebound channel kinetics emerge as crucial determinants of the minimum allowable duration between a sensory cue and a trained motor response. If the delay between the cue and a well-timed response is less than the time needed to activate rebound channels fully from the neuronal resting potential, the magnitude of the learned response declines or vanishes, thereby enacting the lock mechanism. This proposal represents a direct link from channel kinetics to learning performance and yields specific predictions of how learning performance is affected by perturbations to the rebound process.

In eyeblink conditioning, key aspects of the behavior that remain poorly understood concern stimulus timing. Training of a reliable reflex requires the conditioned stimulus (CS), such as a tone, to start at least 100 ms prior to the unconditioned stimulus (US), such as an air puff to the eye (Fig. 1A) (Gormezano et al. 1962; Ohyama et al. 2003b). Even after averaging data over multiple subjects, there remains a steep dependence of reflex acquisition on the CS–US training interval (Fig. 1B), with the expression of conditioned blinks falling sharply for intervals <100 ms (Ohyama et al. 2003b; Salafia et al. 1980; Schneiderman and Gormezano 1964; Smith 1968; Smith et al. 1969). What is the mechanistic basis for this effect? Analogous, unexplained dependencies on stimulus timing have been reported for VOR adaptation, in which the magnitude of learned eye movements depends on the timing between pulsed visual and vestibular training stimuli (Raymond and Lisberger 1996).

According to current thinking in the field an important mechanism of memory formation is the long-term depression (LTD) of cerebellar parallel fiber (PF) to Purkinje cell synapses induced by synchronous activation of PF and climbing fiber (CF) inputs to Purkinje cells (Albus 1971; Ito 1989; Ito and Kano 1982; Marr 1969). In eyeblink conditioning, it is thought that PF and CF inputs respectively convey signals regarding the CS and the US (Hesslow et al. 1999; Mauk et al. 1986; McCormick et al. 1985; Steinmetz et al. 1989; Steinmetz et al. 1986), and that LTD resulting from repeated CS–US pairings leads to a conditioned reflex to the CS alone. This is proposed to occur since LTD should diminish the efficacy of CS-driven input to Purkinje cells, allowing disinhibition of deep cerebellar nuclei (DCN) neurons that receive GABAergic Purkinje cell inputs and drive conditioned reflexes (Albus 1971). In VOR adaptation, CFs and PFs respectively convey visual and vestibular information, and LTD is proposed to allow adaptive increases in VOR amplitude by reducing the strength of PF inputs signaling ipsiversive head rotation (Ito 1989). Although another cerebellar plasticity mechanisms exist (Boyden et al. 2004; De Zeeuw and Yeo 2005; Hansel et al. 2001), multiple strains of mice with disrupted LTD show deficits in eyeblink conditioning and VOR adaptation (Feil et al. 2003; Kishimoto et al. 2001; Koekkoek et al. 2003, 2005; Miyata et al. 2001; Shibuki et al. 1996). Nonetheless, accounts of cerebellar-mediated learning based solely on LTD do not easily explain the full range of behavioral data (Boyden and Raymond 2003; Boyden et al. 2006; Kimpo et al. 2005; Medina and Mauk 1999; Ohyama and Mauk 2001; Ohyama et al. 2003a).

One issue concerns whether Purkinje cells purely inhibit motor responses. Purkinje cells might be partly excitatory in their net effect, due to postinhibitory depolarization in their target DCN and MVN neurons (Aizenman et al. 1998; Jahnson 1986a,b; Linilás and Muhlethaler 1988; Sekirnjak and du Lac 2002). Another issue concerns the possible role in learning of long-term potentiation (LTP) at the PF–Purkinje cell synapse. LTP and LTD induction at this synapse are spike-timing dependent (Abbott and Nelson 2000), with LTP induced by unpaired PF or asynchronous PF–CF input (Coemens et al. 2004; Wang et al. 2000). Maximal LTD induction seems to
occur for PF activity that slightly precedes CF activity by 50–100 ms, which likely reflects the kinetics of postsynaptic Ca\(^{2+}\) dynamics (Doi et al. 2005). LTD induction can occur with either PF or CF activity occurring first, but delays of \(\geq 200\) ms are ineffective with either ordering (Wang et al. 2000). It has been suggested that inhibition of cerebellar nuclei neurons and spike-timing dependent plasticity suffice to explain the requirement in eyeblink conditioning for the CS–US interval to be \(> 100\) ms (Wang et al. 2000). However, this has never been demonstrated explicitly using either computational modeling or experimental manipulation of behavior. A main difficulty is that the empirically determined rules for LTD induction suggest LTD should occur at short CS–US intervals that do not lead to acquisition of conditioned reflexes in behavioral experiments (Wang et al. 2000). Furthermore, the dependence of learning performance on the CS–US interval appears much steeper than that of spike-timing dependent plasticity at the PF–Purkinje cell synapse (Salafia et al. 1980; Schneiderman and Gormezano 1964; Smith 1968; Smith et al. 1969; Wang et al. 2000). Thus, the degree to which conditioned reflex acquisition is shaped by physiological mechanisms other than spike-timing dependent plasticity remains an important issue for experimental investigation.

Here, we consider the novel possibility that significant shaping of learned motor expression might occur through the electrophysiological mechanisms of memory recall. In our work LTP and LTD emerge as complementary processes, both of which are important for memory formation as well as for memory clearance. This contrasts with the common view of LTD and LTP as opposing processes, one allowing memory storage and the other clearance (Boydén and Raymond 2003; Coemans et al. 2004; Lev-Ram et al. 2003). Because plasticity induction is spike-timing dependent, we begin by considering the timing of sensory driven activity in the PF axons of cerebellar granule cells. Using a series of electrical compartmental models of increasing complexity, we simulate responses of DCN and MVN cells to learned sensory cues. This allows us to validate quantitatively the data from our DCN cell simulations against the classic behavioral data on eyeblink conditioning (Salafia et al. 1980; Schneiderman and Gormezano 1964; Smith 1968; Smith et al. 1969), by comparing the percentage of trials with successful responses as found experimentally to data generated by our models.

Comparison of the VOR adaptation magnitude in our modeling to that in behavioral studies suggests postinhibitory rebounds might play a role in multiple cerebellum-dependent behaviors. Based on the results of our biophysical models we provide an algorithmic description of the “lock-and-key” mechanism as a temporal filter. Learning experience that successfully modifies motor behavior shapes neural activity to match this temporal filter. Unsuccessful training can yield comparable magnitudes of synaptic plasticity, but the resulting patterns of Purkinje cell activity do not trigger learned motor responses. We have organized the following sections so that readers who wish to omit the computational details may skip the following METHODS section without loss of logical continuity.

METHODS

General simulation procedures

We created compartmental models of DCN and MVN cells in the NEURON (Hines and Carnevale 1997) and MATLAB software environments and set model parameters using empirically determined values whenever possible. Fortunately, much is known about DCN cells from in vitro studies. We found that values determined from measurements in DCN and MVN cells, rather than other cell types, facilitated consistency with behavioral data. The current balance equation describing the balance of capacitive and ionic currents, \(C_m(DV/dt) = -\Sigma I_{ionic}\), was integrated over time using the MATLAB function ode45 for deterministic one-compartment simulations, an Euler method for one-compartment simulations with stochastic synaptic inputs, or NEURON’s implicit Euler method for two-compartment simulations. In all simulations, timesteps were less than or equal to 0.1 ms and the membrane capacitance \(C_m\) was 1 \(\mu\)F/cm\(^2\).

Voltage-dependent currents obeyed equations of the form \(I = g_{\alpha}x(V - V_m)\), where \(g\) is the maximum conductance and \(V_m\) is the reversal potential. Activation variables, \(x\), followed first-order kinetics defined by \(dx/dt = \phi_x(\alpha_x(V)(1-x) - \beta_x(V)(x))\), where \(\alpha_x\) and \(\beta_x\) are forward and backward rates and \(\phi_x = Q_{10}^{T/T_0}\) is a temperature factor. \(Q_{10}\) was 1.4 for T-type current and 2.3 for all other conductances. \(\Delta T\) is the difference between the physiological temperature of 37°C used for all simulations and the temperature at which experimental measurements of channel kinetics were made. Inactivation variables, \(y\), obeyed analogous expressions. Steady-state and relaxation time constants are given in terms of \(\alpha\) and \(\beta\); \(x = \alpha/(\alpha + \beta)\) and \(\tau = 1/(\phi_x(\alpha + \beta)).\)

The firing rates of Purkinje cells were modeled to be from a cerebellar network after behavioral training. Electrophysiological data from in vivo recordings were used to constrain background firing rates, \(r_{PKj,b}\) = 40 Hz (Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006), and the modulation of Purkinje cell firing rates due to learning-related cerebellar plasticity; low and high Purkinje cell spike rates following depression and potentiation of parallel fiber inputs were \(r_{PKj,d} = 20\) Hz and \(r_{PKj,p} = 100\) Hz, respectively (Berthier and Moore 1986; Jirenhede et al. 2007; Kotani et al. 2006).

Given these basic constraints the average Purkinje cell spike rate, \(R_{PKj}(t)\), was determined by first convolving a smooth plasticity function, \(S(\Delta t)\), whose argument is the relative delay between activity in parallel fibers and climbing fibers (Fig. 2A), with a boxcar function, \(U(t)\), representing a US of 10 ms duration. The result of this convolution was multiplied by a smooth function, \(C(t)\), representing a CS of duration no less than a minimum interval, \(t_{CS_{min}} = 50\) ms

\[
S(\Delta t) = A_1 + A_2[(\tau_1 - t_{LTD})/\tau_1 - T(\tau_1 - t_{LTD})/\tau_1]
\]

\[
U(t) = \begin{cases} 0, & t < t_{LTD} \\ 1, & t_{LTD} \leq t \leq t_{LTD} + 10 \text{ ms} \\ 0, & t > t_{LTD} + 10 \text{ ms} \end{cases}
\]

\[
C(t) = T((t - \tau)/\tau) - T((t - \tau - \max(t_{CS_{min}}, t_{LTD} + 10 \text{ ms}))/\tau)
\]

\[
R_{PKj}(t) = r_{PKj,b} + C(t) \int_{-\infty}^{t} S(t' - t) U(t') dt'
\]

where \(t_{LTD}\) is the interstimulus interval (ISI) between the CS and US onset times, \(t_{LTD} = -10\) ms and \(t_{LTD} = 75\) ms, respectively, set the minimum and maximum allowable delay between CS-driven parallel fiber and US-driven climbing fiber activity for induction of LTD, and \(\tau = 10\) ms is a characteristic time describing the smooth
CS-driven modulation of the rate of mossy fiber spiking was also constrained by data from in vivo electrophysiological recordings and was expressed as

$$R_{MF}(t) = r_{MF,b} + (r_{MF,CS} - r_{MF,b}) C(t)$$

where $r_{MF,b} = 10$ Hz is the background firing rate for mossy fibers and $r_{MF,CS} = 50$ Hz is the spiking rate of mossy fibers during presentation of the conditioning stimulus (Freeman Jr and Nicholson 1999; Nicholson and Freeman Jr 2002).

**Model 1: a single-compartment model of DCN neurons**

We modeled a DCN cell with a single electrical compartment that included leak ($I_L$) and T-type Ca$^{2+}$ ($I_{T}$) currents, as well as synaptic currents due to inputs from Purkinje cells ($I_{syn,Pkj}$) and mossy fibers ($I_{syn,MF}$). Membrane voltage dynamics were determined by time integration of the current balance equation: $C_m(dV/dt) = -I_T - I_L - I_{syn,Pkj} - I_{syn,MF}$. The passive current, $I_L = g_L(V - V_L)$, was an admixture of two components: a tonic mixed-cation current that is characteristic of DCN cells and has a $-30$ mV reversal potential (Raman et al. 2000) and a standard leak current with $-75$ mV reversal potential (Jahnsen 1986b; Llinás and Muhlethaler 1988). Total leak conductance, $g_L$, and leak reversal potential, $V_L$, were determined by the DCN cell’s resting potential of $V_{rest} = -58$ mV (Aizenman and Linden 1999; Llinás and Muhlethaler 1988), and the observed membrane time constant of about 12 ms (Jahnsen 1986a; Llinás and Muhlethaler 1988)

$$g_L = C_m/\tau_m - \sum_i I_i,$$

where $g_L$ and $I_i$ are, respectively, the steady-state conductance and current density at $V_{rest}$ for each of the active conductances, and $I_{syn}$ represents the steady-state synaptic current densities determined by $V_{rest}$ and the background rate of spiking of each type of synaptic input.

Parameter values for Purkinje and mossy fiber synaptic inputs were constrained by physiological measurements: $V_{syn,Pkj} = -75$ mV (Jahnsen 1986b; Llinás and Muhlethaler 1988), $\tau_{syn,Pkj} = 14$ ms (Anchisi et al. 2001), and $V_{syn,MF} = 0$ mV (Anchisi et al. 2001) (Table 1). Glutamatergic synapses in the DCN have significant $\alpha$-amino-3-hydroxy-5-methyl-4-isoxazolepropionic acid (AMPA) and N-methyl-d-aspartate (NMDA) components (Anchisi et al. 2001). As a simplification, $\tau_{syn,MF}$ for mossy fibers was chosen to be 23 ms by weighting the AMPA and NMDA decay time constants at $-60$ mV by the measured relative amplitudes of AMPA and NMDA glutamatergic input (Anchisi et al. 2001). T-current was the sole voltage-dependent current:

$$\tau_m = 0.287 + 0.0711 \cdot \exp(-V/15.8)$$

$$\tau_t = 5.96 + 0.00677 \cdot \exp(-V/7.85)$$

$$n_s = \{1.00 + \exp([- (V + 42.0)/4.25])^{-1}$$

$$I_s = \{1.00 + \exp([V + 63.0]/3.50])^{-1}$$

where in this and all subsequent expressions numerical parameters with dimensions of time and voltage are expressed in units of milliseconds and millivolts, respectively.

Figure 2: Cerebellar memory formation based on temporally sparse granule cell coding and bidirectional plasticity at the PF–Purkinje cell synapse. A: the relative timing of PF and CF activation sets the propensity toward long-term depression (LTD) or long-term potentiation (LTP). Maximal LTD induction arises when PF activity precedes CF activity by up to a time, $t_{LTD}$, of about 75 ms, but LTD can also occur when CF activity slightly precedes PF activity (Coehmans et al. 2004; Wang et al. 2000). B: in classical eyelink conditioning, individual PFs are assumed to exhibit elevated activity during only a brief portion of the CS. By the plasticity rule in A, some PF inputs will be strengthened and others depressed, depending on the relative timing of PF and US-driven CF activity. DCN cells receive input from populations of Purkinje cells whose activity reflects aggregate input from CS-activated PFs. C: repeated CS–US training (top) leads to biphasic CS-driven Purkinje cell spiking due to the bidirectional plasticity shown in B. In subjects that received forward training (bottom left), spiking rises and then falls relative to baseline (red curve). In subjects that received backward training (bottom right), spiking falls and then rises (blue curve). The red arrows (bottom left) correspond to $t_{LTD}$-temporal evolution of neural dynamics. We used the smoothing function $T[x]$, to ensure gradual changes in spike rates

$$T[x] = \begin{cases} 0 & x < -1 \\ [1 + \cos(\pi x)]/2 & -1 \leq x < 0 \\ 1 & x \geq 0 \end{cases}$$

The constants $A_1$ and $A_2$ were set such that the minimum and maximum Purkinje cell firing rates for a long ISI were $r_{Pkj,d} = 20$ Hz and $r_{Pkj,f} = 100$ Hz, respectively (Table 1) (Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006). These plasticity rules led to gradual transitions between distinct average firing rate values over intervals of about 20 ms, approximating the observed intervals over which Purkinje cells modulate their spiking rates during expression of motor learning (Berthier and Moore 1986; King et al. 2001).
chose subsequent single-compartment simulations (Models 1 and 2) we
sensitive to the value of the T-type conductance density. In all
indicating that the occurrence of postinhibitory rebound is not highly
conductance values over which rebound depolarizations occurred,
However, in initial simulations we identified a broad range of T-type
tion of total T-type conductance from somatic recordings is difficult.
Thus, estimation of total T-type conductance in Models 1 and 2
0.5 mS/cm², within the middle of this identified range.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
<th>Model(s)</th>
<th>Reference(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$g_{syn,Pkj}$</td>
<td>Maximum high-voltage-activated Ca²⁺ conductance in Model 3, somatic compartment</td>
<td>0.15 mS/cm²</td>
<td>3</td>
<td>Mainen and Sejnowski 1996</td>
</tr>
<tr>
<td>$g_{syn,MF}$</td>
<td>Maximum high-voltage-activated Ca²⁺ conductance in Model 3, dendritic compartment</td>
<td>0.15 mS/cm²</td>
<td>3</td>
<td>Mainen and Sejnowski 1996</td>
</tr>
<tr>
<td>$g_{SK}$</td>
<td>Maximum Ca²⁺-dependent K⁺ conductance</td>
<td>32 µS/cm²</td>
<td>3</td>
<td>Aizenman and Linden 1999; Llinás and Muhlethaler 1988</td>
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<td>$g_{Na}$</td>
<td>Maximum Hodgkin-Huxley type fast Na⁺ conductance</td>
<td>144 µS/cm²</td>
<td>3</td>
<td>Aizenman and Linden 1999; Llinás and Muhlethaler 1988</td>
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<tr>
<td>$g_{Kv}$</td>
<td>Maximum Hodgkin-Huxley type K⁺ conductance</td>
<td>56 mS/cm²</td>
<td>3</td>
<td>Aizenman and Linden 1999; Llinás and Muhlethaler 1988</td>
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<td>$\tau_m$</td>
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<td>Jähnse 1986b; Llinás and Muhlethaler 1988</td>
</tr>
<tr>
<td>$\tau_{syn,Pkj}$</td>
<td>GABAergic synaptic time constant</td>
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<td>1,2,3</td>
<td>Archi et al. 2001</td>
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<tr>
<td>$\tau_{syn,MF}$</td>
<td>Glutamatergic synaptic time constant</td>
<td>23 ms</td>
<td>1,2,3</td>
<td>Archi et al. 2001</td>
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<td>$N_{syn,Pkj}$</td>
<td>Number of Purkinje cell inputs</td>
<td>50</td>
<td>2,3</td>
<td>Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006</td>
</tr>
<tr>
<td>$N_{syn,MF}$</td>
<td>Number of mossy fiber inputs</td>
<td>10</td>
<td>2,3</td>
<td>Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006</td>
</tr>
<tr>
<td>$R$</td>
<td>Ratio of Purkinje to mossy fiber inputs</td>
<td>5</td>
<td>2,3</td>
<td>Mainen and Sejnowski 1996; Pinsky and Rinzel 1994</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Percentage of membrane surface area occupied by somatic compartment</td>
<td>5%</td>
<td>3</td>
<td>Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006</td>
</tr>
</tbody>
</table>

The symbol, description, value, and literature citations are given for each parameter in Models 1–3 of DCN cells.

Unfortunately, several DCN cellular parameters could not be tightly constrained by biophysical data. T-type channels appear to be most dense in DCN cell distal dendrites (Gauck et al. 2001). Thus, estimation of total T-type conductance from somatic recordings is difficult. However, in initial simulations we identified a broad range of T-type conductance values over which rebound depolarizations occurred, indicating that the occurrence of postinhibitory rebound is not highly sensitive to the value of the T-type conductance density. In all subsequent single-compartment simulations (Models 1 and 2) we chose $g_T = 0.5$ mS/cm², within the middle of this identified range.

The weight of Purkinje cell synaptic input, $W_{syn,Pkj} = 0.2$ mS/cm², was chosen to be near the middle of a range of values capable of inducing physiological 10 to 15 mV changes in membrane voltage when input firing rates were modulated. The mossy fiber synaptic conductance weight, $W_{syn,MF} = 4$ µS/cm², was chosen such that mossy fiber input alone was insufficient to drive the cell to rebound. Without this stipulation there would be little dependence of learned responses on Purkinje cell input, contrary to experimental findings. In Model 1 all synaptic inputs were simulated in a deterministic fashion. Each synaptic conductance density, $g_{syn}()$, was determined by con-
volved the input spike rate with an exponential function of time constant $\tau_{syn}$ and amplitude $W_{syn}$, which represented the conductance response (Table 1).

**Model 2: a single-compartment model of dendritic $\text{Ca}^{2+}$ spiking**

Model 2 was the same as Model 1 but with two modifications. First, we added a high-voltage-activated (HVA) $\text{Ca}^{2+}$ current, so we could study how graded T-current-mediated rebound depolarizations led to the initiation of HVA $\text{Ca}^{2+}$ spikes. The conductance model for $I_{TVA}$ was identical to that used by Mainen and Sejnowski (1996). Second, membrane voltage dynamics were no longer deterministic. Instead, the time-varying synaptic conductance density was determined by the stochastic arrival of action potentials at times selected independently, as governed by Poisson statistics and the instantaneous spike rate. The number of Purkinje cell ($N_{syn,Pkj} = 50$) and mossy fiber ($N_{syn,MF} = 10$) inputs roughly matched the ratio, $R$, of GABAergic to glutamatergic synapses found in the DCM (Chan-Palay 1973) (Table 1). The occurrence of a presynaptic spike on any of these independent individual inputs led to an instantaneous jump in synaptic conductance of amplitude $W_{syn,Pkj}/N_{syn,Pkj}$ or $W_{syn,MF}/N_{syn,MF}$, which then declined exponentially with time constant $\tau_{syn,Pkj}$ or $\tau_{syn,MF}$, respectively (Table 1).

**Model 3: a two-compartment model of DCN neurons**

A DCN cell model with dendritic and somatic compartments was used to test the effect of rebound conductances on $\text{Na}^{+}$ spiking output. The potentials of dendritic ($V_d$) and somatic ($V_s$) membranes were determined by the currents flowing in each compartment (Pinsky and Rinzel 1994)

$$C_m \frac{dV_d}{dt} = -I_L - I_T - I_{HVA} - I_{TVA} - I_{syn,Pkj} - I_{syn,MF} - \frac{g_L(V_d - V)}{1 - \rho}$$

$$C_m \frac{dV_s}{dt} = -I_L - I_T - I_{HVA} - I_{TVA} - I_{Kv} - I_{Na} - \frac{g_L(V_s - V)}{\rho}$$

where the coupling between the two compartments was specified by the conductance between compartments, $g_c$, and the ratio of somatic membrane surface area to total cell surface area, $\rho$. The passive current, $I_L$, was determined independently in both compartments from $V_{rest} = -58 \text{ mV}$ and the membrane time constant $\tau_m = 12 \text{ ms}$. The somatic compartment exhibited spontaneous $\text{Na}^{+}$ spiking, so we determined $I_L$ by setting the $I_{Na}$ gating variables to $m_{\infty}(V_{rest})$ and $h_\infty(V_{rest})$, and the $I_{Kv}$ gating variable to $n_{\infty}(V_{rest})$. Stochastically arriving synaptic currents entered the dendritic compartment. For computational ease, we modeled the spike rate of Purkinje cells using a simple formula that closely approximates the rate function used in Models 1 and 2

$$R_{PKJ}(t) = r_{PKJ} + C(t) \left[ \frac{r_{PKJ} - r_{PKJ} + (r_{PKJ} - r_{PKJ})}{T(1 + \tau_{syn} + \tau_{LTD} / \tau_{syn} + \tau_{LTD})} \right]$$

Active somatic currents were T-type $\text{Ca}^{2+}$, high-voltage-activated $\text{Ca}^{2+}$ ($I_{TVA}$; Gauck et al. 2001), $\text{Ca}^{2+}$-activated $K^+$ ($I_{SK}$; Raman et al. 2000), fast $\text{Na}^{+}$ ($I_{Na}$), and delayed rectifying $K^+$ ($I_{Kv}$). The simulation used the total $\text{Ca}^{2+}$ current, $I_{Ca}$, to determine the internal $\text{Ca}^{2+}$ concentration, which controlled the gating of $I_{SK}$. In addition to $I_L$, the dendrite had T-type currents (Gauk et al. 2001), $I_{TVA}$ (at half the density as in the soma; see Gauck et al. 2001), $I_{SK}$, and synaptic input. Conductance models for $I_{HVA}$, $I_{TVA}$, $I_{Kv}$, and $I_{Ca}$ were identical to those used by Mainen and Sejnowski (1996), including parameter values.

$I_{Na}$ was based on the model of Mainen and Sejnowski (1996) (see also Hines and Carnevale 2001; Schaefer et al. 2007). For $\text{Na}^{+}$ channel activation, $\psi = 3$ with kinetics determined by

$$\alpha_{Na} = 0.182(V + 31)/(1 - \exp[-(V + 31)/9])$$

$$\beta_{Na} = -0.124(V + 31)/(1 - \exp[(V + 31)/9])$$

For $\text{Na}^{+}$ channel inactivation, $\psi = 1$ and

$$\tau_{Na} = (\phi_{Na}[0.024(V + 48)/(1 - \exp[-(V + 48)/5])] - 0.0091(V + 73)/(1 - \exp[(V + 73)/5]))^{-1}$$

$$y_{Na} = [1 + \exp[(V + 64)/6.2]]^{-1}$$

Conductance densities and the voltage dependence of $I_{Ca}$, gating were chosen to reproduce the observed tonic DCN cell firing rate of about 25 Hz (Aksevov et al. 2005; Jahnsen 1986a; Raman et al. 2000) and spike width of about 1.5 ms (Aizenman and Linden 1999; Llinás and Mulheflaher 1988). Reversal voltages were $V_{Na} = 50 \text{ mV}$, $V_{K} = -90 \text{ mV}$, and $V_{Ca} = 140 \text{ mV}$ (Jahnsen 1986b; Mainen and Sejnowski 1996).

Coupling parameters, $g_c = 0.53 \mu \text{S/cm}^2$ and $\rho = 0.05$, were chosen to ensure each compartment had relatively independent dynamics while still permitting dendritic voltage deflections to affect somatic spiking. Synaptic weights were set by the same criteria as for the one-compartment models, with $W_{syn,Pkj} = 0.2 \mu \text{S/cm}^2$ and $W_{syn,MF} = 4 \mu \text{S/cm}^2$. As in Models 1 and 2, in the dendrite $\bar{g}_{TVA} = 0.5 \mu \text{S/cm}^2$ was set near the middle of a broad range of values that allowed rebound depolarization. In the soma $\bar{g}_{TVA} = 5 \mu \text{S/cm}^2$, reflecting the lower density of low-voltage-activated $\text{Ca}^{2+}$ channels in this compartment (Gauck et al. 2001). The densities of $\text{Ca}^{2+}$-activated $K^+$ conductance, $\bar{g}_{SK} = 32 \mu \text{S/cm}^2$, and of high-voltage-activated $\text{Ca}^{2+}$ conductance in the soma, $\bar{g}_{TVA} = 0.3 \mu \text{S/cm}^2$, and dendrite, $\bar{g}_{HVA} = 0.15 \mu \text{S/cm}^2$, had scarcely any effect on the probability of HVA $\text{Ca}^{2+}$ spiking in response to synaptic inputs across a broad range of conductance densities and were chosen to reduce the duration of the $\text{Ca}^{2+}$ spike to physiologically realistic values (Jahnsen 1986b; Llinás and Mulheadrle 1988). Hodgkin-Huxley conductances, $\bar{g}_{Na} = 144 \mu \text{S/cm}^2$ and $\bar{g}_{Kv} = 56 \mu \text{S/cm}^2$, were chosen to reproduce the experimental observation of spontaneous spiking in the soma at $V_{rest} = -58 \text{ mV}$.

**Phase plane analysis of rebound depolarizations**

To study whether a memory recall mechanism based on rebound depolarization would be robust, we reduced Model 1 to a system of two dynamical degrees of freedom amenable to graphical phase plane analysis. This involved an approximation in which the T-type activation variable was set equal to its asymptotic value, $n = n_{\infty}(V)$, reducing the dynamical variables to only the T-type inactivation variable ($l$) and the membrane voltage ($V$). Because this approximation increased the membrane excitability, resulting in larger magnitude rebounds, we decreased the density of T-type $\text{Ca}^{2+}$ channels to $\bar{g}_{TVA} = 0.3 \mu \text{S/cm}^2$ as a compensatory measure. The system’s dynamical trajectories within the ($V$, $l$) phase plane could then be fruitfully studied by determination of the two nullclines, on which the time derivatives vanish

$$\frac{dl}{dt} = 0 \rightarrow l = L(V)$$

$$\frac{dV}{dt} = 0 \rightarrow l = \frac{g_L(V - V_L) + \bar{I}_{syn,Pkj}(V) + \bar{I}_{syn,MF}(V)}{\bar{g}_{TVA}(V - V_C)}$$

where the Purkinje cell and mossy fiber synaptic input currents $I_{syn}(V) = g_{syn}(V - V_{syn})$ represent the mean synaptic currents as determined from the synaptic weights and background firing rates.
Both time derivatives vanish at the intersection point of the two nullclines, so this is a fixed-point of the dynamics. Fixed-points during the neuronal resting state (stage 1), the CS–US interstimulus interval up until \(t_{ISI} \) before the expected US onset (stage 2), and the remaining portion of the CS (stage 3), were found using the MATLAB function \texttt{fzero} to solve for the intersection of the nullclines. Linear stability analysis within a neighborhood of the resting state (stage 1) fixed-point at \( V = -58 \) mV revealed that this fixed-point is stable for \( \bar{g}_T < 1.28 \) mS/cm\(^2\). The dynamical trajectories near this fixed-point exhibit damped oscillations for \( \bar{g}_T \geq 0.20 \) mS/cm\(^2\). The density of T-type channels used in our studies (Table 1) results in a stable spiral fixed-point.

A map of rebound magnitudes in the phase plane (Fig. 6C) was built by numerically integrating the equations of motion using MATLAB’s Runge–Kutta initial-value differential equation solver, \texttt{ode45}. A series of evenly spaced initial points was chosen along the boundary lines of the phase plane, defined by \( V = -72 \) mV and \( I = 0 \), and trajectories were integrated forward in time using the current balance equation across the constant synaptic input values of stage 3. Integration proceeded until the trajectories reached the stage 3 fixed-point. Each trajectory formed a contour (level curve) on the phase plane map with the contour amplitude given by the maximum depolarization achieved on that trajectory.

To determine the voltage threshold curve for firing all-or-none Ca\(^{2+}\) spikes (Fig. 6D), we added a high-voltage-activated (HVA) Ca\(^{2+}\) conductance (Mainen and Sejnowski 1996) to the phase plane treatment of Model 1 in which \( n \) relaxes instantaneously to its asymptotic value, \( n = n_{\infty}(V) \) (Fig. 6, A–C). This yielded a deterministic version of Model 2 that produced virtually the same trajectories as those of Model 1 over the voltage range, \( V < -35 \) mV, in which the HVA channels are largely closed (Fig. 6D). As before, the instantaneous activation of T-type currents led to increased membrane excitability, for which we compensated by decreasing the density of T-type Ca\(^{2+}\) channels to \( \bar{g}_T = 0.3 \) mS/cm\(^2\) and the density of HVA Ca\(^{2+}\) channels to \( \bar{g}_{HVA} = 0.09 \) mS/cm\(^2\). We solved for the dynamical trajectories by integrating the equations of motion forward in time starting at a series of initial points distributed along two boundary lines of the phase plane, defined by \( V = -72 \) mV and \( I = 0 \). The trajectories fell into two classes depending on whether the T-current-mediated rebound was of sufficient magnitude to cross the threshold for generation of a HVA Ca\(^{2+}\) spike.

**Phase plane movies showing model trajectories**

Movies of deterministic (Movies S1 and S2 using Model 1) and stochastic (Movie S3 using Model 2) voltage trajectories were created in MATLAB.\(^1\) As in the phase plane analysis of Fig. 6, Movies S1 and S2 relied on the mathematical approximation of instantaneous relaxation of the T-channel activation variable to its asymptotic value. The motion of the \( V \) nullcline was determined by solving the equation \( dV/dt = 0 \) for \( t \), using the steady-state values of the synaptic conductances, \( g_{syn} \), that would be attained given constant Purkinje cell and mossy fiber spiking at rates equal to their instantaneous values. Numerical integration of the current balance equation used a maximum timestep of 0.1 ms. In Movie S3 the synaptic conductances were modulated by the independent but stochastic arrivals of spikes from 50 Purkinje cells and 10 mossy fibers.

**Single-compartment model of MVN neurons**

We created a simple one-compartment model of MVN cells (Table 2) obeying the current balance equation, \( C_m(dV/dt) = -I_L - I_h - I_{syn,Pkj} - I_{syn,MF} \), in which the reversal potential and conductance values for the leak current, \( I_L = g_L(V - V_L) \), were determined by the membrane time constant (12 ms), the resting potential (−58 mV), and

\[ I_h = g_h(V - V_h) \]

where \( V_L = -20 \) mV is the mixed-cation reversal potential (Dickson et al. 2001; Pape 1996) and \( g \) is the activation variable. Synaptic inputs were modeled in a deterministic fashion, as in Model 1 above, with synaptic time constants \( \tau_{syn,Pkj} = 8.9 \) ms and \( \tau_{syn,MF} = 5.5 \) ms (Chun et al. 2003) and synaptic weights \( W_{syn,Pkj} = 0.5 \) mS/cm\(^2\) and \( W_{syn,MF} = 4 \) μS/cm\(^2\).

Measured h-current time constants vary broadly across cell types, but detailed measurements of h-current in MVN cells have not yet been made. The HCN2 isoform appears to be the predominant subtype of h-channel in the vestibular nuclei (Santoro et al. 2000), and the kinetics of this isoform are consistent with the activation time constant of hyperpolarization-activated rebound burst firing in the MVN, measured to be \( \approx 620 \) ms at 31°C (Sekirnjak and du Lac 2002).

Following Sekirnjak and du Lac (2002) we modeled \( I_h \) kinetics with a fixed time constant, \( \tau_h \). To determine the steady-state voltage dependence for HCN2 we fit measurements of total h-current obtained in a Xenopus oocyte expression system (see Fig. 9C in Santoro et al. 2000)

\[ q_h = \left[ 1.00 + \exp\left( \frac{V + 78}{5.53} \right) \right]^{-1} \]

\( \bar{g}_h = 3 \) mS/cm\(^2\) was chosen to be within a range of values that produced rebound depolarization. We used \( \tau_h = 400 \) ms for MVN simulations shown in Fig. 7, C and E, because this value approximated the time constant that generated the largest ratio of rebound amplitude between the long ISI condition and the zero ISI condition. Rebound amplitude in the zero ISI condition varied by only about 3 mV across a wide range of time constants, 50 ms \( \leq \tau_h \leq 1,000 \) ms.

**Linear–nonlinear (LN) model of lock-and-key mechanism**

For our algorithmic description of memory retrieval we generated a set of “key” activity patterns, \( K(t) \), using the CS-driven waveforms for the instantaneous Purkinje cell spike rates arising for ISI values ranging from 0 to 200 ms. The Purkinje cell spiking rates were the same as those for biophysical Model 1. We created a linear filter

\[ F(t) = \frac{1}{Z} \left[ -T \left( \frac{t - \tau}{\tau} \right) - T \left( \frac{t - t_F - \tau}{\tau} \right) \right] \]

\[ + \frac{2}{3} \left[ T \left( \frac{t - t_F - \tau}{\tau} \right) - T \left( \frac{t - 2t_F - \tau}{\tau} \right) \right] \]

where \( Z \) is a normalization constant chosen to be the maximum absolute value of the linear response, \( T[t] \) is the smooth transition function (see General stimulation procedures), \( t_F = 20 \) ms, and \( \tau = 10 \) ms. The filtered key activity was determined by the convolution

\[ x(t) = \int_0^t K(t') F(t - t') \, dt' \]

Finally, this signal was passed through an exponential nonlinearity, \( M(t) = G[x(t)] = \exp(h \ast x(t)) \), where \( h = 12 \) is a gain factor. The response amplitude for a given ISI value (Fig. 8E) was determined by the peak value of \( M(t) \) normalized by the amplitude attained for a long ISI of 200 ms.

**RESULTS**

**A theoretical framework for cerebellum-dependent learning and memory**

Cerebellar granule cells number in the tens of billions but individually appear to be rarely active, producing only a few spikes at a time in response to mossy fiber input (Chadderton...
et al. 2004). Such transient activation implies that after behavioral training and plasticity induction at PF–Purkinje cell synapses, presentation of a learned sensory cue should drive a biphasic modulation of population Purkinje cell activity (Fig. 2). For example, in classical conditioning transient CS-driven granule cell activity that is concurrent with US-driven CF activity will lead to LTD at PF–Purkinje cell synapses (Fig. 2). For example, in classical conditioning transient CS-driven granule cell activity that is concurrent with US-driven CF activity will lead to LTD at PF–Purkinje cell synapses (Fig. 2). We studied whether forward and backward patterns of biphasic Purkinje cell spiking could lead to distinct patterns of rebound activity in DCN cells after presentation of a classically conditioned stimulus. We created a series of compartmental DCN cell models that received inputs from both Purkinje cells and mossy fibers and we interpreted the resulting rebounds as the initiators of conditioned motor responses. The simplest model (Model 1) had one electrical compartment, lacked fast spiking capability, and had only leak, T-type, and synaptic

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
<th>Reference(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( C_m )</td>
<td>Membrane capacitance</td>
<td>1 ( \mu F/cm^2 )</td>
<td>du Lac and Lisberger 1995b; Straka et al. 2005</td>
</tr>
<tr>
<td>( V_{rest} )</td>
<td>Resting membrane potential</td>
<td>-58 mV</td>
<td>Hille 2001</td>
</tr>
<tr>
<td>( V_{syn,Pkj} )</td>
<td>GABAergic reversal potential, determined by Cl⁻ gradient</td>
<td>-75 mV</td>
<td></td>
</tr>
<tr>
<td>( V_{syn,MF} )</td>
<td>Glutamatergic reversal potential</td>
<td>0 mV</td>
<td>Chun et al. 2003</td>
</tr>
<tr>
<td>( V_a )</td>
<td>( I_{l_m} ) mixed-cation reversal potential</td>
<td>-20 mV</td>
<td>Dickson et al. 2001; Pape 1996</td>
</tr>
<tr>
<td>( r_{Pkj,b} )</td>
<td>Background Purkinje cell spike rate</td>
<td>40 Hz</td>
<td>Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006</td>
</tr>
<tr>
<td>( r_{Pkj,d} )</td>
<td>Reduced Purkinje cell spike rate due to LTD of parallel fiber inputs</td>
<td>20 Hz</td>
<td>Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006</td>
</tr>
<tr>
<td>( r_{Pkj,p} )</td>
<td>Elevated Purkinje cell spike rate due to LTP of parallel fiber inputs</td>
<td>100 Hz</td>
<td>Berthier and Moore 1986; Jirenhed et al. 2007; Kotani et al. 2006</td>
</tr>
<tr>
<td>( r_{MF,b} )</td>
<td>Background mossy fiber spike rate</td>
<td>10 Hz</td>
<td>Freeman Jr and Nicholson 1999; Nicholson and Freeman Jr 2002</td>
</tr>
<tr>
<td>( r_{MF,CS} )</td>
<td>Mossy fiber spike rate during head rotation</td>
<td>50 Hz</td>
<td>Freeman Jr and Nicholson 1999; Nicholson and Freeman Jr 2002</td>
</tr>
<tr>
<td>( g_{h} )</td>
<td>Maximum h-type cation conductance</td>
<td>3 mS/cm²</td>
<td></td>
</tr>
<tr>
<td>( W_{syn,Pkj} )</td>
<td>Maximum total conductance of Purkinje cell synapses</td>
<td>0.5 mS/cm²</td>
<td></td>
</tr>
<tr>
<td>( W_{syn,MF} )</td>
<td>Maximum total conductance of mossy fiber synapses</td>
<td>4 mS/cm²</td>
<td></td>
</tr>
<tr>
<td>( \tau_m )</td>
<td>Membrane time constant</td>
<td>12 ms</td>
<td>Chun et al. 2003</td>
</tr>
<tr>
<td>( \tau_{syn,Pkj} )</td>
<td>GABAergic synaptic time constant</td>
<td>8.9 ms</td>
<td>Chun et al. 2003</td>
</tr>
<tr>
<td>( \tau_{syn,MF} )</td>
<td>Glutamatergic synaptic time constant</td>
<td>5.5 ms</td>
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<tr>
<td>( \tau_s )</td>
<td>h-current activation time constant</td>
<td>400 ms</td>
<td></td>
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The symbol, description, value, and literature citations are given for each parameter used in simulations of MVN cells.
FIG. 3. Compartimental modeling of T-type Ca\(^{2+}\) current rebounds in DCN cells. Compartmental simulations of a Purkinje target neuron in the DCN involved 3 models of increasing complexity. A: Model 1 has one electrical compartment, contains T (\(g_T\)) and leak (\(g_L\)) conductances, and receives glutamatergic mossy fiber and GABAergic Purkinje cell inputs. Membrane voltage follows a deterministic time course. B: Model 2 adds high-voltage-activated Ca\(^{2+}\) (\(g_{HVA}\)) channels. Synaptic inputs arrive stochastically, leading to membrane potential fluctuations and nondeterministic dynamics. C: Model 3 has dendritic and somatic compartments, coupled by a conductance \(g_c\). Synaptic inputs are localized to the dendrite, approximating empirical findings. The soma has fast Na\(^{+}\) (\(g_{Na}\)) and delayed rectifier K\(^{+}\) (\(g_{K}\)) conductances. Both compartments have leak, T, Ca\(^{2+}\)-activated K\(^{+}\) (SK), and HVA Ca\(^{2+}\) conductances. Synaptic inputs arrive stochastically, leading to nondeterministic dynamics. D: voltage dependence of the activation (dashed red curve) and inactivation (solid blue curve) gating variables for the T-type conductance in DCN neurons. At the resting potential (about −58 mV, dashed vertical line), T-currents are largely inactivated. Hyperpolarization deactivates T-currents, allowing activation during subsequent depolarization. E: voltage dependence of the T-channel activation (dashed red curve) and inactivation (solid blue curve) time constants. Parameter dependencies in D and E are based on Gauck et al. (2001) and McRory et al. (2001).

Conductances (Fig. 3A). This allowed us to focus initially on rebound generation, apart from issues studied later concerning membrane potential noise and downstream readout. Kinetic parameters for T-currents were obtained from in vitro measurements in DCN cells (Gauck et al. 2001; McRory et al. 2001). Deactivation can occur within about 20–100 ms of hyperpolarization from the resting potential and activation can then occur within a few milliseconds during subsequent depolarization (Fig. 3, D and E). Conductance densities were set to reproduce the observed resting potential of −58 mV and membrane time constant of about 12 ms (Aizenman and Linden 1999; Jahnsen 1986a; Llinás and Muhlethaler 1988).

We compared the model’s responses to forward and backward patterns of biphasic Purkinje cell input. In our initial studies, the forward CS–US interstimulus interval (ISI) was ≥200 ms, more than sufficient delay for reliable conditioning in rabbits (Fig. 1B) (Ohyama et al. 2003b). Mossy fiber excitation rose during the entire CS but was insufficient to drive a rebound during baseline or elevated Purkinje cell spiking. This is consistent with data supporting a key role for Purkinje cells in generating properly timed flexes via the suppression of early, mossy fiber-driven responses to the CS, which can be unveiled by blocking Purkinje cell inputs to the DCN (Ohyama and Mauk 2001; Perrett et al. 1993). We found that biphasic Purkinje cell input shaped by forward training led to rebounds that initiated as Purkinje cell spiking transitioned from an elevated to a diminished rate, about \(t_{LTD}\) prior to the expected US onset (Fig. 4A, red traces). Hence, rebounds could drive blinks that anticipate the US. We then tested the effect of varying the ISI value. With backward training there was insufficient deinactivation of T-currents to generate rebounds (Fig. 4A, blue traces). With positive ISI values <100 ms, rebounds occurred but with diminished amplitude, since there was insufficient time for T-channel deinactivation during the brief increase in Purkinje cell spiking (Fig. 4A, orange trace). Thus, rebound generation occurred selectively for sufficiently positive ISI values and anticipated US arrival.

We also explored the dependence of rebound generation on the graded magnitude of LTD and LTD at the PF–Purkinje cell synapse, as quantified through the resulting elevation and diminution in Purkinje cell spike rates, respectively (Fig. 4, B.

FIG. 4. DCN cell rebounds require a minimum CS–US ISI and sufficient expression of cerebellar LTD and LTD. A: the time course of CS-driven depolarization in Model 1 (Fig. 3A). If prior training involved a sufficiently positive ISI, the CS-driven rebound is of large amplitude and occurs at a time approximately \(t_{LTD}\) before the expected US (red traces). If training involved an insufficient ISI value, CS-driven rebounds do not occur (blue traces). For short ISI values, rebounds are diminished in amplitude (orange trace). The color bar indicates the ISI values, which are also marked above the graph with the color corresponding arrowheads for each voltage trace. Rebounds occur prior to the expected US, indicating anticipatory responses. B: rebound amplitude varies with the degree to which the CS drives biphasic Purkinje cell activity. This, in turn, depends on having sufficient expression of both PF–Purkinje cell LTP and LTD (Fig. 2). Driving a large-amplitude rebound in the DCN cell requires that during the first phase of biphasic activity the Purkinje cell spiking rate rises well above the spontaneous frequency of 40 Hz. The 3 voltage traces (blue, cyan, red) in B1 occurred with the color corresponding. Purkinje cell peak spiking rates shown in B2. Lower peak spiking rates reflect lower expression levels of LTD. The arrowhead indicates the ISI value of 200 ms. C: driving a large-amplitude rebound in the DCN cell also requires that during the second phase of biphasic activity the Purkinje cell spiking frequency drops below the 40 Hz spontaneous rate. The 3 voltage traces in C1 (blue, cyan, red) were created using the color corresponding. Purkinje cell minimum spiking rates shown in C2. The higher rates reflect lesser degrees of LTD. The arrowhead indicates the ISI value of 200 ms.
Rebound generation in the DCN cell required biphasic Purkinje cell spiking, with both a sufficient elevation and subsequent decline in spiking needed for large-amplitude rebounds (~50 mV). Ample levels of both LTP and LTD would thus be needed to induce sufficient biphasic variation in Purkinje cell spiking. These findings held across a broad range of T-channel densities, opening the possibility that DCN cell T-currents help shape the differences in conditioned reflex expression following backward and forward training (Ohyama et al. 2003b).

Readout mechanisms of rebound depolarization and correspondence to conditioned behavior

If rebounds induce learned motor action, how do DCN cells convey rebound magnitudes via the rate of Na⁺ spikes sent to premotor areas? The graded amplitude of pure T-current-mediated rebounds indicates these low-voltage-activated events are not stereotyped Ca²⁺ spikes. Real DCN neurons do exhibit Ca²⁺ spikes, mediated by high-voltage-activated Ca²⁺ channels and, as in other cell types, dendritic Ca²⁺ spikes may be good triggers of somatic Na⁺ spike bursts (Jahnsen 1986b; Llinás and Muhlethaler 1988). We reasoned that the amplitude of T-current-mediated rebounds should set the likelihood of crossing the voltage threshold for Ca²⁺ spike generation, with membrane potential fluctuations influencing the degree of variability. Smaller-amplitude rebounds that occur with shorter ISI values would be less likely to cross the Ca²⁺ spike threshold. Within this framework we interpret a Ca²⁺ spike as the initiator of signals sent downstream to drive a conditioned motor response.

To test whether this readout mechanism would be able to convert the amplitude of rebound depolarization into the probability of Ca²⁺ spike generation, we examined an enhanced one-compartment model that included high-voltage-activated Ca²⁺ channels (Model 2, Fig. 3B) and membrane potential fluctuations due to stochastic arrival of synaptic inputs (METHODS). This contrasts with Model 1, in which both synaptic inputs and membrane voltage followed deterministic time courses. In Model 2 a biphasic pattern of Purkinje cell input resulting from forward training with a long ISI value led reliably to a T-current-mediated rebound of sufficient magnitude to trigger a Ca²⁺ spike. These Ca²⁺ spikes were properly timed, prior to the expected US. Backward training led to small rebounds and virtually no Ca²⁺ spiking. Forward training with a short ISI value led to unreliable Ca²⁺ spiking, with the amplitude of the T-current-mediated rebound being sufficient to trigger a Ca²⁺ spike on some trials but not others (Fig. 5A). Thus, as the ISI value varied, the amplitude of T-current-driven rebounds set the probability of crossing the Ca²⁺ spike threshold (Fig. 5B, closed green triangles). Of prime interest, the shape of the curve describing this response probability as a function of the ISI closely resembles that obtained in rabbit eyeblink conditioning studies (Fig. 5B, open red squares, diamonds, and downward facing triangles), validating the plausibility of a rebound-based recall mechanism. The sum of tLTD and the T-channel inactivation time constant determine the temporal offset of the curve from the origin. It follows that experimental manipulations lengthening the time needed for T-channel deactivation during the ISI are predicted by our theory to cause a rightward shift of the behavioral data curve (DISCUSSION).

We examined readout issues in greater depth using a two-compartment model DCN cell (Model 3, Fig. 3C) that included a dendrite and soma, as well as channels mediating dendritic Ca²⁺ and somatic Na⁺ spikes (see METHODS). The somatic and dendritic compartments were only weakly coupled, which was intended to mimic the electrotonic isolation between the cell body and the long distal dendrites of DCN cells where T-channels appear to be most dense, >100 μm from the cell body (Gauck et al. 2001). This is consistent with the observation that Purkinje cell input triggers DCN cell rebounds much more effectively than somatic hyperpolarization of comparable magnitude (Aizenman and Linden 1999). Synaptic inputs in Model 3 arrived stochastically, inducing membrane potential fluctuations. As in real DCN cells, a tonic cation current induced a basal rate of somatic spiking at about 25 Hz (Aksenov et al. 2005; Jahnsen 1986a; Raman et al. 2000). Simulations revealed that a dendritic rebound induces a Ca²⁺ spike, which in turn drives a corresponding increase in the rate of somatic Na⁺ spikes (Fig. 5, C–E). This increase represents a plausible signal from the DCN cell to downstream pathways for driving learned motor output (Fig. 1A). Forward training with an ISI >100 ms virtually always led to such a spike burst. Na⁺ spike bursts occurred with lower probability under the same conditions that failed to produce large-amplitude rebounds in Model 1, such as backward training or forward training with a short ISI. Across ISI values the probability of a Na⁺ spike burst closely matched the behavioral dependence of conditioned blinking on the ISI value as observed in rabbits (Fig. 5B, closed blue circles).
Phase plane analysis of rebound generation as a robust mechanism for recall

To further explore the basic dynamics and robustness of rebound mechanisms, we studied DCN neuronal dynamics using a phase plane analysis of Model 1. Prior applications of such analysis to other neuron types have provided considerable insight into Ca\textsuperscript{2+} spike generation, spike bursting, and transitions between “up” and “down” activity states (Fitzhugh 1960; Loewenstein et al. 2005; Rinzel and Ermentrout 2001; Rush and Rinzel 1994). As is common in phase plane analysis, we focused on the slow dynamic variables that set the relevant timescale. Here, these variables are membrane voltage (V) and the T-type channel inactivation variable (l). The latter has a voltage-dependent time constant of about 10–100 ms (Fig. 3E), close to the minimum ISI for reliable memory retrieval (Fig. 1B). By comparison, the time constant for T-current activation is about 1–10 ms, considerably faster than motor memory recall and rebound depolarization. Because of this separation of timescales we approximated T-type activation as occurring instantaneously and thus restricted to the (V, l) plane. Rebounds may then be viewed as trajectories in this two-dimensional (2-D) phase plane (Fig. 6).

Phase plane analysis of Model 1 revealed the key ingredients for rebounds. The analysis can best be understood by breaking a CS presentation into three stages: the initial resting condition, the ISI, and the remainder of the CS following the ISI (Fig. 6A). During each stage, the system has a unique attractive fixed-point at the intersection of the V and l nullclines, the curves on which the time derivatives dV/dt and dl/dt, respectively, vanish (Fig. 6B). The three fixed-points and the ISI value are the chief determinants of the dynamics. At rest (stage 1), the system resides at a fixed-point location at which the T-current is mainly inactivated (open black circle in Fig. 6B and Movies S1 and S2). At CS onset and during the ISI (stage 2), mossy fiber and Purkinje cell input to the DCN cell shift the fixed-point location to a potential at which the T-channel deactivates (open green triangle in Fig. 6B and Movies S1 and S2). The system approaches the stage 2 fixed-point during the ISI, starting from the resting position (Fig. 6B; Movies S1 and S2). The ISI value determines the duration and proximity of the system’s approach. At about t_{ISI} prior to the moment of the expected US (stage 3), Purkinje cell activity declines and the fixed-point shifts to a third location that is depolarized relative to rest (open red square in Fig. 6B and Movies S1 and S2). This initiates a rebound that is well timed for driving an anticipatory reflex. More precisely, there is a family of trajectories that undergo rebound depolarization during stage 3, with rebound amplitude a strict function of the (V, l) values attained by the end of stage 2. A 2-D color map of rebound amplitude as a function of (V, l) reveals the basis for the sharp dependence on the ISI value and the stage 2 and stage 3 fixed-point locations (Fig. 6C). In turn, these fixed-point locations depend critically on the degree of biphasic Purkinje cell spiking and thus on the levels of LTP and LTD attained during training.

Stage 3 rebound trajectories with the greatest depolarization initiate in a neighborhood of the (V, l) plane that may be viewed as a memory recall “reliability zone” from which a large rebound will occur without fail (Fig. 6C, red shaded region). The level of LTP and the peak Purkinje cell spiking rate are important because they determine the proximity of the stage 2 fixed-point to the reliability zone. However, even with sufficient LTP if the ISI is too brief the system does not have time to reach the reliability zone during stage 2, leading to a small or no rebound (Fig. 6C, blue shaded region; Movie S2). The rebound amplitude also hinges on the location of the stage 3 fixed-point, due to the dependence of T-channel activation on the reduction in Purkinje spike rate and the level of LTD.

To understand the implications of these observations for a readout mechanism based on Ca\textsuperscript{2+} spike generation (Fig. 5), using Model 2 we determined the set of stage 3 trajectories in the (V, l) plane that lead to a Ca\textsuperscript{2+} spike (see METHODS). Large-amplitude rebounds that initiated within the reliability zone passed furthest above the spiking threshold (Fig. 6B). This initiates a rebound well timed for driving an anticipatory reflex (Movie S2).
Rebounds that initiated elsewhere either failed to reach or just crossed threshold. In the presence of membrane potential noise, this implies that if the system reaches the reliability zone the probability of Ca\(^{2+}\) spike generation is high. Much as in our two-compartment simulations, this probability falls dramatically as the ISI is shortened (Movie S3 and Fig. 5B). The Ca\(^{2+}\) spike voltage threshold does not vary much across a wide range of HVA Ca\(^{2+}\)-channel density (data not shown), indicating Ca\(^{2+}\) spiking is a robust readout of whether the system has entered the recall reliability zone. Thus the phase plane analysis illuminates key features of a rebound-based memory recall mechanism, including conditions for reliable recall.

**Role of postinhibitory rebounds in VOR gain adaptation**

Because cerebellar circuitry is highly conserved, rebound depolarization might serve multiple forms of cerebellar memory recall. For example, floccular Purkinje cells involved in horizontal VOR adaptation project to target cells in the vestibular nuclei that also exhibit significant rebound depolarization in vitro mediated by hyperpolarization-activated currents (Sekirnjak et al. 2003; Serafin et al. 1991). These currents require further characterization and are expressed to varying degrees across MVN cell types, but as a group the MVN neurons receiving input from the floccular Purkinje cells exhibit exceptionally pronounced rebound burst spiking (Sekirnjak et al. 2003). The currents involved seem to include the h-type cation current and probably some amount of Na\(^+\) and T-type Ca\(^{2+}\) currents (Sekirnjak and du Lac 2002; Serafin et al. 1991; Smith et al. 2002). Regardless of the current identities, the empirically determined time constant (\(-620\ \text{ms}\) describing the duration of hyperpolarization needed for maximal rebound burst firing is considerably longer than that for DCN cells (Fig. 2E) (Sekirnjak and du Lac 2002). Might rebound depolarization and the need for a long period of hyperpolarization underlie some of the temporal asymmetries seen in behavioral studies of VOR adaptation?

Well-known primate behavioral studies have shown that the amplitude of learned VOR responses depends on the relative timing of vestibular and visual stimuli in a manner resembling the dependence on CS–US timing in classical conditioning. Raymond and Lisberger (1996) repeatedly paired a vestibular stimulus, a 600 ms pulse of head rotation, with a brief visual stimulus consisting of moving dots. The visual motion stimulus was presented at one of three different ISI values: a zero ISI condition analogous to backward conditioning (Fig. 7C, left), a short forward ISI of 225 ms (Fig. 7C, middle), and a long forward ISI of 450 ms (Fig. 7C, right). A learned VOR
response developed in all cases, but the response amplitude grew as the ISI lengthened. Such dependence on the ISI may be analogous to that seen in eyelink conditioning. Could rebounds underlie this effect? The timescale of the behavioral effect is similar to that of h-current activation.

To study the issue we created a simple, one-compartment model of an MVN cell in which h-currents mediated rebounds (Fig. 7B). The model is analogous to Model 1 of a DCN cell in that the model has only one compartment and lacks the channels responsible for the fast spontaneous spiking that MVN cells exhibit. The single compartment thus better mimics a dendrite than a soma. As before, we interpreted the rebounds as signals driving learned motor responses. MVN simulations used a fixed time constant, $\tau_q$, for $I_h$ activation, as in the MVN cell model of Sekirnjak and du Lac (2002).

We used a stimulus protocol based on the Raymond–Lisberger experiments and found the largest rebounds arise when the visual stimulus occurs during the latter portion of the vestibular impulse (Fig. 7E). Longer ISI values allow more time for h-currents to activate at hyperpolarized voltages, heightening rebound depolarization. Rebound amplitude also depends on biphasic Purkinje cell spiking and thus on the levels of LTP and LTD induced during training (data not shown). By varying $\tau_q$ over a range of values, we found that a value of ~400 ms generated the largest ratio of rebound amplitudes between the long ISI condition and the zero ISI condition (Fig. 7, D and E). This value of ~400 ms for $\tau_q$ at a physiological temperature appears consistent with the empirical value of about 620 ms measured at 31–33°C by Sekirnjak and du Lac (2002). Thus, the amplitude dependence of learned eye movements on the ISI value might stem from variable levels of current flow through hyperpolarization-activated conductances such as h. However, the component of the learned response that is independent of the ISI value is unlikely to be driven by rebounds and is beyond the scope of our present model, which seeks to account only for the ISI-dependent component.

**DISCUSSION**

We have presented a lock-and-key hypothesis on how the expression of memory responses may undergo filtering via neurophysiological mechanisms active during memory retrieval. This hypothesis and our computational work exploring a candidate rebound-based lock-and-key mechanism were prompted by data suggesting that backward-ordered classical eyelink conditioning as well as noncerebellar forms of aversion conditioning can lead to latent memory storage or changes in neural activity, despite a lack of conditioned responses (Barnet et al. 1997; Gould and Steinmetz 1996). The complex manner in which plasticity might evolve across a large network of synaptic connections throughout learning experience also suggests some constraints on motor memory expression might be implemented via neurophysiological mechanisms of recall (Mauk and Ohyama 2004).

We explored these ideas through computational studies of two cerebellar behaviors by examining whether DCN and MVN cells can filter signals from Purkinje cells to influence response timing and prevent certain motor responses. Biophysical models of these two cell types that incorporate rebound channels lead to consistent explanations for behavioral data on cerebellar motor learning. These models make direct links between ion channel kinetics and memory expression and, particularly for eyelink conditioning, yield specific predictions of how learning performance varies as a function of the relative timing of paired training stimuli. Within our lock-and-key framework for these models, subjects undergo both cerebellar LTP and LTD regardless of whether the training stimuli were presented in forward or backward order. As a result, the learned sensory cue drives biphasic Purkinje cell activity. Yet, this biphasic activity triggers rebound depolarization in the DCN cells and drives well-timed classically conditioned reflexes only if the training ISI was sufficiently positive. In this way, inappropriate motor responses to conditioned stimuli that do not precede the US sufficiently are avoided. Phase plane analysis reveals the basic ingredients for reliable reflex expression, including ample levels of both LTD and LTP. In MVN cells, rebound currents may underlie the variation of VOR adaptation magnitude with the relative timing of visual and vestibular training stimuli. Such effects hinge on the observed capabilities of both DCN and MVN cells for rebound depolarization.

**Electrophysiological properties of DCN neurons are consistent with the rebound theory**

In vitro studies of DCN cells have found that rebounds occur in both cerebellar slice and isolated cerebellum–brain stem preparations (Aizenman and Linden 1999; Jahnsen 1986a,b; Llináš and Muhlethaler 1988). MVN neurons also undergo rebounds in vitro, but there is more uncertainty about the channels involved (Sekirnjak and du Lac 2002, 2006). There is also indirect physiological and pharmacological evidence DCN cells rebound in vivo (Aksenov et al. 2005; Hesslow 1994a), including for a class of neurons with blink-related activity (Chen and Ewing 2006). Input from a single Purkinje cell induces a large conductance change in the DCN cell (Pedroarena and Schwarz 2003), which is sufficient to allow a modest postinhibitory rebound and increase in Na$^+$ spike rate (M. Molineux, personal communication). Multiple Purkinje cells might drive larger rebounds and spike bursts in concert, such as through coordinated Purkinje cell spiking (Heck et al. 2002; Thier et al. 2000). The anatomical convergence of many hundreds of Purkinje cells onto each DCN neuron implies that the aggregate activity of a population of Purkinje cells influences DCN cell activity.

The in vivo extracellular recordings performed to date of DCN neurons during classical conditioning do not provide strong evidence either for or against our rebound theory. Single-unit and multi-unit recordings both reveal an increase in DCN spiking rate that precedes motor output (Berthier and Moore 1990; Choi and Moore 2003; McCormick and Thompson 1984a,b; McCormick et al. 1982). By comparison, evidence for a pause in spiking during early portions of the ISI is limited. Berthier and Moore reported some cells with reduced spiking at the beginning of the CS, although this pattern is not apparent in all single-unit recordings (Berthier and Moore 1990; Choi and Moore 2003). Multi-unit recordings of DCN cell activity do not exhibit a pause, but these recordings may not provide sufficient sensitivity to reveal a partial reduction in spiking within a subpopulation of recorded neurons (McCormick and Thompson 1984a,b; McCormick et al. 1982).
Irrespective of these results, the rebound model does not make a strong prediction concerning DCN firing during early portions of the CS. During the early portion of the ISI, DCN neuron spiking might remain virtually unchanged, despite increased Purkinje input, due to the dendritic location of most Purkinje synapses and T-type channels (Fig. 5). Technically difficult in vivo intracellular recordings would be required to determine how subthreshold responses in DCN cells develop during conditioning.

**Experimental predictions for studies of cerebellum-dependent motor learning**

The lock-and-key hypothesis leads to a clear prediction that is testable independent of whether rebound depolarization provides a lock mechanism: Classical conditioning with a short (<100 ms) or backward CS–US interval should lead to plasticity in the cerebellar cortex despite the lack of reflex acquisition. Several experimental tests of this prediction are possible. Second-order classical conditioning, which can induce expression of previously latent first-order conditioning, might be useful for explicitly demonstrating that a memory of backward conditioning is formed (Barnet et al. 1997). Alternatively, studies of backward eyeblink conditioning using human brain imaging techniques might be capable of revealing plasticity-related effects (Cheng et al. 2007). Electrophysiological recordings of Purkinje cell spiking during reflex conditioning in decerebrate ferrets and guinea pigs have revealed changes in spiking patterns in response to forward training (Jirenhed et al. 2007; Kotani et al. 2003), and thus might be used to examine the effects of backward or short-interval conditioning. Recordings from rabbit Purkinje cells, but not DCN cells, were reported to show changes in activity patterns following backward US–CS pairings (Gould and Steinmetz 1996). This lends support to the lock-and-key hypothesis, but more experimental data are still needed.

Several other testable predictions emerge from our modeling of rebound dynamics during memory recall. Removal or blockade of DCN cell rebound conductances should hinder expression of conditioned blinks. To test this idea, T-channel blockers might be used to prevent rebounds in trained subjects (McDonough and Bean 1998; Porcello et al. 2003). Failure to impair conditioned blinks would cast serious doubt on our proposed rebound mechanism. A related test might be performed in trained animals during recordings of DCN cells that drive conditioned responses. Transient depolarization of these cells during the ISI in trained animals should prevent or diminish blink-related spiking activity by thwarting T-channel deinactivation. Although perturbation of one cell seems unlikely to disrupt the blink itself, stimulation of many DCN cells might have such an effect.

A corollary to this logic concerns inhibition of olivary cells by projections from GABAergic DCN cells that also receive Purkinje cell inputs and exhibit rebounds (De Zeeuw and Berrebi 1995; Teune et al. 1998). These connections appear critical for extinction of conditioned reflexes following unpaired CS presentations (Medina et al. 2002). Thus, blockade of rebound channels should hinder both expression and extinction of conditioned reflexes. A caveat is that rebound channel blockers or electrical stimulation applied to the DCN might alter climbing fiber input to the cerebellum through nucleolary inhibitory feedback (Bengtsson et al. 2004; Hesslow and Ivarsson 1996). To dissociate the role of rebounds in excitatory versus inhibitory DCN neurons might require genetic tools for cell-type-specific manipulation, such as optogenetic techniques (Zhang et al. 2007).

Another prediction of the rebound theory is that blink-related Purkinje cells should exhibit, in the aggregate, biphasic patterns of CS-driven activity in conditioned subjects. This contrasts with Albus’s proposal that GABAergic Purkinje cells should drive DCN cells through disinhibition (Albus 1971). The recordings made to date of the spiking activity of individual Purkinje neurons in trained animals have revealed a diversity of spiking patterns in response to the CS (Berthier and Moore 1986; Gould and Steinmetz 1996; Green and Steinmetz 2005; Jirenhed et al. 2007; Kotani et al. 2003, 2006; Tracy and Steinmetz 1998). Although multiple regions of cerebellar cortex have been implicated in eyeblink conditioning, most studies of Purkinje cell activity in classical conditioning have focused on a subset of these areas.

Recordings of Purkinje cell activity in trained rabbits from the cerebellar anterior lobe (Green and Steinmetz 2005) and cerebellar lobule HVI (Berthier and Moore 1986; Gould and Steinmetz 1996), both areas implicated in eyeblink conditioning, have revealed a mixture of activity increases and decreases in response to the CS. Excitatory responses might occur earlier in the ISI, with activity decreases occurring later (Green and Steinmetz 2005). Recordings from lobule HVI in decerebrate guinea pigs and ferrets have also revealed a mixture of responses (Jirenhed et al. 2007; Kotani et al. 2006). One particularly careful study, in which Purkinje cells were first identified as being responsive to the US prior to training, reported mainly decreases in Purkinje cell spiking in response to the CS after training (Jirenhed et al. 2007). However, this study also mentions that after training some cells undergo an increase in firing during the first 50–100 ms of the CS, followed by an abrupt drop in spiking. Overall, Purkinje cell recordings in trained animals are mainly consistent with the rebound theory but do not provide sufficient evidence to validate the prediction that aggregate Purkinje cell activity should be biphasic. Given the central role in the theory of such biphasic aggregate responses, it seems important that future studies testing this prediction should record from multiple Purkinje cells concurrently using multielectrode techniques.

If rebounds are instrumental in driving classically conditioned responses, the timing of training stimuli needed for successful conditioning should depend on rebound channel kinetics. Because the minimum ISI that leads to rebounds is set by the sum of the inactivation time constant and $t_{LTD}$, an increase in the inactivation time constant should increase the minimum ISI for successful training. Likewise, slowing the kinetics of hyperpolarization-activated currents in MVN cells should increase the interval required between vestibular and visual inputs needed to generate the greatest changes in VOR gain.

Further predictions of the rebound theory concern classically conditioned subjects in which cerebellar LTD or LTP is impaired. Elimination of both LTD and LTP would prevent biphasic patterns of Purkinje cell spiking, precluding rebounds. Our simulations also suggest that if either LTP or LTD is partially impaired, rebound amplitude decreases and sporadically triggers readout by $Ca^{2+}$ or $Na^{+}$ spikes (data not shown).
However, rebound-driven spiking remains well timed when it occurs. Thus some animals partially deficient in LTD or LTP might exhibit conditioned responses sporadically or of diminished amplitude, but with proper timing. Greater disruptions of cerebellar plasticity would disrupt response timing due to insufficient biphasic modulation of Purkinje cell spiking.

To date, several groups have studied eyelink conditioning in mice with disrupted cerebellar LTD. Four strains of such mice exhibited blinks that occurred sporadically or with altered amplitude, but with the same distribution of time courses as that of wild-type mice (Kishimoto et al. 2001; Koekkoek et al. 2005; Miyata et al. 2001; Shibuki et al. 1996). It was reported that mice expressing a protein kinase C (PKC) inhibitor that impaired LTD had ill-timed residual blinks (Koekkoek et al. 2003). However, questions have been raised about this study regarding the degree to which motor learning was cerebellar in origin (Christian et al. 2004; Jirenhod et al. 2007; Koekkoek et al. 2003). It is possible PKC inhibition disrupts more than just LTD. Although further study is needed, the former four strains seem consistent with the rebound theory and suggest normal LTD levels might be unnecessary for normally timed responses.

### Comparison to other work on the role of rebounds in cerebellar function

Several other authors have considered a potential role for DCN cell rebounds in cerebellar network function. Inspired by the observation that Purkinje cell activity effectively triggers rebounds in vitro (Aizenman and Linden 1999), Kistler and de Zeeuw (2003) created computational models emphasizing a potential role for rebounds in reverberatory olivo-cerebellar network activity through which Purkinje cells can affect their own subsequent activity and timed motor responses. In experiments on classically conditioned cerebrate cats, Hesslow (1994a,b) noted that brief electrical stimulation of the cerebellar cortex leads to a delayed activation of muscle fibers assessed by electromyography. This finding was explained as arising from postsynaptic rebound depolarization in the DCN and supports a basic assumption underlying our models—that rebound-driven DCN cell activity can trigger motor action.

Aizenman and Linden (1998) found that DCN cell rebound depolarization and the associated spike burst are important for determining the polarity of gain changes at the Purkinje cell to DCN cell synapse. Mauk and collaborators (Mauk and Donegan 1997; Medina and Mauk 1999) performed extensive network modeling studies of cerebellar learning and suggested that the rise in intracellular Ca2+ due to DCN cell rebounds might be a potent trigger for plasticity at the mossy fiber to DCN cell synapse. A recent experimental study has demonstrated this effect, confirming the importance of postsynaptic rebound current for potentiation of mossy fiber to DCN cell synapses (Pugh and Raman 2006). However, in the original simulations the inefficacy of brief ISI values for classical conditioning arises from a minimum time interval for synchronization of granule cell activity following the CS, rather than from a rebound-based mechanism (Mauk and Donegan 1997).

For ISI values shorter than the minimum for granule cell synchronization, plasticity in the cerebellar cortex is precluded. By comparison, our lock-and-key hypothesis is based on the supposition of at least some plasticity occurring with brief forward or backward ISI values.

A non-synaptic form of plasticity capable of increasing the intrinsic excitability of DCN and MVN neurons appears suited to raise the propensity for rebounds over the course of training. Bursts of synaptic input can induce DCN and MVN cells to display long-lasting gains in excitability due to increases in the maximum rebound current (Aizenman and Linden 2000; Smith et al. 2002; Zhang et al. 2004). A biphasic burst-and-pause pattern of Purkinje cell activity may be optimally suited to induce this increase (Aizenman and Linden 2000; Medina and Mauk 1999; Pugh and Raman 2006). Thus, rebound generation might be facilitated during training, perhaps reducing the number of Purkinje inputs needed to drive motor action. Overall, multiple cerebellar plasticity mechanisms in addition to those invoked here at the PF–Purkinje synapse are likely to occur during motor training and to shape both cerebellar dynamics and motor learning in a cooperative fashion (Boyden et al. 2004; D’Angelo et al. 1999; De Zeeuw and Yeo 2005; Hansel et al. 2001; Mauk and Donegan 1997; Medina and Mauk 1999; Soler-Llavina and Sabatini 2006). Collectively, the existing experimental data not only are consistent with our computational models but also reach well beyond, suggesting that rebound currents have multiple functions additional to the temporal filtering role explored here.

### A role for rebounds in temporal shaping of learned responses

A long-standing debate has concerned the issue of whether cerebellar-mediated memory storage occurs within the cerebellar cortex or within the deep cerebellar or vestibular nuclei (du Lac et al. 1995; Ito 1982; McCormick and Thompson 1984a; Miles and Lisberger 1981). Consistent with the identification of multiple plasticity mechanisms in vitro, recent in vivo studies indicate both the cortex and the nuclei have a role in memory storage, but with distinct kinetics for plasticity induction and with distinct roles in setting the timing of motor expression (Kassardjian et al. 2005; Medina and Mauk 1999; Ohyama and Mauk 2001; Perrett et al. 1993; Shutoh et al. 2006). In both eyelink conditioning and ocular reflex adaptation, shortly after the start of training motor memory is susceptible to extinction and is impaired by lesion or pharmacological disconnection of the cerebellar cortex. After a few days, motor memories are more resistant to extinction and can persist without Purkinje cell involvement (Kassardjian et al. 2005; Ohyama and Mauk 2001; Perrett et al. 1993; Shutoh et al. 2006).

However, even long after training, Purkinje cells appear important for setting the proper timing of learned responses. In eyelink conditioning, disconnection of Purkinje cells’ projections to the DCN leads to ill-timed, short-latency blink responses to the CS (Ohyama and Mauk 2001; Perrett et al. 1993). These short-latency blinks probably arise because without inhibitory input from Purkinje cells, DCN cells may be driven strongly by mossy fiber inputs starting from the onset of the CS. For VOR adaptation, the relative contributions of the floccular Purkinje cells and the MVN neurons in shaping the temporal character of the learned motor response remain less clear. Our interpretation of the available data are that for VOR adaptation, a baseline component of the learned motor re-
response that is not as sensitive to the relative timing of vestibular and visual training stimuli arises from mossy fiber-driven activity in the MVN (Fig. 7C). However, there also appears to be another component that is sensitive to the relative timing of the training stimuli (Raymond and Lisberger 1996); it is this second component that we propose has the proper form and kinetics to be explained by a rebound-based mechanism using a slow, hyperpolarization-activated current (Fig. 7E), such as that identified by Sekirnjak and du Lac (2002). Unlike eyelink conditioning, for which there is no learned response with short ISI values, there is VOR adaptation following short-interval training, but at reduced amplitude relative to adaptation at longer ISI values (Raymond and Lisberger 1996). Thus, rebound mechanisms cannot quantitatively account for the full magnitude of VOR adaptation.

Generalizations of the proposed rebound mechanism

Our simulations involved specific choices of cellular parameters, but the ideas presented here on rebounds may have explanatory power surpassing that of our detailed models. One aspect of generality concerns the channels that mediate rebounds. It was first thought mainly T-type channels drive DCN cell rebounds, but new evidence also suggests a role for Na\(^+\) currents (Sangrey and Jaeger 2005). Further, rebound amplitude or kinetics may vary between individual DCN neurons due to differential expression of T-channel isoforms (Molineux et al. 2006). Identities of the rebound channels in MVN cells are still in question, but in addition to the h-type current there is evidence Na\(^+\) and low-voltage-activated Ca\(^{2+}\) currents play a role (Sekirnjak and du Lac 2002; Serafin et al. 1991). Further characterization of rebound channels may be important for understanding the precise timing relations seen in behavioral studies. However, the basic idea that rebounds shape temporally asymmetric behavioral responses is general and may apply to other cerebellum-dependent learning paradigms. For example, learned aspects of smooth visual pursuit exhibit temporal dependencies on the approximately 200 ms scale that might reflect requirements for rebound generation in cells of the cerebellar caudal fastigial nucleus (Medina et al. 2005).

Role of synaptic plasticity in memory formation and recall

A prevalent view holds that LTD and LTP are opposing mechanisms, with one encoding memories and the other erasing (Boyden and Raymond 2003; Coesmans et al. 2004; Lev-Ram et al. 2003). We are proposing a different view, in which both cerebellar LTD and LTP are needed for reliable recall. The lock mechanism based on rebound depolarization enforces the requirement for forward training, but nevertheless both LTD and LTP are induced during forward and backward training.

In our lock-and-key framework, backward conditioning and forward training at short intervals induces synaptic plasticity at parallel fiber to Purkinje cell synapses, despite the absence of behavioral output. In this respect, our work follows several prior models of cerebellar-mediated learning in which neuronal plasticity can occur without any change in motor behavior. Models of learning with two or more stages have been proposed for eyelink conditioning (Mauk 1997; Mauk and Donegan 1997), VOR adaptation (Boyden et al. 2004; du Lac et al. 1995), and other motor behaviors (Smith et al. 2006). These models involve an intermediate stage of learning during which plasticity has occurred but learning is not yet expressed. More generally, any model of learning with two or more serial stages of plasticity inherently implies the possible existence of plasticity without expression of learning. We also present a two-stage model, but here the second stage of processing is

FIG. 8. A lock-and-key description of memory recall. A: schematic of memory formation within the lock-and-key description. Paired PF and CF activity induces synaptic plasticity in the cerebellar cortex. This shapes Purkinje cell “key” activity in response to subsequent presentations of the learned sensory input. B: schematic of memory recall, in which the lock resides in the DCN. Key activity driven by learned sensory input is sent to the DCN via Purkinje cell axons. Not all keys will be successful at driving DCN cell activity and learned motor responses. The lock prevents inappropriate motor responses by filtering out nonmatching key activity. Partially matching key activity leads to unreliable recall or responses of diminished amplitude. C: an implementation of a lock-and-key mechanism using a linear–nonlinear (L-N) filter model, similar to those used to describe sensory receptive fields. Key activity, \(K(t)\), undergoes linear filtering according to \(F(t)\), then the result is filtered by a nonlinear threshold function, \(G(x)\). D: the L-N model enables responses, equal to \(G[K(t) \ast F(t)]\), to be made selectively to only those keys, \(K(t)\), that are shaped by training with sufficiently positive ISI values. E: response of the L-N model as a function of ISI in eyelink conditioning. The results mimic those of DCN cell simulations (Figs. 4–6) and the classic rabbit behavioral data (Figs. 1B and 5B).
implemented as temporal filtering occurring at memory recall rather than as plasticity occurring during memory formation. As with prior two-stage models of plasticity, our model also predicts the possibility of plasticity without behavior modification.

The idea of rebound generation as a temporal filter pertains to the ongoing debate about mechanisms that shape the dependence of classically conditioned responses on the CS–US ISI (Fig. 1B). Ideas from recent studies on synaptic plasticity and animal behavior have suggested conflicting explanations. Some authors have suggested spike-timing-dependent plasticity can account for the variation in performance with the ISI value (Wang et al. 2000). A timing-dependent plasticity rule in which PF activity preceding CF activity is optimal for LTD induction does create a distinction between backward and forward training (Fig. 2). However, the recent and older experimental data show that LTD can occur with forward or backward timing protocols (Fig. 2A) (Chen and Thompson 1995; Ito and Kano 1982; Wang et al. 2000), so another mechanism auxiliary to LTD seems needed to create conditioned reflexes selectively following forward but not backward training. Our model incorporates spike-timing-dependent plasticity, and is a key factor that causes the conditioned response to precede the expected US. However, it is rebound generation that precludes learned responses following backward training. In a sense, a memory of backward training is formed in the resulting patterns of LTD and LTP, but this memory is not retrieved in response to the CS.

This statement of the lock-and-key hypothesis fits well with studies of classical aversion conditioning, which have shown backward training leads to an associative memory of the US–CS pairing (Gallistel and Gibbon 2000). CS presentation alone does not yield conditioned motor responses, but the associative memory can be demonstrated through second-order conditioning (Barnet et al. 1997). Thus, at least for this form of aversion conditioning, mediated outside the cerebellum, the lock-and-key hypothesis appears to be correct. What mechanism prevents the stored memory from yielding a response to the CS? For aversion conditioning the answer remains unknown, but our study points to rebound depolarization as a candidate mechanism by which such behavioral filtering might occur for cerebellum-dependent behaviors.

An algorithmic lock-and-key description of memory retrieval

In sensory neuroscience, filters have been fruitfully used to describe receptive fields and spiking behavior in an algorithmic manner, apart from physiological details. Our study suggests an algorithmic lock-and-key description of cerebellar memory recall (Fig. 8). The “lock” resides in the DCN or MVN as a temporal filter that requires specific “key” input activity to drive rebound spiking and a motor response. The key is the biphasic pattern of Purkinje cell activity that is shaped by training and driven by a learned sensory cue. Synaptic plasticity does not lead to learned responses unless key activity is shaped to match the temporal filter of the lock (Fig. 8, A and B). Backward training induces plasticity, but the resulting key activity does not fit the lock, precluding conditioned responses.

We found that a simple linear–nonlinear (L-N) filter model, inspired by those used to describe visual receptive fields (Baccus and Meister 2002; Korenberg and Hunter 1986), can accurately predict the responses of our biophysical models and the behavioral dependence of learned responses on ISI (Fig. 8, C–E). Thus from an algorithmic standpoint memory retrieval may involve a temporal filter that excludes certain behaviors and allows others.

The lock-and-key model of recall might be adaptable to other nondeclarative forms of memory involving feedforward networks. Striatal memory for motor sequences shows promising similarities, since both Purkinje cells and striatal medium spiny neurons receive diverse sensory information, undergo bidirectional plasticity, and are GABAergic projection neurons that trigger motor sequences (Fino et al. 2005). The similarity between these two GABAergic cell types also extends to their respective targets, because there is one class of striatal target neuron in the globus pallidum that is spontaneously active, has a baseline membrane potential of about –60 mV, and reliably undergoes postinhibitory rebound depolarization in response to electrical stimulation of striatal input fibers (Nambu and Llinás 1994). By analogy, corticostratial plasticity alone may not represent a memory, since select patterns of striatal input activity to the globus pallidum may be needed to unlock motor expression. These ideas challenge classical theories of memory storage that focus almost exclusively on neuronal plasticity but avoid mention of how retrieval dynamics may help shape memory expression.

Neuroscientists have long sought the location and substance of memories. This quest led to the notion of the engram, the physical unit of memory, and to the later idea that changes in synaptic strength constitute a candidate substrate for memory (Bliss and Lomo 1973; Lashley 1950). Cognitive scientists have countered that synaptic plasticity alone does not account for the complex phenomenology of memory recall (Gallistel 1993; Martin et al. 2000). In this opposing view, a memory is a physical dynamic that occurs exclusively at recall. Plasticity may help shape this dynamic, but is not by itself a memory. Our computational models provide concrete examples in which it is difficult to identify any physically localized engram. Would the engram include the synapses that have undergone plasticity, the key activity that triggers a memory, the activity unlocked at a rebound, or all of the above? By itself plasticity seems a poor candidate for a complete engram, since it is insufficient to allow recall. Questions regarding the physical substance of memory may be misleading, neglecting that recall occurs due to a sequence of events culminating in a specific form of neural dynamics. This caveat regarding the substance of memory in our models might also apply broadly to multiple memory systems.

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