Astrocytes as the Glucose Shunt for Glutamatergic Neurons at High Activity: An In Silico Study

Rossana Occhipinti, Erkki Somersalo, and Daniela Calvetti
1Departments of Mathematics and 2Mathematics and Cognitive Science, Case Western Reserve University, Cleveland, Ohio

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Occhipinti R, Somersalo E, Calvetti D. Astrocytes as the glucose shunt for glutamatergic neurons at high activity: an in silico study. J Neurophysiol 101: 2528–2538, 2009. First published October 15, 2008; doi:10.1152/jn.90377.2008. The question of the preferred substrate of glutamatergic neurons at high neural activity has been vigorously debated for over a decade since the classical hypothesis (CH) of the primacy of glucose has been challenged by the astrocyte-neuron lactate shuttle hypothesis (ANLSH), which replaces the primacy of glucose with astrocyte produced lactate. We perform Bayesian Flux Balance Analysis (BFBA) with a new mathematical model of cellular brain energetics, comprising detailed biochemical pathways in and between astrocytes and glutamatergic neurons and partitioning of each cell type into cytosol and mitochondria. Supported by the results of our in silico studies, which are in remarkable agreement with previously published results, we posit the Glucose Shunt Hypothesis (GSH) that during high activity, the inhibition of the phosphofructokinase (PFK) enzyme in neuron impairs neuronal glycolysis, enabling the process by which lactate effluxed by astrocytes is taken up by glutamatergic neurons, whereas at low activity, glucose remains the preferred substrate for neurons. We postulate that the ANLS is a shunt utilized by glutamatergic neurons to bypass their glycolysis impaired by the inhibition of PFK in connection with increased oxidative phosphorylation at high neuronal activity.

INTRODUCTION

The brain is a highly oxidative organ that requires a continuous supply of nutrients and a disproportionate amount of energy compared with most of the other organs in the body. It is well established that under normal physiological conditions, glucose is the main obligatory fuel of the brain, (Siesjo 1978). The classical concept that glucose is the sole energy substrate used by the neurons in adult brain to sustain neuronal activity has dominated the field of brain energy metabolism for many years until the results of PET imaging (Fox and Raichle 1986) has dominated the field of brain energy metabolism for many years until the results of PET imaging (Fox and Raichle 1986) has dominated the field of brain energy metabolism for many years until the results of PET imaging (Fox and Raichle 1986) has dominated the field of brain energy metabolism for many years until the results of PET imaging (Fox and Raichle 1986) has dominated the field of brain energy metabolism for many years until the results of PET imaging (Fox and Raichle 1986).

Since the primacy of glucose was challenged, plenty of evidence has been provided to support both classical (Bak et al. 2006; Zielke et al. 2007) and ANLS hypotheses (Magistretti et al. 1993; McKenna et al. 1993), but the debate remains vibrant because obtaining in vivo and in situ data is difficult, and indirect observations may have a feasible interpretation in both frameworks (Chih and Roberts 2003; Chih et al. 2001). Recent two-photon fluorescence imaging studies of NADH in hippocampal slice preparations (Kasischke et al. 2004) have been interpreted as experimental evidence of the ANLS (Pellerin and Magistretti 2004), although it has been argued that none of the key components of the ANLS, i.e., lactate or pyruvate, were measured in this study (Gjedde 2007; Riera et al. 2008).

The ANLS, featuring astrocytes as suppliers of lactate at high activity, does not fully explain why neurons should prefer lactate to glucose. Indeed, expression of glycolytic enzymes in neurons and abundance of the GLUT-3 glucose transporters in synaptic membranes (Leino et al. 1997), with higher affinity compared with the GLUT-1 transporters in astrocytes (Vannucci et al. 1997), would suggest the opposite.

One of the problems in settling the question of the lactate shuttling and quantifying the contribution of lactate generated within the brain to neuronal energetics is the difficulty of distinguishing in vivo the transfer of lactate among brain cells (Dienel and Cruz 2004). It has in fact been observed that the lactate shuttling is a cell-to-cell phenomenon (Dienel and Cruz 2004) not limited to the lactate exchange between astrocytes and neurons, but it can occur within populations of cells of the same type. As pointed out in Aubert et al. (2005), “interpretation of lactate kinetics in terms of cellular production, utilization, or disposal remains complex.”

In this article, we propose a mechanism capable of explaining the shift of the neuronal preference toward lactate at high activation. We hypothesize that increased oxidative metabolism of glutamatergic neurons at high neuronal activity exerts an inhibition on the glycolytic enzymes phosphofructokinase (PFK) and hexokinase (HK). Our computational results show that while the same mechanism occurs in astrocytes, their lower oxidative activity does not significantly inhibit glycolysis, therefore shifting their equilibrium toward lactate production. The astrocyte produced lactate, effluxed in extracellular space, is taken up by neurons to fuel their TCA cycle, thus bypassing the glycolytic quench, whereas at low activity, glucose remains the main energy substrate. In practice, we implement the glycolytic inhibition as a downregulation of PFK by the increased oxidative phosphorylation of the cell. The allosteric sensitivity of PFK to changing cytosolic conditions, e.g., the equilibrium state of adenosine phosphates (Gjedde 2007), variations in pH, redox
states, and creatine kinase equilibrium (Sappey-Marinier et al. 1992), is known. This leaves several possibilities open to explain the regulatory mechanism.

The Glucose Shunt hypothesis (GSH) posits that neuronal uptake of astrocyte produced lactate is a glucose shunt at high activity, whereas at low activity, the neuron’s own glycolysis is the main source of pyruvate entering the TCA. To test the feasibility of the GSH, we perform steady-state analysis with a new five-compartment model of the astrocyte-neuron cellular complex using Bayesian Flux Balance Analysis (BFBA) (Heino et al. 2007). Classical Flux Balance Analysis (FBA) is a methodology for studying steady-state configurations in metabolic networks starting from mass balance equations (Ramakrishna et al. 2001). The BFBA is a stochastic extension of FBA, where all unknown biochemical reaction fluxes and transport rates are modeled as random variables, the stoichiometric and physiological constraints of the system determining their joint probability distribution. The stochastic formulation allows the expression of the degree of uncertainty in both model and data, and the use of sampling methods for estimating the fluxes and transport rates of interest makes it possible to carry out this type of analysis even where the classical FBA would fail, e.g., when the model is not fully consistent or contains nonlinear constraints. This is the case for our model where the inhibition of PFK in connection with an increase in oxidative phosphorylation is implemented in the form of a nonlinear constraint between these two reaction fluxes.

The results of our BFBA confirm that a GSH is consistent with experimental steady-state data at high and low neuronal activities (Gruetter et al. 2001; Hyder et al. 2006; Shen et al. 1999) and conforms to the original formulation of the ANLS hypothesis in Pellerin and Magistretti (1994), recently revisited in Pellerin et al. (2007).

The present work makes a further contribution toward a unified framework for brain energy metabolism, suggesting a regulatory mechanism of the metabolic interaction between astrocytes and glutamatergic neurons that neither assumes nor excludes either the classical or the ANLS hypothesis. The use of mathematical models to create a coherent quantitative framework for energetics and substrate fluxes through the complex biochemical pathways in astrocytes and neurons has been previously advocated, e.g., by Aubert and coworkers (Aubert and Costalat 2005; Aubert et al. 2005, 2007) to study the dynamics of lactate and test the existence of the ANLSH between astrocyte and neuron under different physiological conditions.

**METHODS**

**New five-compartment model of cellular brain energy metabolism**

The new metabolic model for brain energetics that we propose and utilize for our in silico experiments was developed starting from the model in Occhipinti et al. (2007). The model contains the key metabolic pathways that need to be active whether the metabolic processes follow the classical or the ANLS hypothesis. Thus the preferred metabolic pathways to fuel the neuronal activity are determined only by the energetic needs of the two cell types and on substrate availability. The increased complexity of this model compared with others proposed in the literature (Aubert and Costalat 2005; Gruetter et al. 2001) requires the use of a robust and powerful methodology, described in the following text, to perform steady-state analysis. The main advantage of our approach to modeling cellular brain energy metabolism is that by performing BFBA, we can utilize a very detailed model while keeping the number of fixed input fluxes and transport rates to a bare minimum, letting the stoichiometry and the need of the systems decide what is a suitable distribution of the reactions fluxes and transport rates to attain steady state.

The brain is a strongly localized organ in the sense that the ratio of neurons and glial cells, their relative volumes as well as their morphology and functioning depend strongly on the regionality. Our in silico model is homogenized over a region of interest, so it is natural to assume that the domain consists of neurons and astrocytes that are morphologically and functionally of a given type. The model for an astrocyte-neuron system is a spatially homogenized multicompartment model that differentiates between blood and extracellular space (ECS) on one hand and two cell types, astrocytes and glutamatergic neurons. Furthermore, each cell type is subcompartmentalized into cytosol and mitochondria. Each compartment in turn is characterized by the biochemical reactions taking place in it (see APPENDIX and Tables A1 and A2), and the various compartments are linked through the transport of some biochemical species between them.

**Biochemical pathways**

In our computational model, based on the biochemical pathway chart shown in Fig. 1, both neurons and astrocytes are equipped with the glycolytic pathway in the cytosol domain and the TCA cycles and oxidative phosphorylation in the mitochondria. The TCA cycle reactions have a preferred direction that can be justified by thermodynamic considerations under baseline conditions. The virtual transport of reducing equivalents (NAD+/NADH) between cytosol and mitochondria goes via the malate-aspartate shuttle (Dennis and Clark 1978). Another shuttle mechanism, which is responsible for the transfer of reducing equivalents across the mitochondrial membrane, is the glycerol-3-phosphate shuttle that has not been included in the present model because it is considered of little importance in the brain (Nguyen et al. 2003; Siesjo 1978). Anaplerotic reactions, which serve to replenish pools of TCA cycle intermediates from precursors that are not TCA cycle intermediates, have been also included in the model. More specifically, pyruvate carboxylase, a mitochondrial reaction that occurs only in one direction leading to the formation of oxaloacetate from pyruvate and that has been detected only in astrocytes (Yu et al. 1983), has been included only in the mitochondria of the astrocyte. Both cytosolic and mitochondrial malic enzymes have been detected in astrocytes and neurons (Hassel 2001; Hassel and Brathe 2000) and for this reason have been modeled in the mitochondria of both cell types.

Because our model is utilized to investigate brain glutamate metabolism, it includes the glutamate-glutamine cycle between astrocytes and glutamatergic neurons, referred to as V-cycle. Glutamate, which is the most abundant excitatory neurotransmitter in the brain (Fonnum 1984), is released by presynaptic glutamatergic neurons and rapidly removed by astrocytic glutamate transporters. Once inside the astrocytes, glutamate is metabolized into glutamine through the cytosolic astrocyte-specific enzyme glutamine synthetase (Martinez-Hernandez et al. 1976). Glutamine is further released from astrocytes and taken up by neurons that synthesize glutamate by phosphate-activated glutaminase (PAG), localized on the outer surface of the inner mitochondrial membrane (Kvamme et al. 2000). The biosynthesis of the neurotransmitter glutamate has been modeled following the model suggested by Palaiologos et al. (1988); this model explains the functional role of aspartate aminotransferase (AAT) in glutamatergic neurons. Because it has been shown that, in both cultured astrocytes and neurons, glutamate can be converted into α-ketoglutarate and enters the TCA cycle for further oxidation (Erecinska et al. 1988; Sonnenwald et al. 1997), the bidirectional biochemical reaction GLU⇌AKG has been included in the mitochondria of both cell types.
In neurons, glutamate can be converted into GABA through the GABA shunt, comprising glutamate decarboxylase, GABA transaminase, and SSA dehydrogenase, that allows four of the five carbons lost from the TCA cycle to reenter at the level of succinate (Siesjo 1978; Waagepetersen et al. 1999).

The transport rates of oxygen and glucose are modeled as influxes, whereas the carbon dioxide transports are effluxes. The lactate transports between the two cytosolic domains and the ECS are not forced in either direction, so our system is free to choose the preferred lactate influx/outflux pattern. This modeling strategy allows both cells to produce or utilize lactate in function of their metabolic needs without imposing the activation of either hypothesized metabolic channeling.

**Multicompartment computational model**

Our model can be used for both steady-state and dynamic studies of cellular brain energy metabolism. Although in this analysis, we focus on the steady-state case, hence we are not tracking metabolites and intermediates concentrations, which are assumed to remain constant in time, for sake of completeness, we present an overview of the computational model, which in the future will be employed for dynamic studies following the methodology proposed in (Calvetti and Somersalo 2006; Calvetti et al. 2006).

Metabolic substrates pass from the blood through the blood-brain barrier (BBB) and enter the extracellular space. Whereas in dynamic studies it is important to model the BBB and to account for a partitioning of ECS and blood, in our steady-state analysis, we combine them into a lumped perfectly mixed compartment, referred to as “ECS/blood,” where the substrate dynamics is described by convection and diffusion. The corresponding vector of substrate concentrations is denoted as \( C_a(t) \), where \( t \) is time. The system of differential equations describing the time evolution of the concentrations is of the form

\[
V_b \frac{dC_a}{dt} = Q(C_a - C_v) + \sum_j J_{b,h}^j
\]

where \( V_b \) is the volume of the ECS/blood compartment in the region of interest, \( Q = Q(t) \) is the blood flow, \( C_a - C_v \) is the vector of the differences between arterial and venous concentrations of the biochemical species (GLC, LAC, O2, CO2) tracked in the ECS/blood compartment, and the vector \( J_{b,h}^j \) contains the net transport rates of the substrates between ECS/blood and the cytosol domains of the neurons \( j = 1 \) and astrocytes \( j = 2 \). The concentration vector \( C_b \) is a convex combination of venous and arterial concentration vectors, \( C_b = F C_v + (1 - F) C_a \), with a mixing ratio \( F \), \( 0 < F < 1 \).

Consider the cytosol domain of one cell type \( j \). We denote by \( C_j^c \) the vector of cytosolic concentrations and write the mass balance equation as

\[
V_j \frac{dC_j^c}{dt} = S_j^c \Phi_j^c - J_{c,b}^j - J_{c,m}^j - T^{j_1}_c, \quad j = 1, 2
\]

where \( V_j \) is the compartment domain volume, \( \Phi_j^c \) is the vector of reaction fluxes in the domain, and \( S_j^c \) is the corresponding stoichiometric matrix, expressing how many moles per unit time each species is produced (positive entry) or consumed (negative entry) in each reaction. The transport rates \( J_{c,b}^j \) and \( J_{c,m}^j \) express the net substrate interchange between cytosol and ECS/blood and cytosol and mitochondria in the same cell. Observe that because not all metabolites are exchanged between the compartments, several components of the transport rates are known to vanish. The vector \( T^{j_1} \), which denotes the neuronal activity vector, is present only in the cytosol of the neuron, and it is added to assign an energetic price for neuronal activity. In our model, the neuronal activity increases ATP hydrolysis, \( ATP \rightarrow ADP + Pi \), because it depletes ATP concentration \( T^{j_1}_{ATP} < 0 \) and increases the ADP and phosphate concentrations \( T^{j_1}_{ADP} = T^{j_1}_{Pi} = T^{j_1}_{ATP} > 0 \), hence the \( T^{j_1} \) vector has only three nonzero elements.

Finally, we write the mass balance equation for the concentration vector in the \( j \)th mitochondria as

\[
V_{m,j} \frac{dC_{m,j}}{dt} = S_{m,j} \Phi_{m,j}^c + J_{m,b}^j + J_{m,n}^j, \quad j = 1, 2
\]

where the notation is in agreement with the one in the preceding text.

We couple the neuronal activity with the transport of the neurotransmitter glutamate. Assuming no loss of neurotransmitter in the

*FIG. 1. A schematic of the biochemical pathways in the 5 compartment model of energy metabolism for a cellular complex including astrocyte, glutamatergic neuron and a lapsed blood and extracellular space (shaded area). The markers on the arrows indicate the malate/alpha-ketoglutarate and the glutamate/aspartate antipporter pairs of the malate-aspartate shuttle in each cell type.*
extracellular domain, we lump the transports of glutamate into a single transport between the cytosol compartments of neuron and astrocyte, \( J_{\text{GLU},N \rightarrow A} \), and write \( T_{\text{ATP}} = \alpha_{\text{GLU}} J_{\text{GLU},N \rightarrow A} \). The value of the activity coefficient \( \alpha_{\text{GLU}} \) is chosen on the basis of experimental information that 68% of the cellular metabolic rate is required for maintaining the entire activation machinery associated with the V-cycle (Hyder et al. 2006). In our model, the metabolic rate is identified with the total aerobic and anaerobic ATP production per each unit of glucose (Gjedde et al. 2002). Estimating the total ATP production as \( 2 + 36 = 38 \) units per unit of glucose, we set \( \alpha_{\text{GLU}} = 0.68 \times 38 = 25.84 \). The activity level of the neuron is implemented by imposing a lower bound for the transport rate of glutamate as explained in the following text.

At steady state, the rates of change of the concentrations in Eqs. 1–3 are negligible, leading to a set of homogenous linear equations with respect to the reaction fluxes, transport rates, and concentration differences in the ECS/blood domain. Here we assume that we have an estimate for arterial and venous blood concentrations and consider \( r = Q(C_o - C_v) \) as data. Collecting the reaction fluxes and the nonvanishing components of the transport fluxes in the vector \( u \), the steady-state equations can be written concisely as

\[
Au = b = \begin{bmatrix} 0 \\ r \end{bmatrix}
\]

that is, \( b \) is a vector of zeros (cytosol and mitochondria, Eqs. 2 and 3) and \( r \) as before. The system (Eq. 4) is underdetermined because the matrix \( A \) has a nontrivial null space. To properly handle the null space of \( A \) and to guarantee physiologically meaningful solutions, it is necessary to require that the unknowns satisfy some bound constraints, which include loose upper bounds for the absolute values of the unknowns and nonnegativity for reaction fluxes. Thermodynamics determines the preferred direction of reversible biochemical reactions and facilitated transport rates. Thermodynamic constraints cannot be implemented without information about the values of the concentrations of the substrates, but because at normal steady-state conditions the prevailing directions of many reversible reactions are known, we import this additional information by modeling them as unidirectional. Similarly, the preferred directions of some transport rates at baseline steady state are uncontroversial, thus we only model \( O_2 \) and glucose as influx and \( CO_2 \) as efflux. The information about the activity level of the oxidative phosphorylation reaction flux as a controller ade nosine phosphates or \( pH \) is modeled in both cells using the oxidative phosphorylation activity coefficient.

The crucial bound constraint in our model is related to the regulation of glycolysis by oxidative phosphorylation. It is known that the glycolytic enzymes, HK and PFK, are inhibited by several factors, such as depressed \( pH \) and elevated levels of cytosolic ATP and activated by high ADP/AMP concentrations (Lowry and Passonneau 1964, 1966). The increased energetic need of a cell elevates ADP/AMP concentrations, thus activating the glycolytic enzymes. The concomitant production of pyruvate may result in an increased lactate production or in an increased oxidative phosphorylation, which efficiently restores the ATP/ADP equilibrium and redox states. Therefore in brain cells, where pyruvate is the main oxidative substrate, it is reasonable to posit that oxidative phosphorylation downregulates glycolysis.

Since the steady state computational model utilized for this study does not provide concentration information, the regulation of PFK by adenosine phosphates or \( pH \) is modeled in both cells using the oxidative phosphorylation reaction flux as a controller

\[
\frac{\Phi_{\text{G6P} \rightarrow \text{GA3P}}}{\Phi_{\text{G6P} \rightarrow \text{GA3P}}^0} \leq \frac{1}{1 + \beta \Phi_{O_2 \rightarrow H_2O}}
\]

where the indicated reaction fluxes are intended within the same cell type. The inequality (Eq. 5) conveys the information that an increase in the oxidative phosphorylation activity, \( \Phi_{O_2 \rightarrow H_2O} \), inhibits the PFK, which in our model regulates the G6P breakdown, \( \Phi_{\text{G6P} \rightarrow \text{GA3P}} \). While we do not exclude a prominent role of cytosolic redox in the regulation of glycolysis, because the redox states are affected by lactate dehydrogenase, malate aspartate shuttle, and glycolysis itself, it is not possible to test this alternative without concentration information.

In our computational experiments we set the value of the affinity parameter \( \beta \) to 1 and the saturation value \( \Phi_{\text{G6P} \rightarrow \text{GA3P}}^0 \) was found by a preliminary tuning run as will be explained later.

Bayesian flux balance analysis

The computational steady state model used for our in silico experiments is the stochastic extension of the linear system (Eq. 4), where the unknowns must satisfy the nonlinear inequality constraints \( Cu \preceq c(u) \), the source of nonlinearity in the bounds being the control constraints (Eq. 5). The Bayesian stochastic extension of the linear system (Eq. 4) is analyzed with sampling techniques as explained in Occhipinti et al. (2007), Calvetti et al. (2007), Heino et al. (2007), and Calvetti and Somersalo (2007). More specifically, we first replace the linear system (Eq. 4) by the stochastic model, \( b = Au + e \), where the variables \( b \), \( u \), and \( e \) are random variables. The additive term \( e \), or noise term, accounts for uncertainties in the measured rate \( r \) of transfer across the BBB as well as for the fact that the system may be close to, but not exactly at, a steady state. The stochastic reformulation of the problem is not only in better agreement with the stochastic nature of biological processes but also important from the mathematical and computational perspective. In fact, there is no guarantee that the system (Eq. 4) has a solution that satisfies the bound constraints. We assume that the noise term is a zero mean Gaussian random variable with covariance matrix

\[
\Gamma = \begin{bmatrix} \delta^2 I & \text{diag}(\sigma^2_1, \ldots, \sigma^2_n) \end{bmatrix}
\]

where \( \delta^2 \) is the variance expressing the uncertainty of the system being at steady state, and \( \sigma^2 \) are the variances of the rates of transfer. The choices of these parameters are discussed in connection with the computed results. The likelihood probability density of \( b \) conditional on \( u \) is

\[
\pi(b|u) \propto \exp\left( -\frac{1}{2} (b - Au)^T \Gamma^{-1} (b - Au) \right)
\]

where "\( \propto \)" means “proportional up to a normalizing factor.” The bound constraints are imported in the model via the prior density, which is defined as

\[
\pi_{\text{prior}}(u) \propto \pi_u(Cu - c(u))
\]

where \( \pi_u \) denotes a function that takes on the value 1 if all the components of its argument are positive and vanishes otherwise. By Bayes’ formula, the posterior probability density is

\[
\pi_{\text{post}}(u) \propto \pi_u(b) \pi_{\text{prior}}(u) \pi_{\text{prior}}(b|u) \pi_u(Cu - c(u)).
\]

We explore the posterior probability density using a Markov Chain Monte Carlo (MCMC) scheme appropriate for the present problem. A large sample \{\( u^1, u^2, \ldots, u^n \}\) of vectors distributed according to the probability measure \( \pi_{\text{post}} \) is generated using a Markov transition rule that defines a move from the previous sample point \( u^{n-1} \) to the next one \( u^n \). The method of choice here is a hybrid of full scan Gibbs sampler (Geman and Geman 1984) and the hit-and-run algorithm (Calvetti et al. 2008; Smith 1984).

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We express the vector \( u \) as the sum of two mutually orthogonal components, \( u = v + w \), where \( w \) is in the null space of \( A \), i.e., \( Aw = 0 \). Since the likelihood is independent of \( w \), \( \pi(b|u) = \pi(b|v) \). Given the current sample point \( u^{-1} = v^{-1} + w^{-1} \), we update first \( v^{-1} \to v^{-1} \), drawing the \( k \)th new component value \( v_k^{-1} \) from the Gaussian distribution with bound constraints

\[
v_k^{-1} \sim N(t_{b_k}, c_{v_k})
\]

where we use the notation \( v(k)(t) \).

Conversely the null space component is independent of the likelihood, and the new update \( w \) is drawn from the uniform distribution over the polyhedral domain

\[
t \to \pi(b|v_k(t)), \quad C_{v_k}(t) = (v_k^{-1} + w^{-1}) - C_{w^{-1}}
\]
GLUCOSE SHUNT FOR GLUTAMERGIC NEURONS

TABLE 1. CMR of glucose, oxygen, OGI, Vcycle and total glucose equivalents entering the TCA cycle in astrocyte and neuron at high and low activity

<table>
<thead>
<tr>
<th>Activity</th>
<th>Low</th>
<th>High</th>
</tr>
</thead>
<tbody>
<tr>
<td>CMRGLC</td>
<td>0.36 ± 0.02</td>
<td>0.44 ± 0.01</td>
</tr>
<tr>
<td>CMRO2</td>
<td>1.81 ± 0.10</td>
<td>2.27 ± 0.05</td>
</tr>
<tr>
<td>VTCA</td>
<td>0.60 ± 0.03</td>
<td>0.76 ± 0.02</td>
</tr>
<tr>
<td>Vcycle</td>
<td>0.22 ± 0.06</td>
<td>0.54 ± 0.01</td>
</tr>
<tr>
<td>OGI</td>
<td>5.01 ± 0.08</td>
<td>5.22 ± 0.05</td>
</tr>
</tbody>
</table>

Estimated mean values ± SD in μmol·g tissue⁻¹·min⁻¹ for CMR of glucose, CMR of oxygen, total tricarboxylic acid cycle rate and Vcycle under low and high activities. We also report the mean value ± SD of the predicted oxygen-glucose index (OGI).

\{w \in \mathbb{R}^n \mid Cw \geq (v^j + w^j+1) - Cv^j \}

using the hit-and-run algorithm. The partition of the space into the null space of A and its orthogonal complement can be done in a straightforward manner using the singular value decomposition of the matrix A. Since the resulting update step \(a^j \rightarrow a^{j+1}\) is not reversible, we need to add an acceptance/rejection step as in the Metropolis-Hastings algorithm. It can be shown that with this modification the updating scheme becomes reversible.

This sampling algorithm is quite effective, with computing time in a standard personal 2GB computer using Matlab R2006b of the order of 25 min per 100,000 sample vectors.

RESULTS

In this section, we present the results of our computational experiments, and we explain how they fit into the ongoing debate about cellular brain energy metabolism. Before commenting on the distributions of the values of reaction fluxes and transport rates, we remark that the fluxes of the bidirectional biochemical reactions glycogen synthesis, glycogen phosphorylase, and creatine kinase were not included in the estimation of reaction fluxes and transport rates, we remark that the fluxes of the bidirectional biochemical reactions glycogen synthesis, glycogen phosphorylase, and creatine kinase were not included in the estimation of reaction fluxes and transport rates.

For each activation level, we estimated the posterior mean by 10.22 ± 0.32 ± 2.246 on September 24, 2016 http://jn.physiology.org/ Downloaded from

Before generating the MCMC sample, tuning runs were performed to choose the saturation value of \(\Phi^{0}_{G6P\rightarrow GA3P}\) with different activity levels, using a model without the PFK feedback control inequality (Eq. 5). The saturation value chosen, \(\Phi^{0}_{G6P\rightarrow GA3P} = 0.8 \text{ mmol/min}\), is slightly higher than the upper bound for this flux suggested by the results of test runs with no control on PFK.

The MCMC sampling was preceded by a burn-in run of 600,000 sample points to make sure that all sample histories stabilize. Subsequently, a sample of 100,000 points was generated saving only every 10th vector from a Markov chain of size 1,000,000 to obtain a sample of more independent realizations. Two samples of size 100,000 were generated in this manner, corresponding to high and low neural activity, respectively. Diagnostics of the convergence of the samples, reported in detail in the supplemental materials, were performed by calculating the autocorrelation functions (ACF) of all components, providing an estimate of the correlation lengths of the chain (Calvetti and Somersalo 2007). More specifically, for each unknown, we plot the sample history, the ACF and the histogram as illustrated in Fig. 2. The width of the histogram gives an indication about how tightly the variable is estimated.

For each activation level, we estimated the posterior mean and SD from the collected sample. Tables A3 and A4 of the APPENDIX list the predicted mean values and SDs of all reaction fluxes and transport rates considered in the steady state model. A summary of the overall preferred biochemical pathways suggested by our computational model at the two different activation levels can be found in Fig. 3, where we also indicate the mean values of the key fluxes and transports rates.

Interaction between astrocyte and glutamatergic neuron at high activity

At high activity level, brain energetics follows the original ANLS hypothesis (Pellerin and Magistretti 1994),

\[\text{FIG. 4. Comparison of our model predictions for CMRGLC (left) and VTCA (right) at low (1st bar) and high (2nd bar) neuronal activity and of the experimental results reported by Shen et al. (1999) (3rd bar) and Gruetter et al. (2001) (4th bar).}\]
with a glycolytic activity in astrocyte of $0.36 \pm 0.04 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$, about five times higher than in neuron. Almost all the end product of the astrocyte glycolytic process, pyruvate, is converted into lactate and released in the extracellular space from where it is taken up by the "hungry" neurons. The active glutamatergic neuron utilizes $0.59 \pm 0.07 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$ of the $0.70 \pm 0.07 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$ lactate released by the astrocyte, while the remaining is effluxed into the ECS. In neuron the oxidative phosphorylation flux is $\sim 45$ times faster than in astrocyte, the malate-aspartate shuttle and the TCA cycle activity $\sim 37$ times faster, and the exchange of ATP, ADP and Pi between cytosol and mitochondria $\sim 46$ times faster. The GABA shunt in neuron is $\sim 0.15 \pm 0.14 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$, one-fifth of its TCA cycle flux.

Interaction between astrocyte and glutamatergic neuron at low activity

At low activity, the interaction between the two cell types follows the classical hypothesis with a glycolytic activity in neuron of $0.14 \pm 0.06 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$, only slightly lower than $0.22 \pm 0.06 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$ in astrocyte, and the oxidative activity of astrocytes, $0.61 \pm 0.29 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$ is half the one in neuron, $1.20 \pm 0.28 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$. In astrocyte, $0.21 \pm 0.10 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$ glucose equivalents enter the TCA cycle, the remaining $0.24 \pm 0.19 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$ being converted into lactate and effluxed into the ECS. Although the astrocyte-neuron lactate shuttle is active also during low neural activity, the influx of lactate from the ECS is lower, $0.12 \pm 0.19 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$, about one-fifth of the neuronal lactate uptake at high activity. Our results support the presence of pyruvate carboxylation and malic enzyme in astrocyte. The pyruvate carboxylation flux replenishes the loss of malate in the TCA cycle through the malic enzyme. The GABA shunt in neuron, at $0.20 \pm 0.13 \mu\text{mol} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$, is about one-half of the TCA flux.

Validation of the in silico results

The values of the predicted cerebral glucose utilization, or cerebral metabolic rate (CMRGLC), total tricarboxylic acid
Finally the estimated neuronal lactate uptake from the ECS at high activity is about five times the corresponding lactate influx during low activity, suggesting a proportionality between neuronal lactate uptake and activity levels.

**DISCUSSION**

Our metabolic model, which identifies separate mitochondria and cytosol compartments and accounts for complete glycolytic pathways for both glutamatergic neuron and astrocyte, is a modification of the one proposed in Occhipinti et al. (2007). To avoid coercing the mathematical model of brain energetics toward either the classical or the ANLS hypothesis, we limit the information entered to a bare minimum, namely to the assumption that the system is at a steady state and to the values of arterial-venous differences of glucose, lactate, oxygen, and carbon dioxide, without assuming a priori any imbalances of glucose uptake between the two cell types. We simulate two different levels of neuronal activity by setting the lower bound for the transport rate of glutamate from neuron to astrocyte at high activity four times higher than at low activity. We test whether the regulation of glycolysis by oxidative metabolism can explain the lactate trafficking from astrocyte to neuron by implementing symmetrically in both cells the simplified feedback control inequality (Eq. 5). Since our steady-state analysis does not provide estimates of the concentrations

### Table A1. Cytosol reactions and stoichiometry

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<tbody>
<tr>
<td>1. Hexokinase</td>
<td>GLC+ATP → G6P+ADP</td>
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<td>2. Glycogen synthesis</td>
<td>G6P+ATP → GLY+ADP+2Pi</td>
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<td>3. Glycogen phosphorylase</td>
<td>GLY+Pi → G6P</td>
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<td>5. Glyceraldehyde 3-phosphate dehydrogenase</td>
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<td>6. Pyruvate production</td>
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<td>7. Lactate dehydrogenase</td>
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<td>8. Creatine kinase</td>
<td>PCR+ADP → CR+ATP</td>
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<td>9. ATP hydrolysis</td>
<td>ATP → ADP+Pi</td>
</tr>
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<td>10. Malate dehydrogenase</td>
<td>OAA+NADH → MAL+NAD⁺</td>
</tr>
<tr>
<td>11. Aspartate aminotransferase</td>
<td>Asp+AKG → OAA+GLU</td>
</tr>
<tr>
<td>12. Glutamine synthetase*</td>
<td>GLU+ATP → Gln+ADP+Pi</td>
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<td>Gln → GLU</td>
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Biochemical reactions in the cytosol of astrocyte and neuron. *, the reaction takes place only in the astrocytes.

### Table A2. Mitochondria reactions and stoichiometry

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<tr>
<td>16. Oxidative phosphorylation</td>
<td>O₂+2NADH+6ADP+6Pi → 2H₂O+2NAD⁺+6ATP</td>
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Biochemical reactions in the mitochondria of astrocyte and neuron. †, the reaction takes place only in the astrocytes; †, the corresponding reaction occurs only in neurons.

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Biochemical reactions in the mitochondria of astrocyte and neuron. †, the reaction takes place only in the astrocytes; †, the corresponding reaction occurs only in neurons.
of metabolites and intermediates in the cellular compartments, we link the regulation of glycolysis to oxidative phosphorylation at the level of PFK. The distributions of all reaction fluxes and transport rates are determined by the system as needed to sustain a near steady state.

In addition to the hypothesis of glycolytic regulation, we suggest a mechanism that could be responsible for the control of the glycolysis, namely the allosteric downregulation of PFK and HK by the phosphorylation state. This can be seen as a follow up and extension to the attempts to reconcile the ANLS hypothesis and the classical hypothesis already done in Hyder et al. (2006) and Aubert and Costalat (2005). It is known that the glycolytic enzymes are sensitive to other external conditions such as the cytosolic redox state via pH, and we do not exclude the possibility that the mechanism could be different from the proposed one. The present study is only concerned with steady-state analysis and does not provide any information about the concentrations of metabolites and intermediates. Therefore it is not possible to test if changes in the adenosine phosphate concentrations in cytosol are sufficient to explain the activation of the lactate shuttle, nor can we exclude the possibility that the control of glycolysis is exerted by the redox state. However, the statistical framework of our analysis makes it possible to consider the correlation between oxidative phosphorylation and the malate aspartate shuttle, on one hand, and lactate dehydrogenase on the other, which together with glycolysis itself are the main controllers of the redox state. From the corresponding scatters plots, shown in Figs. 5 and 6, it is clear that oxidative phosphorylation is highly correlated with the malate-aspartate shuttle at both activity levels and in both cell types, while its correlation with lactate dehydrogenase is much lower at high neuronal activity, not excluding the possibility that the primary glycolytic controller could indeed be the redox state or a more complex interplay between the redox and phosphorylation states. The observation that in some cellular systems a high glycolytic activity with lactate production can occur concurrently with high oxidative metabolism levels (Kemper et al. 2001) suggests that mechanisms behind the regulation of glycolysis can be more complex, in particular in the presence of alternative sources of oxidative substrates.

The inclusion of the main biochemical pathways that could be active under either hypothesis of brain energy metabolism makes our five compartment model substantially more complex.
plex than previously published ones (Aubert and Costalat 2005; Aubert et al. 2005, 2007; Gruetter et al. 2001). In this model, we also implement a physiological mechanism that regulates glycolysis and explains the lactate trafficking without assuming uneven partitioning of glucose uptake. In the debate on brain energy metabolism, the difference in availability of substrates to astrocyte and neuron has received a lot of attention without being definitely resolved. The closer proximity of astrocytes to the capillaries has been used to argue their easier—and more plentiful—access to glucose and hence their higher glycolytic activity. The presence of glucose transporters, mainly GLUT-1 in the membranes of astrocytes and of GLUT-3 in the membranes of neurons (Gjedde 2007), nonetheless undermines this argument. Recently it has been pointed out (Gjedde 2007) that “under normal circumstances, glucose transport is not rate limiting and glucose concentrations in the different cellular compartments of brain tissue are likely to be similar.” However, the experimental results reported by Loaiza et al. (2003) and Porras et al. (2004) indicate that increased extracellular glutamate concentration inhibits glucose uptake in neurons and activates it in astrocytes. The mechanism of this regulation and its connection to the ANLS is yet to be fully explained. The uneven partitioning of glucose uptake for the two cell types implemented in Aubert et al. (2005, 2007) and Occhipinti et al. (2007) could be therefore supported in the light of these findings. Our present model does not assume uneven partitioning of glucose uptake but it does not exclude it either. Thus it is the first model of the astrocyte-neuron cellular complex that permits both an even and an uneven partitioning of the transport of glucose as a function of neuronal activity without asymmetric regulation of glucose uptake and lactate trafficking. Our model predicts that at high activity the transport rate of glucose from ECS/blood to astrocyte is approximately five times higher than from ECS/blood to neuron, whereas it is only 1.5 times higher at low activity.

Our analysis suggests that indeed at high neuronal activity the glutamatergic neuron fuels its energetic needs by taking up astrocyte produced lactate. The shunting of lactate from astroocyte to neuron is made possible by accounting for influx and efflux of lactate from both cell types into the ECS/blood compartment. In our model, both cells can efflux/influx lactate into/from the ECS/blood compartment, leaving it up to the system to decide the lactate trafficking needed to sustain a steady state at a specified activity level. Our model suggests that at high neuronal activity lactate produced anaerobically by astrocyte is effluxed into the ECS/blood compartment, from which it is taken up by the neurons where it undergoes oxidation. While most of the astrocyte produced lactate is taken up by the neuron, a portion of it, independent of the activation level, leaks into the ECS/blood compartment, in agreement with published results. The mechanism whereby glucose transformed into lactate by astrocyte glycolysis undergoes oxidation in neuron, according to our model appears to be the way to bypass the impaired glycolysis in neuron.

The predictions of our model are qualitatively in agreement with the results reported in a recent review (Hyder et al. 2006). A direct quantitative comparison with the values reported there is not immediate because their model lumps glutamatergic and GABAergic neurons and different values for neuronal activity are used.

APPENDIX

In this appendix, we present the biochemical reactions included in the model and their stoichiometry, see Table A1 for cytosol and Table A2 for mitochondria. The posterior mean and SDs of the reaction fluxes and transport rates found by our Bayesian flux balance analysis at high and low neuronal activity are reported in Tables A3 and A4.

GRANTS

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REFERENCES


