Adaptation and Temporal Decorrelation by Single Neurons in the Primary Visual Cortex

Xiao-Jing Wang,1 Yinghui Liu,1 Maria V. Sanchez-Vives,2 and David A. McCormick3

1Volcan Center for Complex Systems, Brandeis University, Waltham, Massachusetts 02454; 2Instituto de Neurociencias, Universidad Miguel Hernandez-Consejo Superior de Investigaciones Cientificas, San Juan de Alicante, Spain; and 3Department of Neurobiology, Yale University School of Medicine, New Haven, Connecticut 06510

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INTRODUCTION

In natural environments, sensory inputs from the external world to the brain are statistically redundant, characterized by strong and long-range correlations in space (Ruderman 1994; Ruderman and Bialek 1994) and in time (Doug and Atick 1995a; van Hateren and van der Schaaf 1996). For the brain to encode sensory stimuli and detect changes efficiently, it is desirable to reduce input redundancy through a decorrelation operation (Atick 1992; Attneave 1954; Barlow 1961; Barlow and Foldiak 1989; Field 1994; Srinivasan et al. 1982). In the visual system, theoretical models, natural scene analysis, and physiological studies have shown that decreases of redundancy by decorrelation is key to the efficient neural encoding of images (Bell and Sejnowski 1997; Dan et al. 1996; Dong and Atick 1995b; Laughlin 1981; Olshausen and Field 1996; Vinjı and Gallant 2000. For a review, see Simoncelli and Olshausen 2001). Barlow (1961, 1990) suggested that decorrelation could be subserved by neuronal adaptation in the neocortex. This idea is supported by recent work demonstrating that neuronal adaptation occurs over a wide range of time scales (Fairhall et al. 2001) and that these adaptation dynamics can serve to maximize information transmission (Baddeley et al. 1997; Brenner et al. 2000; Wainwright 1999). It is thus of considerable interest to identify cellular and synaptic mechanisms of adaptation and to investigate whether the same mechanisms can also subserve decorrelation in the brain.

In the primary visual cortex (V1), a neuron’s response to a low-contrast visual pattern is substantially reduced (adapted) following a few seconds of stimulation (Ahmed et al. 1997; Blackmore and Campbell 1969; Càrandoni et al. 1998; Dragoi et al. 2000; Greenlee and Heitger 1988; Greenlee et al. 1991; Maffei et al. 1973; Movshon and Lennie 1979; Nelson 1991; Ohzawa et al. 1985; Sclar et al. 1985; Vidyasagar 1990). This history-dependent adaptive gain control allows visual cortical neurons to display a high sensitivity without being limited by saturation or insensitivity. In addition, pattern adaptation provides a mechanism to reduce redundancy in the processing of natural scenes—by removing temporally constant stimuli while remaining responsive to more rapid changes. Several mechanisms have been proposed for contrast adaptation of V1 neurons, including a slow form of synaptic depression (time constant: 10 s) (Adorjàn et al. 1999; Chance et al. 1998; Finlayson and Cynader 1995). Recent studies with intracellular recordings of cat primary visual cortical neurons in vivo revealed that prolonged (tens of seconds) presentation of optimal high-contrast visual stimuli results in a hyperpolarization of the recorded cell (Càrandoni and Ferster 1997; Sanchez-Vives et al. 2000a). This hyperpolarization correlates with the persistent decrease in sensitivity following adaptation and appears to be generated through ionic mechanisms intrinsic to single neurons. For example, intracellular current injection into single cortical cells could replicate the hyperpolarization induced by high-contrast visual stimuli (Sanchez-Vives et al. 2000a). Ex-
amination of similar hyperpolarizations generated in response to prolonged action potential activity in vitro reveal that it is generated by a Ca\(^{2+}\)-activated K\(^+\) current \(I_{KCa}\) and especially a Na\(^+\)-activated K\(^+\) current \(I_{KNa}\) (Sanchez-Vives et al. 2000b).

Based on these data, we constructed a conductance-based model of a visual cortical neuron endowed with \(I_{KCa}\) and \(I_{KNa}\). The model was calibrated by reproducing the adaptive neural response to long-lasting sinusoidal currents (Sanchez-Vives et al. 2000b). Using correlated stochastic inputs (with 2nd-order statistics of natural scenes), we show that adaptation currents endow the model neuron with the ability to remove long-range temporal correlations in the input so that the output spike discharges are decorrelated at long time scales. Applying the same protocol of stochastic inputs to V1 cells in cortical slices, we found that neurons of primary visual cortex can indeed remove long-range temporal correlations in the stochastic inputs. Furthermore, an enhancement of the slow hyperpolarization in single cells increased the degree of decorrelation. These results suggest that intrinsic adaptation ionic currents provide a candidate cellular mechanism for temporal decorrelation in V1 neurons.

**METHODS**

**The model**

We were primarily motivated by the observation that slow membrane hyperpolarization resulting from repetitive activation of cortical neurons is largely produced by sodium/calcium-dependent potassium currents (Sanchez-Vives et al. 2000a,b). Here we implemented both types of adaptation currents in a Hodgkin-Huxley-type conductance-based model (Hodgkin and Huxley 1952). The model was modified from Wang (1998) with the addition of a sodium-activated potassium current \(I_{KNa}\).

The model has two compartments, one representing the soma/axonal initial segment (\(V_s\)), the other representing the dendrite (\(V_d\)) (Pinsky and Rinzel 1994). The spike-generating Na\(^+\) current is distributed in both compartments and activate Ca\(^{2+}\)-dependent K\(^+\) currents \(I_{KCa}\). A slow Na\(^+\)-activated K\(^+\) current \(I_{KNa}\) is located in the somatic compartment.

The model obeys the following seven differential equations:

\[
\begin{align*}
C_m \frac{dV_s}{dt} &= -I_h - I_{Na} - I_K - I_{Ca,s} - I_{KCa,s} - I_{KNa} - (g_L/p)(V_s - V_L) + I \\
\frac{dh}{dt} &= \phi_h[\alpha_h(V_s)(1 - h) - \beta_h(V_s)h] \\
\frac{dn}{dt} &= \phi_n[\alpha_n(V_s)(1 - n) - \beta_n(V_s)n] \\
\frac{d[Ca^{2+}]}{dt} &= -\alpha_{Ca,J_{Ca,s}} - [Ca^{2+}]/\tau_{Ca,s} \\
\frac{d[Na^+]}{dt} &= -\alpha_{Na,J_{Ca,s}} - 3R_{Na}\phi_0([Na^+]_s) - \phi_0([Na^+]_s) \\
C_m \frac{dV_d}{dt} &= -I_h - I_{Na} - I_{K,\text{d}} - (g_L(1 - p))(V_d - V_L) \\
\frac{d[Ca^{2+}]}{dt} &= -\alpha_{Ca,J_{Ca,d}} - [Ca^{2+}]/\tau_{Ca,d} \\
\end{align*}
\]

where \(C_m = 1 \, \mu F/cm^2\), \(I\) is the applied current, and the leak current is \(I_L = g_L(V_s - V_L)\). The coupling current between soma and dendrite is proportional to \((V_s - V_d)\), with coupling conductance \(g_c = 2 \, mS/cm^2\). The parameter \(p = (\text{somatic area/total area}) = 0.5\). Maximum conductances \(g_L = 0.1\), \(g_{Na} = 45\), \(g_K = 18\), \(g_{Ca,s} = 1.5\), \(g_{Ca,k,s} = g_{KCa,s} = 5\), \(g_{KNa} = 5\) in mS/cm\(^2\). The reversal potentials \(V_L = -65\), \(V_{Na} = +55\), \(V_K = -80\), \(V_{Ca} = +120\) in mV.

The voltage-dependent currents are described by the Hodgkin-Huxley formalism (Hodgkin and Huxley 1952). The dynamics of the gating variable \(x\) follows first-order kinetics

\[
\frac{dx}{dt} = \phi_x[\alpha_x(V_s)(1 - x) - \beta_x(V_s)x] \\
= \phi_x\left(x_s(V_s) - x\right)\tau_x(V_s)
\]

with \(x_s(V) = \alpha_x(V)/(\alpha_x(V) + \beta_x(V))\) as the steady-state value and \(\tau_x(V) = 1/(\alpha_x(V) + \beta_x(V))\) as the time constant, and \(\phi_x\) is the temperature factor.

The sodium current in the somatic compartment is \(I_{Na} = g_{Na,S}m_d(V_s)(V_s - V_{Na})\). The fast activation variable is \(m_d\) replaced by its steady-state value \(m_{Na}(V_s)\) (given that \(\tau_m\) is only a fraction of a millisecond): \(m_{Na} = \alpha_{Na}(V_s)/[\alpha_{Na}(V_s) + \beta_{Na}(V_s)] \approx -0.1(V_s + 33)/(\exp[-0.1(V_s + 33)] - 1)\) and \(\beta_{Na}(V) = 4 \exp[-(V_s + 58)/12]\). The inactivation variable \(h\) for \(I_{Na}\) is described by \(\alpha_h(V_s) = 0.07 \exp[-(V_s + 50)/10] \approx 0.01(V_s + 20)/1 + 1\). The delayed rectifier is \(I_K = g_Kn(V_s - V_K)\), with the activation variable \(n\) described by \(\alpha_n(V_s) = -0.01(V_s + 34)/(\exp[-0.1(V_s + 34)] - 1)\) and \(\beta_n(V_s) = 0.125 \times \exp[-(V_s + 44)/25]\). The temperature factor \(\phi_h = \phi_n = 4\).

The high-threshold calcium current \(I_{Ca} = g_{Ca,S}V_d^2(V_s - V_{Ca})\), where the activation variable \(v\) is replaced by its steady-state value \(v_{Ca}(V_s) = 1/\left[1 + \exp[-(V_s + 20)/9]\right]\) because of its fast dynamics. The voltage-independent, calcium-activated potassium current \(I_{KCa} = g_{Ca,K}(C_{[Ca^{2+}]} + K_D)(V_s - V_{K})\), with \(K_D = 30\) \(\mu M\). The intracellular calcium concentration \([Ca^{2+}]\) is assumed to be governed by a linear equation with \(\alpha_{Ca}\) proportional to the ratio of the membrane area and the volume immediately beneath the membrane, \(\alpha_{Ca} = 0.002 \, \mu M^{-1} \text{cm}^2\) in the dendritic compartment and 0.00067 \(\mu M^{-1} \text{cm}^2\) in the somatic compartment. The various extrusion and buffering mechanisms are described collectively by a first-order decay process with a time constant \(\tau_{Ca} = 80\) ms in the dendritic compartment and 240 ms in the somatic compartment (Helmchen et al. 1996).

The Na\(^+\)-activated K\(^+\) current \(I_{KNa}\) (Dryer 1994; Egan et al. 1992a,b; Kameyama et al. 1984; Schwinding et al. 1988, 1989) is modeled according to a quantitative study of this ionic current in dorsal root ganglion cells (Bischoff et al. 1998). The intracellular \([Na^+]\), concentration is incremented by Na\(^+\) influx through \(I_{Na}\) during action potentials. (In cortical neurons, Na\(^+\) influx could also be contributed by synaptic currents, which we do not model here for the sake of simplicity.) The Na\(^+\)-dependent K\(^+\) current \(I_{KNa} = g_{KNa}\omega_s([Na^+]_s)(V_s - V_{Ca})\), with the activation function \(\omega_s([Na^+]_s)\) given by (Bischoff et al. 1998)

\[
\omega_s([Na^+]_s) = \frac{P_{max}}{1 + (EC_{50}/[Na^+]_s)^v} 
\]
where $P_{\text{max}} = 0.37$ defines the maximum opening probability of the channels. $E_{C_{50}} = 38.7$ mM is the [Na$^+$] for half activation and the Hill coefficient $n_H = 3.5$. The influx of [Na$^+$] is controlled by $-\alpha_{Na} [\text{Na}^+]$. We chose $\alpha_{Na} = 0.0003$ mM (ns$\mu$A)$^{-1}$ cm$^2$ so that the influx of [Na$^+$] is $\sim 100$ $\mu$M per action potential. This number is consistent with the measurements using the Na$^+$-sensitive dye SBF1 from hippocampal pyramidal neuron’s soma and dendrites (Jaffe et al. 1992; Rose and Ransoms 1997; Rose et al. 1999). Although SBF1 imaging gives only relative changes rather than absolute Na$^+$ concentration, indirect estimates range from 50 to 300 $\mu$M/spike (Rose et al. 1999; W. N. Ross, personal communication).

The extrusion of [Na$^+$], assumed to be largely due to a Na$^+/K^+$ ionic pump, which extrudes three Na$^+$ ions for every two K$^+$ ions brought into the cell (Fain 1999). Previous in vitro studies (Sanchez-Vives et al. 2000a) show that the slow afterhyperpolarization following prolonged discharge is mediated largely by $I_{\text{KNa}}$ with a relatively small or latent contribution by the Na$^+/K^+$ pump. Therefore here we have focused on the influence of $I_{\text{KNa}}$ on temporal decorrelation and for simplicity have not included the current generated by the Na$^+/K^+$ pump. However, our conclusions would remain the same, if such a current is taken into account, because it has the same time course as $I_{\text{KNa}}$.

The [Na$^+$], extrusion by the ionic pump was modeled (Li et al. 1996) as $-3R_{\text{pump}} (\psi_{\text{Na}}([\text{Na}^+]_{\text{eq}}) - \psi_{\text{Na}}([\text{Na}^+]_{\text{in}}))$ where $\psi_{\text{Na}}(x) = x/(x + K_p)$ with $K_p = 15$ mM. The cubic nonlinearity is related to the cooperative binding of three Na$^+$ ions to the pump molecule in the early steps of Na$^+$ transport. $R_{\text{pump}} = 0.0006$ mM/ms. The sodium concentration at the resting state is assumed to be $[\text{Na}^+]_{\text{eq}} = 8$ mM (Galvan et al. 1984; Grafe et al. 1982). The equilibration of [Na$^+$], is a nonlinear process and takes tens of seconds. The very slow kinetics of the Na$^+/K^+$ ionic pump is important for the model to reproduce visual cortical neurons’ slow adaptation behavior.

Model simulations were carried out on a PC Pentium computer, using the fourth-order Runge-Kutta integration method and a time step of 0.05 ms.

**Temporally correlated input**

The spatial-temporal power spectrum $S(k,f)$, where $k \sim 1/L$ is the spatial frequency and $f \sim 1/T$ is the temporal frequency, has been used to characterize the second-order statistics of natural scenes. Typically, the spatial power spectrum of a natural image behaves $\sim k^2$ (Ruderman 1994). The temporal power spectrum scales like $1/f^2$ when observed with a broad visual field (at large $L$) and $1/f$ when observed with a narrow visual field (small $L$) (Dong and Atick 1995a; van Hateren 1997). The characteristic relationship between power and frequency reflect strong temporal-spatial correlations present in natural scenes. Both $1/f^2$ and $1/f$ type inputs were used in this study.

A temporally correlated stochastic input with $1/f^2$ type spectral scaling can be generated by an Ornstein-Uhlenbeck process as

$$\frac{d\tilde{f}}{dt} = -R_{\tau_{\text{corr}}} + \sigma \eta(t)$$

where the decay time constant is $\tau_{\text{corr}} = 2000$ ms, $\eta(t)$ is a Gaussian white-noise term, and $\sigma$ is the standard deviation of the noise distribution. Note that the precise value of $\tau_{\text{corr}}$ is not important as long as it is large enough so that the power spectrum of the input has a reasonable range of $1/f^2$ scaling (see following test). The generated input $\tilde{f}(t)$ is a correlated stochastic process, its autocorrelation function is

$$\langle \tilde{f}(t) \tilde{f}(t + \tau) \rangle = \langle \sigma^2 \tau_{\text{corr}} \rangle \exp(-\tau/\tau_{\text{corr}})$$

which shows a positive correlation with characteristic correlation range $\tau_{\text{corr}}$. The power spectrum of $\tilde{f}(t)$ is

$$S(f) = \frac{\sigma^2}{\omega^2 + (1/\tau_{\text{corr}})}$$

Therefore $S_1 \sim \sigma^2/\omega^2$ for $1/\tau_{\text{corr}} \ll \omega$. Therefore, a good range of $1/f^2$ scaling can be realized for a sufficiently long $\tau_{\text{corr}}$. The power reaches a plateau at very low frequencies $\omega < 1/\tau_{\text{corr}}$, or $f = \omega/2\pi < 1/(2\pi\tau_{\text{corr}}) = 0.1$ Hz.

There is no simple stochastic differential equation for generating $1/f$-type inputs. Therefore we used another method, derived from an explicit $1/f$ power spectrum through the inverse Fourier transform

$$\tilde{f}(t) = \int \sqrt{S(f)} \tilde{\xi}(f) e^{i2\pi f t} df$$

where $S(f) \sim 1/f$ and $\tilde{\xi}(f)$ is a Gaussian white-noise term with a prescribed variance, and $\phi(f)$ is a statistically independent random phase. By this construction, the power spectrum of $\tilde{f}(t)$ is $\langle \tilde{\xi}(f) \tilde{\xi}(f') \rangle = S(f)$. Experimental evidence indicates that the early stage of visual signal processing (such as a photoreceptor) acts as a low-pass filter and the power for frequencies $>20$–$30$ Hz is filtered out (van Hateren 1997). To mimic this in our model, we introduced a cutoff of $|S(f)| = 0$ for $f > 20$ Hz.

**Temporal correlation of the neuronal activity**

A spike train is a point process described by a sequence of delta functions in time $s(t) = \sum \delta(t - t_i)$. One could calculate directly the autocorrelation function of this point process (Gabbiani and Koch 1998). However, to assess the decorrelation effect, we need to compare the time correlation of the output with that of the signal, which is an analog quantity. For this reason, we converted the discrete spike train into a continuous instantaneous rate function $r(t) = 1/(t_{i+1} - t_i)$ for $t_i < t < t_{i+1}$. The autocorrelation function for $r(t)$ is calculated, with normalization, as follows

$$\phi(\tau) = \frac{\int_{T} r(t + \tau) dr - \left(\int_{T} r(t) dt\right) \left(\int_{T} \tau(t) dt\right)}{\left(\int_{T} r(t) dt\right)^2}$$

with $\phi(-\tau) = \phi(\tau)$, $-1 \leq \phi(\tau) \leq 1$ and $\phi(\tau = 0) = 1$. The same formula is used to compute the autocorrelation function of the input current $I(t)$. Because both are normalized to 1 at $\tau = 0$, the input and output autocorrelations can be compared directly on the same graph.

The power spectrum density is calculated directly from long time series (time duration $T > 50$ s if $f_{\text{min}} = 1/T < 0.02$ Hz). We normalized the power spectrum so that its integral (the total power) is the same for the input and the output. This allowed the relative power at different frequencies in the input and output to be compared.

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In vitro experimental work

To test the theoretical predictions, intracellular recordings were performed from layers 2/3 and 4 (pyramidal and spiny stellate) neurons in primary visual cortex slices from the ferret. Ferrets were cared for and used in accordance with all appropriate regulatory guidelines. For the preparation of slices, 2- to 4-month-old ferrets of either sex were deeply anesthetized with pentobarbital sodium (40 mg/kg) and killed by decapitation. The forebrain was rapidly removed, and the hemispheres were separated with a midline incision. Four-hundred-micrometers-thick coronal slices of the primary visual cortex were cut on a vibratome (DSK Microslice; Ted Pella, Redding, CA). A modification of the technique developed by Aghajanian and Rasmussen (1989) was used to increase tissue viability. During preparation of slices, the tissue was placed in a solution in which NaCl was replaced with sucrose while maintaining an osmolarity of 307 mosM. After preparation, slices were placed in an interface style recording chamber (Fine Sciences Tools, Foster City, CA). Cortical slices were superfused for the first 10 min with an equal mixture by volume of the normal bathing medium and the sucrose-substituted solution. Following this, normal bathing medium was switched into the chamber throughout the experiment. Bath temperature was maintained at 34–35°C.

Intracellular recordings were initiated following 2 h of recovery. The normal bathing medium contained (in mM) 124 NaCl, 2.5 KCl, 2 MgSO4, 1.25 NaHPO4, 2 CaCl2, 26 NaHCO3, and 10 dextrose and was aerated with 95% O2-5% CO2 to a final pH of 7.4. Block of transmembrane Ca2+ currents was achieved by replacing CaCl2 with either MnCl2 or CoCl2 while sodium phosphate was omitted from the bathing medium to avoid precipitation.

Sharp intracellular recording electrodes were formed on a Sutter Instruments (Novato, CA) P-80 micropipette puller from medium-walled glass (1BF100, WPI Sarasota, FL) and beveled on a Sutter Instruments beveller to final resistances of 50–100 MΩ. Micropipettes were filled with 2 M Kacetate. Only those cells that maintained a stable resting membrane potential and responded to depolarizing current injection with the generation of trains of action potentials were included for analysis. In addition to square current pulses and sinusoidal currents, correlated stochastic currents with either I/f2 or I/f statistics—the same inputs used in model simulations—were also injected into the recorded cells. Clampex 6.0 (Axon Instruments) was the software used to transform the numerical series into an intracellular mechanism to remove temporal redundancy in the input. For the purpose of this study, the size of the slow afterhyperpolarization in a cell was measured from responses to either current pulses or sinusoidal currents of long duration. The temporal correlations in the output spike trains were analyzed and compared with that of the injected waveform.

RESULTS

Adaptive response to high-low sinusoidal current input

We first calibrated our model by simulating intracellular data from visual cortical neurons (Sanchez-Vives et al. 2000b). To compare the model with data, we used the same low-high-low intensity pattern of 2-Hz sinusoidal injected current in the simulation as in the experiments (Fig. 1). The 2-Hz sinusoidal current input in the model has a mean of 2 μA/cm². The low-intensity input (with an amplitude of 0.3 μA/cm²) is applied before and after the high-intensity input (amplitude of 3 μA/cm², duration of 20 s). The model cell generates two spikes per cycle with the low-intensity input before the high-intensity input. At the beginning of the high-intensity current, as many as nine spikes are generated during the first cycle. The steady state of four spikes per cycle is reached after slow adaptation (Fig. 1B). Following the high-intensity sinusoidal current, a prolonged slow afterhyperpolarization (sAHP) of ~10 s can be observed (Fig. 1A). These results are similar to those obtained with recordings of visual cortical neurons in vitro (Sanchez-Vives et al. 2000b). The effects of IKCa and IKNa are clearly different in the model. Because the decay time constant for [Ca2+], is only 80 and 240 ms (in the dendritic and somatic compartments) and each cycle is 500 ms long, [Ca2+], does not accumulate over cycles and IKCa is effective as a feedback control mechanism only within a cycle (Fig. 1D). By contrast, IKNa is much slower. During low-intensity sinusoidal stimulation, intracellular [Na+], has a steady state of ~14 mM (Fig. 1C). During high-intensity stimulation, [Na+], accumulates slowly to a plateau level of 17.5 mM. The time course is exponential with a time constant of τadap = 4 s. A qualitative derivation of τadap is given in the appendix (see also Liu and Wang 2001; Wang 1998). The same exponential time course is seen for the decreasing instantaneous firing rate associated with adaptation (Fig. 1B), showing that the slow spike-frequency adaptation is caused by the increase of [Na+], hence IKNa. The slow afterhyperpolarization following the high-intensity stimulation displays a similar time course as [Na+], and the decay of IKNa controls the time course of the post-adaptation recovery of neuronal excitability. The decay time constant of sAHP is therefore governed by the slow kinetics of the Na+/K+ pump. When the [Na+] is around [Na+]eq = 8 mM, its decay through the ionic pump can be approximately linearized by (φ) = φ(Na) = φ(Na)φ(Na–) = φ(Na–) = 0.220.33.5 on June 22, 2017 http://jn.physiology.org/ Downloaded from
As shown in Fig. 2, in response to such a correlated stochastic current, the model neuron’s spike activity is not a linear transformation of the input (Fig. 2A). Compared to the input, the output autocorrelation is suppressed at long time scales, and is zero for $\tau > 2$ s (Fig. 2B). The power spectrum shows a relative enhancement at high frequencies ($>1$ Hz). Concomitantly, there is a relative loss of power at low frequencies ($<0.1$ Hz), the plateau is reduced from 1.8 for the input to 0.5 for the output (Fig. 2C).

We noticed that decorrelation could occur even without
adaptation currents if the model neuron fires at such a low rate that the spike discharges before and after a long silent episode could become statistically uncorrelated. We examined this effect by removal of the adaptation currents from the model cell. Replacing the adaptation currents with constant current injection revealed that obtaining decorrelation effects similar to those of the intact model (e.g., such as those illustrated in Fig. 2) required the average firing rate to be very low ($r < 1–2$ Hz; data not shown). Roughly speaking, to achieve significant decorrelations, the average interspike interval ($1/r$) should be comparable to, or longer than, the input correlation time (e.g., seconds in the present case). When the firing rate is reasonably high ($\approx 10$ Hz), this effect cannot produce significant decorrelation of input.

In the presence of the slow adaptation currents $I_{KCa}$ and $I_{KNa}$, the activation of $I_{KNa}$ occurs in response to action potential activity as a slow negative feedback (as opposed to the constant injection of current) such that the occurrence of slow modulations of the membrane potential are decreased, whereas fast modulations are left intact. Thus the activation of adaptation currents in response to activity is more effective in reducing slow temporal correlations without destroying the fast responsiveness of the neuron (e.g., the membrane potential is “recentered” during slow changes as opposed to just simply constantly hyperpolarized). Maintained periods of depolarization and activity result in an increase in activation of the adaptation current therefore a reduction in excitability, whereas prolonged periods of hyperpolarization result in a de-activation of the adaptation currents and consequently an increase in neuronal responsiveness. Consequently, while without adaptation, the neuron’s current threshold for spike discharges is 0.5 $\mu$A/cm$^2$, in the presence of slow adaptation (e.g., during periods of sustained current injection), the neuron do not fire all the time even though the average injected current ranges from 1 to 4 $\mu$A/cm$^2$ (Fig. 2A).

**Decorrelation of 1/f-type inputs by $I_{KCa}$ and $I_{KNa}$ at separate time scales**

In contrast to an 1/f$^2$-type input generated by an Ornstein-Uhlenbeck process, an 1/f-type input displays temporal correlations over arbitrarily long time scales: its autocorrelation is large over many seconds, and its power spectrum increases as 1/f at low frequencies (Fig. 3, B and C). The input shows very slow time modulations (Fig. 3A, top). Compared to Fig. 2, there is also larger fluctuations at high frequencies because the power decreases more slowly (1/f) than an 1/f$^2$ input. In the absence of $I_{KCa}$ and $I_{KNa}$, the model neuron transduces the input faithfully, the autocorrelation function and power spectrum of its spike train output is identical to those of the input (data not shown). Endowed with adaptation currents, the model neuron shows transient activity (Fig. 3A, 3rd panel). The autocorrelation quickly decays to zero within 500 ms (Fig. 3B). Compared to the input, the output power spectrum shows a strong suppression at low frequencies. In effect, the output spectrum is flattened or “whitened” for $f < 0.1$ Hz, in contrast to the increases according to 1/f for the input (Fig. 3C). The transient nature of the neural activity is not simply due to a constant hyperpolarization but to time-dependent negative feedback. Compare for instance the two time windows indicated by horizontal bars, each lasting for 10 s (Fig. 3A, top). The second marked time window has a lower average “ambient” input current $I$ than the first one. However, the first time window is preceded by a period of high activity and a large $[\text{Na}^+]_i$ plateau (hence a strong $I_{KNa}$), whereas the second time window follows a period of relative quiescence (Fig. 3A). As a result, the effective current input $I - I_{KNa}$ is larger, and the overall firing rate is actually slightly higher (8 Hz) during the second time window than that (7.6 Hz) during the first time window. Therefore, the slow changes in $[\text{Na}^+]_i$ track the input history over a period of seconds. The subsequent activation of $I_{KNa}$ then acts as a negative feedback signal, the size of which...

![Fig. 2. Decorrelation of 1/f$^2$-type stochastic inputs. A: membrane potential (top), instantaneous firing rate (middle), and input current (bottom). B: the autocorrelation function of the output is reduced compared to that of the input at all time scales and is essentially 0 for $\tau > 2$ s. C: power spectrum analysis for both the output and the input. The relative power for the output is reduced at low frequencies and enhanced at high frequencies.](http://jn.physiology.org/.)
is proportional to the time-averaged input in the recent past. The neuron becomes relatively insensitive to “ambient” input levels, yet still responds vigorously to transient input changes thanks to the lagged action of slow adaptation.

How large are the increases in membrane conductance that mediate these effects? An increase of the internal Na$^{+}$/H$^{+}$ from 17 to 20 mM in the model leads to an increase of $g_{KNa}$ by 0.07 $\mu$S/cm$^2$, resulting in an increase in total resting membrane conductance of only 30%. Thus the temporal decorrelation occurs largely through slow changes in membrane potential (recentering) mediated by activation and de-activation of the adaptation currents and not through a “shunting” of the membrane.

We have examined the differential roles of $I_{KCa}$ and $I_{KNa}$ in the reduction of input redundancy. Without adaptation by either $I_{KNa}$ or $I_{KCa}$, the output firing rate time course is nearly identical to the time course of the inject current (Fig. 4A). Addition of $I_{KCa}$ alone leads to a suppression of the slow temporal modulation of the firing output compared to the input. This effect is significant only at moderate frequencies that
match the time scale of activation and deactivation of this current. This appeared as a “flattening” of the power-frequency relationship between 1 and \( \sim 10 \) Hz. At low (<1 Hz) frequencies, \( I_{KCa} \) is not persistent enough to influence interspike intervals, and therefore the power-frequency relationship has a similar shape as without \( I_{KCa} \) (see Fig. 4B). The relative power at 1–20 Hz is enhanced (Fig. 4B). At higher frequencies (>20 Hz), the rate of activation of \( I_{KCa} \) is too slow to have a significant effect on the firing temporal fluctuations. In the Appendix, we provide an analytical derivation to show that the relative enhancement of power at 1–20 Hz is due to a high-pass filtering of inputs by the adaptation current \( I_{KCa} \).

The addition of \( I_{KNa} \) to the model results in a marked flattening of the power-frequency relationship at frequencies below \( \sim 1 \) Hz (Fig. 3). This effect is dependent upon the time scale of the [Na\(^+\)]\()_i\) dynamics as demonstrated directly by accelerating the [Na\(^+\)]\()_i\) kinetics with a scaling factor \( \phi_{Na} \) (so that both the influx and extrusion are faster)

\[
\frac{d[Na^+]_i}{dt} = \phi_{Na}(-\alpha_{Na}^{in} - 3\beta_{Na}(\phi_{Na}[Na^+]_i - \phi_{Na}(Na^+)])
\]  

while all other parameters were maintained. As \( \phi_{Na} \) is increased from 1 to 2 and 4, the temporal decorrelation by \( I_{KNa} \) at relatively short temporal ranges (<2 s) becomes more effective as shown in the autocorrelation function (Fig. 4C, left). The power spectrum shows stronger flattening (whitening) in the frequency range \( \leq 1 \) Hz (Fig. 4C, right). The relative power at higher frequencies, however, remains unaffected.

Temporal decorrelation in visual cortical neurons

To test whether real cortical neurons can indeed decorrelate the inputs by intrinsic adaptation mechanisms, we used intracellular recordings from layer 2/3 pyramidal and layer 4 stellate neurons (n = 32) in ferret primary visual cortical slices. The injected stochastic currents are the same as those used in model simulations and possessed a prescribed long temporal correlations. Figure 5 shows an example with the 1/f\(^2\) type input (the Ornstein-Uhlenbeck process with a correlation time \( \tau_{corr} = 2000 \) ms). The baseline of the current was adjusted so that the neuron had an average firing rate \( \sim 10 \) Hz throughout each 60-s period of injected current. Although the recorded output exhibits some similarity with the input pattern, it is more transient in time (Fig. 5A). Temporal correlation analysis revealed that correlations in the output spike trains were significantly reduced with respect to the input and decayed to zero for times >2 s (Fig. 5B). The power spectrum shows a reduced relative power at low frequencies and is significantly flattened between 0.1 and 1 Hz (Fig. 5C).

Similar decorrelation effects were observed with the 1/f-type stochastic current injection (Fig. 6). The baseline of the current was adjusted through the injection of constant current so that each neuron had a firing rate of \( \sim 10 \) Hz throughout each 120-s recording session. The 1/f-type input exhibits slow variations over time scales of seconds (Fig. 6A, top). This slow modulation is virtually absent in the neural firing output (Fig. 6A, bottom). The output’s autocorrelation is dramatically suppressed and is near zero for time scales >1 s (Fig. 6B). The power spectrum is flattened (whitened) for frequencies <1 Hz (Fig. 6C).

The behavior of the recorded cortical neuron is strikingly similar to that of the model endowed with \( I_{KCa} \) and \( I_{KNa} \) (compare Fig. 6 with Fig. 3). We also compared the histograms of the instantaneous firing rates (calculated as the inverse of the ISIs) for the model and a cortical neuron (Fig. 7). The input amplitude has a Gaussian distribution (Fig. 7A). The firing rate histogram for the model neuron without any adaptation current is almost Gaussian-shaped, like the input, except for an additional small peak near zero (corresponding to time periods of relative quiescence; Fig. 7B). Adaptation by \( I_{KCa} \) increases the probability for low firing rates (peak near 0) and decreases the

FIG. 5. In vitro intracellular recording from a visual cortical neuron (1/f\(^2\) type input). A: top, injected current with 1/f\(^2\) type power spectrum; middle, recording of membrane potential; bottom, instantaneous firing rate. B: autocorrelation function for the input and the output. The output is significantly decorrelated at long time scales. C: power for the output is reduced in the low frequency range.
Gaussian-shaped peak at high rates (Fig. 7C). The addition of $I_{\text{KNa}}$ further altered the firing rate histogram. The peak at high rates virtually disappears, and the peak near zero becomes dominant (Fig. 7D). In other words, although most of the time the model neuron fires at low rates, it can occasionally fire transiently at high rates ($\leq 100$ Hz). The same characteristic firing rate histogram was found for a real cortical neuron (Fig. 7E). The agreement between data and the model provide supporting evidence that intrinsic membrane dynamics of a single neuron in the visual cortex can decorrelate natural-scene-like inputs with long-range temporal correlations.

**Relationship between slow hyperpolarization and decorrelation**

Because decorrelation is observed with current injection in our slice experiments, it is a single-cell phenomenon. What are the specific membrane mechanisms underlying this decorrelation effect? Evidence indicates that a $[\text{Na}^{+}]_o$-activated $K^+$ current $I_{\text{NaK}}$ plays a large role in the slow hyperpolarization that contributes to adaptation of visual cortical neurons to prolonged inputs (Sanchez-Vives et al. 2000a,b). We attempted to establish a link between the decorrelation effect and slow hyperpolarization, based on the previous observation that the slow hyperpolarization (presumably produced by $I_{\text{NaK}}$) is enhanced in zero calcium solution, compared to control with $[\text{Ca}^{2+}]_o/2$ mM (Sanchez-Vives et al. 2000b). The reason for this enhancement is that under control condition there is a calcium-activated inward current that counteracts $I_{\text{NaK}}$. The removal of calcium eliminates this inward current and unveils a larger slow hyperpolarization (Sanchez-Vives et al. 2000b). Our reasoning is that, if the same adaptation mechanism serves the decorrelation process, then a stronger decorrelation effect should be observed in zero calcium. We tested this prediction in $n = 5$ cells, with both current pulses and 1/f-type stochastic currents. In some cells, we used more than one sample stimuli per cell to increase the number of trials. Neurons show pronounced afterhyperpolarizations (sAHP) following a long (20 s) current injection that is either a single pulse or a train of periodic pulses (at 2 Hz, period of 500 ms, 250 ms on and 250 ms off; Fig. 8). The sAHP is longer lasting in zero $[\text{Ca}^{2+}]_o$ than in control (Fig. 8), consistent with the previous results (Sanchez-Vives et al. 2000b). To quantify the size of sAHP in zero $[\text{Ca}^{2+}]_o$ and in control, we calculated the time integral of sAHP divided by the total number of spikes during...
As shown in Fig. 9A, the sAHP integral per spike is larger in 0 [Ca$^{2+}$]$_o$ compared to control for all five cells.

When 1/f-type correlated stochastic inputs are applied, the autocorrelation of the spiking output is further reduced (decorrelation is more effective) in 0 [Ca$^{2+}$]$_o$ compared to control. The reduction is very dramatic in some cells (Fig. 8, B and C) and modest in others (Fig. 8, A and D). To quantify the decorrelation effect, we calculated the integral of the autocorrelation functions of the input and the output ($A_{in}$ and $A_{out}$), and used $\rho_{decorr} = A_{out}/A_{in}$ as a decorrelation index. The smaller is $\rho_{decorr}$, the stronger is the decorrelation effect. In each of the five cells, $\rho_{decorr}$ is substantially smaller in 0 [Ca$^{2+}$]$_o$ than in control, when the comparison was made with the same 1/f-type sample input under the two conditions (Fig. 9C). It is important to note that the average firing rate of the neural response to 1/f-type input either remains the same or is higher in 0 [Ca$^{2+}$]$_o$ than in control (Fig. 9B). Therefore the stronger decorrelation

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**FIG. 8.** Increase of slow hyperpolarization and enhancement of decorrelation in 0 [Ca$^{2+}$]$_o$. A–D: 4 different cells are shown. Top: autocorrelation function of input (red), output in control medium (blue), and in 0 [Ca$^{2+}$]$_o$ (green). The autocorrelation is smaller in 0 [Ca$^{2+}$]$_o$ than in control. Bottom: neural response to a long (20 s) current pulse (A and B) or to a period train of current pulses (C and D). Note the slow afterhyperpolarization after the input pulse. Slow hyperpolarization is substantially longer-lasting in 0 [Ca$^{2+}$]$_o$ (green) than in control (blue).
degree of decorrelation is enhanced at the same time as the size and duration of slow afterhyperpolarization, consistent with the notion that the same ionic channels (e.g., $I_{KNa}$) underly slow hyperpolarizations that subserve the decorrelation dynamics of single neurons in the primary visual cortex.

**Biophysical mechanisms of slow (seconds) neuronal adaptation**

In the primary visual cortex, it has been proposed that contrast adaptation operating at time scales of seconds can arise from short-term depression of afferent synapses (Adorján et al. 1999; Chance et al. 1998). Modeling studies also suggest that short-term synaptic depression provides a candidate mechanism for decorrelation of correlated input spike trains (Goldman et al. 1999, 2002; Matveev and Wang 2000). This proposal is consistent with some in vitro slice experiments (Abbott et al. 1997; Finlayson and Cynader 1995; Tsodyks and Markram 1997; Varela et al. 1997). In an in vivo study of the somatosensory cortex, a rapid depression of thalamocortical synapses (time constant of 0.25–0.32 s) was found to underlie adaptation to whisker stimulation (Chung et al. 2002). However, evidence for slow (time constant of seconds) synaptic depression in the intact brain is still lacking. Recently Sanchez-Vives et al. (2000a,b) discovered that slow adaptation during prolonged visual stimuli depends on the intrinsic activation of ionic conductances, such as $I_{KNa}$. These and other (Carandini and Fester 1997) studies did not find a consistent decrease in visually evoked synaptic barrages following adaptation; a finding that is inconsistent with a strong role for synaptic depression in adaptation. In support of this view, we show here that a cortical pyramidal cell model endowed only with $I_{KNa}$ and $I_{KCa}$ can reproduce adaptation to high-amplitude sinusoidal input mimicking a high-contrast visual stimulus (Fig. 1).

Further experiments are needed to quantitatively test our model and the role of $I_{KNa}$ in adaptation. One possibility is to use synthetic Na$^+$ buffers, which should prevent [Na$^+$], accumulation and hence block $I_{KNa}$ activation (K. Svoboda, personal communication). Another critical issue is to determine the [Na$^+$], dynamics in V1 pyramidal cells: what is the [Na$^+$], influx per spike? To what level can [Na$^+$], accumulate during a long-lasting stimulation? How fast is the Na$^+$/K$^+$ exchange? In the model, assuming that the baseline [Na$^+$], is 8 mM (Galvan et al. 1984; Grafe et al. 1982), and that [Na$^+$], is increased by 100 μM per spike, the [Na$^+$], level typically reaches 15–20 mM after long-lasting (many tens of seconds) neural discharges at an average rate of 20 Hz. In a recent experiment, Rose et al. (1999) used Na$^+$ indicator dye SBF1 and two-photon imaging to measure intracellular Na$^+$ concentration evoked by action potentials in dendrites and spines of hippocampal CA1 pyramidal cells. They found that the [Na$^+$], signal can integrate the spike activity, because it has slow kinetics (time constant of several seconds). The spike-triggered [Na$^+$], transients reached values of 1, 2, and 4 mM for a train of 5, 10, and 20 spikes, respectively. Therefore the [Na$^+$], transient is ~200 μM per action potential in the fine dendrites and spines. Because this rate of accumulation is twice the value used in our model, we expect that in pyramidal cell’s dendrites, the [Na$^+$], can reach 15–20 mM after tens of seconds of neural discharges at an average rate of 10 Hz. It would be interesting to test directly our prediction by Na$^+$ imaging of visual cortical

**FIG. 9.** Increased slow hyperpolarization and enhanced decorrelation in 0 [Ca$^{2+}$]o. A: time integral of afterhyperpolarization per spike is larger in 0 [Ca$^{2+}$]o compared to control ($n$ = 5, 7 input trials). B and C: in response to the same sample stochastic 1/f-type input, the decorrelation effect is stronger, whereas the overall firing rate is about the same or higher, in 0 [Ca$^{2+}$]o, than in control ($n$ = 5, 8 input trials).


discussion

Adaptation and gain control of neurons are well-known phenomena and are the subject of many physiological studies over the years. The main novelty of the present work is to demonstrate, using combined computational and electrophysiological methods, that intrinsic spike-frequency adaptation mechanisms can temporally decorrelate inputs at the single neuron level. Based on experimental evidence from V1 pyramidal cells (Sanchez-Vives et al. 2000a,b), we focused on the role in neuronal adaptation of a Na$^+$-activated K$^+$ current $I_{KNa}$. Our main results are: $I_{KNa}$ can dramatically suppress temporal correlations (at time scales >1 s) in the neural firing output when the input is strongly correlated (1/f or 1/f type) such as in natural-scene stimuli; visual cortical neurons in vivo slices decorrelate the inputs in the same way as the model; the

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neurons during prolonged discharges as in the contrast adaptation experiments.

Moreover, it would be important to know the precise spatial site of \([Na^+]\), accumulation with respect to the location of \(I_{KNa}\). For example, an increase in intracellular \([Na^+]\), may be tightly localized in the submembrane space and reach levels high enough to activate \(I_{KNa}\) (Koh et al. 1994). Moreover, due to the difference in the surface/volume ratio, activity-induced \([Na^+]\), accumulation could vary widely at different somatic and dendritic compartments of a single neuron (Qian and Sejnowski 1989). Therefore the spatial distribution of \(I_{KNa}\) across the somatodendritic membrane is important to be determined experimentally. It is conceivable that hyperpolarizations of different portions of a neuron’s dendritic tree may result from localized entry of \(Ca^{2+}\) and \(Na^+\) and activation of nearby \(I_{KCa}\) and \(I_{KNa}\) channels. This may serve to temporally decorrelate inputs to restricted dendritic segments, while leaving others segments less affected.

Finally, it would also be interesting to explore additional or alternative ionic mechanisms for neuronal adaptation in the cortex and other brain structures. In retinal ganglion neurons, slow adaptation (Baccus and Meister 2002; Chander and Chichilinsky 2001; Shapley 1997; Shapley and Victor 1978; Simirnakis et al. 1997) may be related to properties of \(Na^+\) channels in these cells (Kim and Rieke 2001, 2003), or reflect cellular mechanisms upstream in bipolar neurons (Brown and Masland 2001; Rieke 2001). It would be interesting to see if the same is true for other structures.

**Decorrelation at the single-cell level**

In our model, when driven by stochastic inputs with long-range temporal correlations, \(I_{KCa}\) and \(I_{KNa}\) remove correlations in the spiking output at different time scales (10–100 ms and 1–10 s, respectively). In the output power spectrum, at <1 Hz the power is reduced to a plateau level (is whitened) by \(I_{KNa}\), while \(I_{KCa}\) results in a flattening of the power-frequency function at frequencies between 1 and 10 Hz. We noticed that when the output firing rate is very low, decorrelation could be a trivial consequence of the fact that most of the time the cell membrane is subthreshold, the consecutive spikes are separated by long times compared to the input correlation time, so that most of the correlation information in the input is lost. This happens when the output firing rate is roughly lower than the inverse of the input correlation time (<1–2 Hz with an input correlation time of 2 s). For this reason, both for model simulations and experimental studies, we always made sure to depolarize the cell with a baseline current when injected with correlated current, so that the cells fire spikes throughout the stimulation with a relatively high mean firing rate (10–20 Hz generally).

Interestingly, we found that visual cortical neurons in vitro show similar decorrelation properties as the model (compare Figs. 5 and 6 for data with Figs. 2 and 3 for the model). The distribution of instantaneous firing rates is also similar for the visual cortical cell and the model (Fig. 7): it is roughly exponential at low rates, but there is a second broad peak at larger firing rates (~50–80 Hz). We attempted to further establish the link between the slow hyperpolarization and the decorrelation effect by comparing the neuronal behavior in zero-calcium bath solution with that in control. We confirmed the previous observation (Sanchez-Vives et al. 2000b) that for a given cell, the slow hyperpolarization after spiking activity is stronger and longer lasting in zero calcium than in control. Furthermore in response to the exactly same sample of stochastic correlated input, the decorrelation effect was stronger in zero calcium than in control (Figs. 8 and 9). This result lends support to the idea that the same ion channel mechanism responsible for the slow hyperpolarization also underlies the decorrelation process of temporally correlated stochastic inputs. However, our results only show that the two effects increase in a correlated way, and we do not have direct proof for the hypothesized role of \(I_{KNa}\) in the observed decorrelation phenomenon at the single-cell level.

It is worth noting that an adaptation mechanism removes correlations most effectively at time scales comparable to its intrinsic time constant. Therefore with \(I_{KNa}\) and \(I_{KCa}\) a neuron’s output can still show large autocorrelations at time scales shorter than a few hundreds of milliseconds. The adaptation mechanism of redundancy reduction is thus compatible with the fact that cortical neuronal spike trains do show autocorrelations at time scales ranging from one to hundreds of milliseconds (for a review, see Singer and Gray 1995).

We have not addressed the question of whether the filter functions of cortical neurons are optimally designed. That is, the kinetics and strength of adaptation ionic mechanisms might have been optimized, through biological evolution, for redundancy reduction of the kind of natural stimuli that the animal encounters in daily life (Atick 1992). Specifically, one could ask whether the calcium- and sodium-activated potassium currents correlate 1/f and 1/f² stimuli better than inputs with other statistical properties. However, what it means to be “optimal” remains to be clarified. Indeed, most likely, complete whitening of stimulus by decorrelation is not desirable because probability distributions of stimuli may themselves be used for neural representation of the sensory world in the brain (Barlow 2001; Rao et al. 2002).

**Adaptation and decorrelation in the VI network**

Computational theories suggest that in the mammalian visual system, natural inputs are decorrelated spatially at the level of the retina (Atick 1992) and temporally in the lateral geniculate nucleus (LGN) (Dong and Atick 1995b) so that signals that arrive in the visual cortex are encoded in an efficient form. In support of this proposal, physiological studies show that in response to natural time-varying images (movies), neurons in the cat LGN remove temporal correlations at the time scales of 50–300 ms, and the output power spectrum is whitened in the frequency range of 3–15 Hz (Dan et al. 1996).

The underlying biophysical mechanism could be, at least partly, intrinsic membrane properties of the LGN relay cells. Indeed these cells are known to display burst discharges due to a T-type calcium ion current; this burst activity can remove temporal correlations in an input at the time scale of ~100 ms (Kepecs et al. 2002). However, LGN cells fire bursts only under certain conditions (including sodium pentothal anesthesia as in the experiment of Dan et al. 1996); their propensity of burst discharge during waking states remains a matter of debate (Sherman 2001). Therefore it is still unclear whether temporal
decoration primarily takes place in the LGN during animal’s natural behaviors.

Here we hypothesize that temporal decorrelation of inputs is to a large extent accomplished in the primary visual cortex by the same mechanisms responsible for the contrast adaptation. Synaptic depression can temporally decorrelate inputs in a synapse-specific manner and at the time scale of hundreds of milliseconds (on a similar time scale as fast intrinsic adaptation through \( I_{\text{KCa}} \)); whereas intrinsic membrane dynamics mediated by \( I_{\text{KNa}} \) operate at a much slower time scale, for example at the level of the neural activity and at a slower time scale of seconds. To explore this proposal computationally, it will be necessary to extend our investigation to pattern adaptation in a V1 network model, that takes into account short-term synaptic depression (Adorján et al. 1999; Somers et al. 1998) and slow spike-frequency adaptation by \( I_{\text{KNa}} \) in single neurons. Network modeling would enable us to investigate the mechanisms for pattern adaptation and whether the same mechanisms can remove spatiotemporal correlations in the natural-scene inputs thereby performing redundancy reduction in both space and time. Experimentally, our proposal could be tested by physiological studies of V1 neurons in response to natural time-varying stimulations (such as movies). Further experimental and theoretical studies will lead to the elucidation of specific cellular mechanisms of adaptation and redundancy reduction processes in the visual cortex.

**APPENDIX: QUALITATIVE EXPLANATION OF POWER SPECTRUM WHITENING BY AN ADAPTATION CURRENT**

To understand whitening or flattening of the neural output power spectrum within a frequency range, let us consider a linear model of adaptation, \( I_{\text{adapt}} = G_{\text{adapt}} X \) where \( X = [\text{Ca}^{2+}], [\text{Na}^{+}] \) or \( I_{\text{adapt}} = I_{\text{KCa}} \) or \( I_{\text{KNa}} \) respectively. Furthermore, assume that \( X \) obeys a linear kinetic equation

\[
\frac{dX}{dt} = k \sum \delta(t - t_i) - \frac{X}{\tau_X} = \alpha_r(t) - \lambda(t) \tau_X \tag{A1}
\]

where the spike train \( \sum \delta(t - t_i) \) is replaced by the instantaneous firing rate, which is a valid approximation as long as \( \tau_X \) is sufficiently longer than a typical ISI. The parameter \( \alpha_r \) is the X influx per spike, and \( \tau_X \) is the time constant (~100 ms for \([\text{Ca}^{2+}]_o \), and ~10 s for \([\text{Na}^{+}]_o \)). Note that although the \( X \) extrusion process is highly nonlinear, the present discussion assuming a linear kinetics is nevertheless instructive.

Suppose that in response to a time-varying stochastic input current \( I \), the neuron’s output firing rate is given by \( r(t) = \beta I_{\text{tot}}, \) where \( I_{\text{tot}} = I - I_{\text{adapt}} \) and the firing threshold \( I_{\text{th}} \) is absorbed in \( I \). Therefore, \( r(t) = \beta \{I(t) - I_{\text{adapt}}(t)\} \). Inserting this expression into Eq. A1 we have

\[
\frac{dX}{dt} = \alpha \beta r(t) - (\alpha \beta G_{\text{adapt}} + 1/\tau_X)X = \alpha \beta r(t) - X/\tau_X \tag{A2}
\]

where we define the adaptation time constant \( \tau_{\text{adapt}} \) as

\[ 1/\tau_{\text{adapt}} = \alpha \beta G_{\text{adapt}} + 1/\tau_X \tag{A3} \]

Due to the additional term \( \alpha \beta G_{\text{adapt}} \), \( \tau_{\text{adapt}} \) is typically much shorter than \( \tau_X \) (see also Liu and Wang 2001; Wang 1998).

The solution of Eq. A2 yields

\[
X(t) = \int_0^t \alpha \beta r(t') e^{-\frac{t-t'}{\tau_{\text{adapt}}}} dt' = \alpha \beta I \ast K(t) \tag{A4}
\]

where the kernel of the convolution is

\[
K(t) = \begin{cases} 
  e^{-\frac{t}{\tau_{\text{adapt}}}} & \text{if } t \geq 0 \\
  0 & \text{otherwise} 
\end{cases} \tag{A5}
\]

The Fourier transforms of the kernel \( K \), and \( r \) are as follows

\[
F(K) = -\frac{1}{is \omega - \frac{1}{\tau_{\text{adapt}}}} \tag{A6}
\]

\[
F(r) = \beta F(I) = \beta \mathcal{F}[1 - G_{\text{adapt}}F(X)] \tag{A7}
\]

\[
F(r) = \beta F(I) - G_{\text{adapt}}F(X) = \beta F[I(1 - G_{\text{adapt}}\alpha BF(K))] \tag{A8}
\]

Therefore the output power spectrum \( S_o = |F(r)|^2 \) can be expressed as a function of the input power \( S_i = |F(I)|^2 \)

\[
S_o(\omega) = S_i(\omega) \frac{\omega^2 + (1/\tau_X)^2}{\omega^2 + (1/\tau_{\text{adapt}})^2} \tag{A9}
\]

Without adaptation, it is easy to show that

\[
S_o(\omega) = \beta^2 S_i(\omega) \tag{A10}
\]

Thus the presence of \( I_X \) introduces a temporal kernel that convolves with the input to produce the output. This leads to an additional multiplicative factor for the output power spectrum

\[
\omega^2 + (1/\tau_X)^2 \omega^2 + (1/\tau_{\text{adapt}})^2 \tag{A11}
\]

where \( \tau_{\text{adapt}} \) is typically much smaller than \( \tau_X \). At low frequencies \( \omega \ll 1/\tau_X \), the additional factor is \( (\tau_{\text{adapt}}/\tau_X)^2 \ll 1 \). (Note that at very low frequencies, this analysis is no longer valid because the assumption that the firing is faster than the X dynamics is no longer correct.) In the frequency range \( 1/\tau_X \ll \omega \ll 1/\tau_{\text{adapt}} \), this factor is \( \sim \omega^2 \). At very high frequencies, this factor is 1, reflecting the fact that the slow adaptation current has no effect as expected. Thus spike-frequency adaptation provides a high-pass filter in the intermediate frequency range \( 1/\tau_X \ll \omega \ll 1/\tau_{\text{adapt}} \). If \( I(t) \) is a temporally correlated input with a power spectrum \( S_i(\omega) \sim \omega^{-2} \), the output spike train is decorrelated; the power spectrum is \( S_o(\omega) \sim S_i(\omega) \omega^2 \). Thus \( S_o \) would be almost flat (whitened) and behave like white noise for \( 1/\tau_X \ll \omega \ll 1/\tau_{\text{adapt}} \).

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