Phase Locking of Auditory-Nerve Fibers to the Envelopes of High-Frequency Sounds: Implications for Sound Localization

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Dreyer, Anna and Bertrand Delgutte. Phase locking of auditory-nerve fibers to the envelopes of high-frequency sounds: implications for sound localization. J Neurophysiol 96: 2327–2341, 2006; doi:10.1152/jn.00326.2006. Although listeners are sensitive to interaural time differences (ITDs) in the envelope of high-frequency sounds, both ITD discrimination performance and the extent of lateralization are poorer for high-frequency sinusoidally amplitude-modulated (SAM) tones than for low-frequency pure tones. Psycho-physical studies have shown that ITD discrimination at high frequencies can be improved by using novel transposed-tone stimuli, formed by modulating a high-frequency carrier by a half-wave-rectified sinusoid. Transposed tones are designed to produce the same temporal discharge patterns in high-characteristic frequency (CF) neurons as occur in low-CF neurons for pure-tone stimuli. To directly test this hypothesis, we compared responses of auditory-nerve fibers in anesthetized cats to pure tones, SAM tones, and transposed tones. Phase locking was characterized using both the synchronization index and autocorrelograms. With both measures, phase locking was better for transposed tones than for SAM tones, consistent with the rationale for using transposed-tone stimuli. With both measures, phase locking was better for transposed tones and pure tones in both psychophysical studies and neurophysiological studies of central neurons.

INTRODUCTION

Interaural time differences (ITDs) serve two important functions in binaural hearing: localization of sound sources and detection of sounds in noisy environments. Although ITDs are the dominant cue for localizing sources containing low-frequency energy (MacPherson and Middlebrooks 2002; Wightman and Kistler 1992), the use of ITDs in localization tasks is not restricted to low frequencies. Although interaural time differences in the fine structure of high-frequency sounds cannot be detected, the auditory system can exploit the ITDs present in the envelope of high-frequency stimuli to lateralize sounds (Henning 1974; Leakey et al. 1958; McFadden and Pasanen 1976). However, the perceptual ability to use ITDs in high-frequency envelope cues seems weaker than that for low-frequency fine-structure cues. For instance, the extent of lateralization is narrower and ITD discrimination thresholds are poorer for sinusoidally amplitude-modulated (SAM) tones than for low-frequency pure tones of the same frequency as the modulator (Bernstein and Trahiotis 1985, 1994).

Colburn and Esquissaud (1976) indicated that the relatively poor ITD resolution for high-frequency stimuli could be a result of either differences in the temporal properties of the spike trains in the auditory nerves or differences in how the CNS processes low- and high-frequency inputs, or a combination of the two. Van de Par and Kohlrausch (1997) hypothesized that differences in lateralization sensitivity between SAM and pure tones may be attributed to the difference in “the internal representation after transformation in the inner hair cells” for the two stimuli. To a first-order approximation, this transformation can be described as half-wave rectification followed by low-pass filtering. The low-pass filtering is attributed to both the inner hair cell (IHC) membrane time constant (Palmer and Russell 1986) and jitter in transmission at the synapses between the hair cell and primary neurons (Anderson et al. 1971). Half-wave rectification arises in part from the IHC receptor potential versus cilia displacement characteristic.

According to this simplified model for IHCs, a low-frequency pure tone is transformed into a half-wave-rectified sine wave (Fig. 1, top), whereas a high-frequency SAM tone is transformed into a sinusoid if the carrier frequency (f<sub>c</sub>) is above the cutoff frequency of the low-pass filter (Fig. 1, middle). Therefore van de Par and Kohlrausch (1997) suggested a novel stimulus, called a “transposed” tone, designed to produce the same temporal discharge patterns in high-frequency auditory-nerve fibers (ANFs) as a pure tone does in low-frequency fibers. A sinusoidal carrier is multiplied by a half-wave-rectified low-frequency sinusoid, producing a high-frequency transposed tone with the envelope of the low-frequency half-wave-rectified sine wave (Fig. 1, bottom left). After low-pass filtering, the response to a transposed tone is expected to be a half-wave-rectified sinusoid resembling the response to a pure tone.

For modulation frequencies <150 Hz, high-frequency transposed tones produce extents of laterality and ITD sensitivity better than those produced by SAM tones and comparable to those produced by pure tones (Bernstein 2001; Bernstein and Trahiotis 2002). These findings suggest that, for low modulation rates, the poorer sensitivity to ITDs at high frequencies compared with low frequencies results at least in part from...
differences in the temporal discharge patterns produced in the auditory nerve by the two stimuli. However, as modulation frequency increases, lateralization performance in response to transposed tones degrades relative to performance for a comparable pure tone, suggesting that additional factors beyond peripheral representation may also play a role.

The only available neurophysiological study of responses to transposed tones (Griffin et al. 2005) focused on ITD-sensitive neurons in the inferior colliculus (IC), the principal auditory nucleus in the midbrain, using relatively low stimulus levels. Griffin et al. found that ITD sensitivity of IC neurons for transposed tones with low modulation frequencies was comparable to that for pure tones at low and moderate stimulus levels. IC neurons are thought to derive their ITD sensitivity by synaptic inputs from neurons in the lateral and medial superior olives (LSO and MSO), whose function depends critically on phase-locked inputs from the two ears. A quantitative description of phase locking to transposed tones at the earliest stages of processing in the auditory pathway is therefore essential for understanding the central neurophysiological results (Griffin et al. 2005) as well as the psychophysical results (Bernstein 2001; Bernstein and Trahiotis 2002). In this paper, we quantitatively compare the phase locking of ANFs to transposed tones, SAM tones, and pure-tones.

Although the idealized picture of peripheral auditory processing shown in Fig. 1 is a useful first approximation, several arguments suggest that the temporal discharge patterns of ANFs to transposed tones may differ from pure-tone response patterns in significant ways. First, the relationship between IHC receptor potential and cilia displacement cannot be characterized as simple half-wave rectification because a fraction of the transduction channels are open when the cilia displacement is zero, resulting in sustained current flow into the hair cell and spontaneous release of neurotransmitter at the base of the hair cell. As a result, the instantaneous rate of discharge of ANFs in response to low-frequency pure tones falls below the spontaneous rate (SR) during approximately every other half cycle (Johnson 1980), contrary to the idealized model used for motivating transposed tones. Second, phase locking to SAM tones degrades at a higher sound pressure level (SPL) arising from cochlear compressive nonlinearities (Joris and Yin 1992; Smith and Brachman 1980). Given the amplitude-modulated nature of transposed tones, a similar level dependency of phase locking may be expected. Therefore this paper places particular emphasis on the level dependency of phase locking to transposed tones compared with pure tones. We find that, whereas phase locking to transposed tones with low modulation frequencies (<250 Hz) is similar to that to pure tones at sound levels near neural thresholds, this is not the case for higher levels and higher modulation frequencies. Preliminary reports of these findings were previously presented (Dreyer and Delgutte 2004; Dreyer et al. 2005).

**METHODS**

**Procedure**

Healthy adult cats were anesthetized with Dial in urethane (75 mg per kg of body weight) and maintained in an anesthetized state as judged by the toe-pinch reflex (Kiang et al. 1965). The auditory nerve was exposed by opening the posterior fossa and retracting the cerebellum. The tympanic bullae were opened and the round window was exposed. The cat was administered 4.5 ml per kg of lacted Ringer solution, with an additional 4.5 ml booster per day to prevent dehydration, and dexamethasone (0.26 mg/kg) as a prophylactic against brain edema throughout the experiment. Body temperature was maintained at 37°C with a heating blanket.

Single-unit recordings were conducted with the animal placed on a vibration-attenuating table in an electrically shielded, soundproof chamber. A metal electrode near the round window recorded the compound action potential (CAP) in response to click stimuli to assess the sensitivity and stability of the cat’s cochlear response.

Stimuli were generated with a 16-bit A/D converter (NIDAC 6052e, National Instruments) using a sampling rate of 50 kHz. An electrodynamic speaker (Realistic 40–1377) delivered sound stimuli near the cat’s tympanic membrane through a closed acoustic assembly. Stimuli were digitally compensated for the frequency response of the acoustic system by measuring the magnitude and phase of the sound pressure at the tympanic membrane as a function of frequency and designing digital inverse filters.

Single-unit activity was recorded with glass micropipettes filled with 2 M KCl. The electrode was inserted into the auditory nerve with the aid of a microscope and then advanced with a micropositioner (Kopf 650). The microelectrode signal was band-pass filtered and sent to a custom spike detector and timer that records spike arrival times with a precision of 1 μs.

A click stimulus at about 55 dB SPL was used as search stimulus while advancing the electrode into the nerve. On locating a responsive fiber, a threshold tuning curve was measured with an automatic tracking procedure (Kiang and Moxon 1974) using 50-ms tone bursts, and the characteristic frequency (CF) and threshold at the CF were noted. The fiber’s spontaneous discharge rate (SR) was measured over 20 s.

All procedures were approved by the MIT and MEEI Institutional Animal Care and Use Committees (IACUC).

**Stimuli**

Low-frequency pure tones and high-frequency SAM and transposed tones were synthesized digitally. Transposed tones were generated as described by van de Par and Kohlrausch (1997) and Bernstein and Trahiotis (2002). All SAM tones were 100% modulated and all transposed tones had half-wave-rectified sinusoidal envelopes. Pure-tone frequencies (f) and the modulation frequencies (f_m) of both SAM and transposed tones were 60, 125, 250, 500, or 1,000 Hz. The frequencies of these pure tones were always within a half-octave of the fiber CF. The carrier frequency (f_c) of SAM and transposed tones was usually set at the CF. In some fibers, f_c was also set slightly below or above CF, such that the threshold at f_c would be about 20 dB above the threshold at CF. These off-CF responses are important...
because they may convey much of the temporal information at higher sound levels when on-CF responses are saturated. On the average, \( f_e \) was 0.16 ± 0.05 (±SD) octave above the CF and 0.25 ± 0.12 octave below the CF for these off-CF conditions.

Because only limited amounts of pure-tone data were collected, pure-tone responses previously collected by Tsai and Delgutte (1997) were also used and account for most of the pure-tone responses (250/283). In their experiments, the pure-tone frequency was chosen from a fixed grid of frequencies separated by half-octave steps and was typically within a quarter-octave of the CF, so that it always fell within the tip portion of the tuning curve. We include the Tsai and Delgutte data for frequencies <1 kHz for the majority of our analyses and include their data only for frequencies between 1 and 3 kHz for the analyses shown in Figs. 4 and 11.

Responses to pure tones were collected primarily from low-CF fibers, whereas responses to transposed and SAM tones were recorded from high-CF fibers (>3 kHz) to minimize phase locking to the fine structure. In our experiments, responses were measured as a function of stimulus level from rate threshold to 60 dB above threshold in 10-dB steps using 20 repetitions per level. Sound pressure levels did not exceed 85 dB SPL to avoid injuring the cochlea. For all stimuli, stimulus level was defined based on the root-mean-square amplitude of the acoustic pressure waveform. To facilitate comparisons, the high-frequency stimuli were presented in matched pairs consisting of a 480-ms SAM tone, followed by 520 ms of silence, a 480-ms transposed tone with the same modulation frequency, and another 520 ms of silence. Each presentation of a pure-tone stimulus consisted of a 480-ms tone followed by 520 ms of silence. All stimulus durations include 20-ms rise and fall times using raised-cosine ramps to prevent abrupt transients. In the experiments of Tsai and Delgutte (1997), the pure-tone stimuli were 100 ms in duration, including 2.5-ms (raised-cosine envelope) rise and fall times, and were presented at a rate of 2/s. Responses were measured over an 80-dB range of levels in 2-dB steps, with four repetitions at each SPL. Spikes were then grouped into coarser 10-dB-level bins to increase the number of spikes per level and facilitate comparisons with the data collected in our own experiments.

**Analysis**

Period histograms, locked either to the modulation frequency for SAM and transposed tones or to waveform frequency for pure tones, were computed from spike times, discarding the first 16 ms after stimulus onset. The strength of phase locking was characterized by the synchronization index (SI), the ratio of the fundamental frequency component of the period histogram to the average firing rate. Also known as vector strength (Goldberg and Brown 1969), the SI varies from 0 for a flat histogram with no phase locking to 1 for an impulsive histogram indicating perfect phase locking. Statistical significance of the synchronization index was assessed by the Rayleigh statistic (Mardia and Jupp 2000), using a criterion of \( P < 0.001 \), and values of SI failing this criterion were discarded.

To obtain an alternate description of temporal discharge patterns more relevant to binaural hearing, phase locking was also characterized using shuffled autocorrelograms (SACs) (Louage et al. 2004). Temporal analysis using SACs compares the timing of spikes between different presentations of the same stimulus. Whereas the synchronization index must be calculated at a predetermined frequency, computation of SACs does not require knowledge of the stimulus. In addition, because the SAC is a cross-correlation between pairs of spike trains, it is particularly relevant to ITD coding because many models of binaural processing are based on interaural correlation (Colburn 1977; Trahiotis and Stern 1995).

Each SAC was computed from the \( N \) (usually 20) stimulus presentations at each stimulus level. Spike trains from each stimulus presentation were paired, or shuffled, with the \( N - 1 \) others to create \( N(N - 1)/2 \) distinct pairs of spike trains. For each pair, the forward and backward time intervals between all spikes from the first spike train and the spikes from the second spike train were calculated. All intervals were tallied into a histogram using a 50-μs bin width as suggested by Louage et al. (2004). The histograms were then normalized by the square of the average firing rate \( r_0 \), the bin width \( b \), the recording duration (minus discarded times) \( D \), and number of stimulus presentations \( N \) by dividing by \( N(N - 1)r_0bD \). The ordinate of the normalized SAC measures the extent to which a temporal structure related to the stimulus exists in the spike trains, with unity indicating randomly distributed spikes (Louage et al. 2004). For periodic stimuli, this temporal structure primarily reflects phase locking to the stimulus.

Two measures of phase locking were derived from normalized SACs (Louage et al. 2004): the maximum peak height and the peak half-width. The peak height measures the extent to which spikes occur at the same intervals on repeated presentations of the same stimulus relative to randomly distributed intervals. The half-width measures the temporal precision, or spread, of the intervals around the peak. Precise phase locking is indicated by a large peak height and/or a small half-width. To compute these two metrics, we first collapsed the SAC extending over a span of \( 2 \) stimulus cycles onto a folded histogram extending over one cycle.1 This procedure is theoretically justified because the SAC for a periodic stimulus should be periodic in the limit of a large amount of data.

The SI and SAC analyses were applied to all responses to SAM tones, transposed tones, and pure tones. These metrics were then used to characterize how phase locking depends on sound pressure level, modulation frequency, and fiber characteristics.

**RESULTS**

The results are based on recordings from 182 auditory nerve fibers in nine cats. Responses to SAM and transposed tones were collected from 39 high-CF fibers in four cats (CF range: 2.9–13.5 kHz, median 5.7 kHz). These data include 119 level series for matched pairs (same \( f_e \) and \( f_m \)) of SAM and transposed tones. Responses to low-frequency (\( f \leq 1,000 \) Hz) pure-tones were recorded from 70 low-CF fibers from these four and five additional cats (CF range: 170–1,600 Hz, median 740 Hz). Overall, the data include 5.1% low-SR, 37.2% medium-SR, and 57.7% high-SR responses. Responses to pure tones >1,000 Hz were also recorded from an additional 73 high-CF fibers (CF range: 1–3.3 kHz). These higher-frequency data are used only in Figs. 4 and 11.

In the following sections, we first compare phase locking to pure tones, SAM tones, and transposed tones presented at the fiber’s CF using the synchronization index (SI) measure. Then, we compare phase locking for on- and off-CF presentations of SAM and transposed tones. Last, we examine alternate, autocorrelation-based metrics to quantify phase locking to each of the three stimuli.

**Phase locking to pure, SAM, and transposed tones at CF**

A set of period histograms measured as a function of stimulus level in response to a pure tone, a transposed tone, and a SAM tone (Fig. 2A) are shown in Fig. 2B. Responses to the pure tone are recorded from a low-CF fiber (385 Hz), whereas

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1 This folding might appear to contradict our statement that computation of the SAC does not require knowledge of the stimulus period. Folding improved the signal-to-noise ratio of the SAC and was particularly useful for low discharge rates or when phase locking was weak, but it is not theoretically necessary to compute the metrics. Measuring the peak height and half-width does not require knowledge of the stimulus period when signal-to-noise ratio is not an issue.
responses to the SAM and transposed tones are from a high-CF fiber (7,000 Hz). The modulation frequency of the transposed and SAM tones (250 Hz) roughly matches the frequency of the pure tone (354 Hz).

At low stimulus levels, responses to both SAM and transposed tones are restricted to approximately half of the stimulus cycle, indicating a high degree of phase locking to the envelope. As the level increases, spike discharges gradually spread to the other half-cycle, indicating a decrease in phase locking, consistent with previous reports for SAM tones (Cooper et al. 1993; Javel 1980; Joris and Yin 1992; Smith and Brachman 1980). However, for each level, responses to the transposed tone are restricted to a smaller part of the stimulus cycle than responses to the SAM tone. Although the firing rates in response to both SAM and transposed tones saturate at 50 dB SPL (Fig. 2C), phase locking reaches a maximum at lower levels, consistent with previous observations.

For the low-frequency pure tone, the fiber’s response occupies virtually the same portion of the stimulus cycle from threshold (20 dB SPL) = 60 dB above threshold (80 dB SPL), well beyond the point where the rate begins to saturate (Fig. 2C). Thus consistent with previous observations (Johnson 1980), this medium-SR fiber phase locks to the pure tone over a wider range of levels than the rate-based dynamic range.

These observations are reflected in the synchrony level functions derived from the period histograms (Fig. 2B). For the transposed and SAM tones, the SI is highest near threshold and falls dramatically with increasing stimulus level. For each stimulus level, SI is larger for the pure tone than for the SAM tone. Synchrony to the pure tone remains fairly stable with level. Near threshold, the synchrony values are similar for the pure tone and the transposed tone.

Figure 3 shows synchrony-level functions for pure, transposed, and SAM tones for the entire data set. Responses to SAM and transposed tones with all modulation frequencies are included, as well as pure-tone responses for all frequencies <1,000 Hz. Sound level is expressed in decibels with respect to rate threshold to facilitate comparison between fibers. For the most part, responses are well separated based on the stimulus type, even though data from different frequencies and modulation frequencies are pooled: low-frequency fibers phase lock with the greatest precision to pure tones, then high-frequency fibers to transposed tones, followed by high-frequency fibers for SAM tones. Near threshold, fibers tend to show similarly high phase locking to transposed tones and pure tones, although synchrony falls more rapidly with level for transposed tones than for pure tones. Synchrony to SAM tones is poorer near threshold and degrades faster with level than for either transposed or pure tones.

With a few exceptions, the sound pressure level of the maximum synchrony occurred between rate threshold and rate saturation for all stimuli, with an average (± SD) of 15.9 ± 10.3, 5.2 ± 8.7, and 2.5 ± 7.1 dB above threshold for pure, transposed, and SAM tones, respectively. Our average for SAM tones is lower than the value of 10 ± 5.0 dB with respect to threshold given by Joris and Yin (1992), although the rather coarse (10-dB) spacing between adjacent stimulus levels in our experiments makes a precise assessment difficult. Further, the difference could be partially accounted for by clarifying how sound pressure level of the SAM tone is defined: root-mean-square of the waveform versus the peak of the waveform envelope, as well as possibility of different definitions of rate threshold. Consistent with previous observations for SAM tones (Joris and Yin 1992), the SI to SAM and transposed tones decreased monotonically above the level of maximum synchrony and sometimes leveled out at higher levels.
To quantify the fall of synchrony with level for each stimulus, a regression line was fit to the decreasing portion of each SI-level function above the maximum. Only responses containing at least three statistically significant ($P < 0.001$) SI values based on the Rayleigh statistic were used in this analysis. The upward sloping portions of the SI level functions were not fit because they typically contained fewer than three data points. The mean downward slopes ($±$SD) were $−0.0036 ± 0.0043 \text{dB}$ for pure tones, $−0.0064 ± 0.0028 \text{dB}$ for transposed tones, and $−0.0103 ± 0.0026 \text{dB}$ for SAM tones. Our slope estimates for SAM tones are similar to those ($−0.012 ± 0.003/\text{dB}$) given by Joris and Yin (1992). The thick lines in Fig. 3 show the mean slopes for the three stimulus types. The slope relating phase locking to level is almost two times shallower for pure tones than for transposed tones. In addition, phase locking to transposed tones is always greater than phase locking to SAM tones for both the average line and the majority of the data. ANOVA revealed a highly significant effect of stimulus type on the slopes [$F(2,202) = 71.5, P < 0.0001$]. Post hoc multiple comparisons with Bonferroni adjustment indicates that slopes for each stimulus are significantly different from slopes for the other two stimuli ($P < 0.05$).

Although SI-level curves for the three stimuli are fairly well separated (Fig. 3), synchrony to SAM and transposed tones is expected to vary with modulation frequency. As modulation frequency increases, the sidebands are increasingly attenuated by the cochlear filter centered at the CF, thereby decreasing the modulation depth of the mechanical input to the hair cells. In addition, there appears to be a temporal limitation in the ability of AN fibers to phase lock to high modulation frequencies (Greenwood and Joris 1996; Joris and Yin 1992). We therefore examined the dependency of phase locking on modulation frequency for each stimulus type (Fig. 4A). Following Johnson (1980), we use the maximum SI ($S_{\text{max}}$) over all stimulus levels as a measure for comparison. For low modulation frequencies ($f_m ≤ 250 \text{ Hz}$) of the transposed tone, $S_{\text{max}}$ is comparable to that for low-frequency pure tones at 250 Hz. However, synchrony to transposed tones begins to degrade for modulation frequencies between 250 and 500 Hz, whereas phase locking to pure tones does not start to degrade until 1,000 Hz. $S_{\text{max}}$ is always lower for SAM tones than for transposed tones, although the rate of decrease at higher modulation frequencies is similar for both stimuli.

Our finding that $S_{\text{max}}$ is greater for pure tones than for transposed tones $> 250 \text{ Hz}$ might be confounded by the fact the tone-burst stimuli used by Tsai and Delgutte (1997) (on which most of our pure-tone data are based) had shorter durations and higher repetition rates than those of our SAM and transposed tones. However, this is unlikely because a two-way ANOVA comparing $S_{\text{max}}$ for short tone bursts (100 ms; Tsai and Delgutte, 1997) and long-duration tones (15–30 s; Johnson 1980) revealed neither a significant main effect of duration [$F(1,442) = 0.19, P = 0.66$] nor a significant interaction between duration and frequency [$F(6,442) = 1.38, P = 0.22$].

Both the maximum synchrony and the slope of the synchrony-level function above the maximum may depend on modulation frequency. SI-level functions for transposed and SAM tones are shown in Fig. 5 separately for each modulation frequency. Data at $f_m = 1,000 \text{ Hz}$ are not shown because few fibers were studied at this modulation frequency. Figure 5 suggests that the shapes of SI-level functions depend on both the stimulus type and the modulation frequency and that the two variables interact. For low modulation frequencies ($≤ 125 \text{ Hz}$), synchrony falls at a faster rate with level for SAM tones than for transposed tones, as was the case for the pooled data in Fig. 3. However, as modulation frequency increases to 250 Hz and, especially, 500 Hz, the synchrony-level functions for the two stimuli become more parallel. Although the slopes at 500 Hz are similar, the two set of curves remain well separated. These results are confirmed in Fig. 4B, which shows the mean slopes of regression lines fit to the SI-level functions as a function of modulation frequency. In both panels, pure-tone responses are binned to the closest frequency shown.

![Figure 4](http://jn.physiology.org/10.1152/jn.00813.2005)

**Figure 4.** A: maximum values of synchronization index ($S_{\text{max}}$) over all levels as a function of frequency or modulation frequency for pure tones (dotted black), transposed tones (solid blue), and SAM tones (dashed red). Error bars represent $±$1 SE. B: mean slopes of SI-level functions (expressed in dB $−1$) as a function of modulation frequency. In both panels, pure-tone responses are binned to the closest frequency shown.

![Figure 5](http://jn.physiology.org/10.1152/jn.00813.2005)

**Figure 5.** SI vs. level functions for 4 modulation frequencies. Each panel shows responses and best-fitting line (bold) to SAM (dashed red) and transposed (solid blue) tones for one modulation frequency. Best-fit lines are computed using same method as in Fig. 3.
function of modulation frequency for all three stimuli. Excluding the limited data at 1,000 Hz, the mean slope for SAM tones tends to increase with \( f_m \), whereas the mean slope for transposed tones decreases with \( f_m \), so that the two curves converge at 500 Hz. A two-way ANOVA of slopes with stimulus type (SAM and transposed tones) and \( f_m \) as factors indicates that their interaction is highly significant \([F(4,128) = 10.87, P < 0.001]\). The mean slopes for transposed tones are always more negative for those with their pure-tone counterparts, except again for \( f_m = 1,000 \text{ Hz} \), where few data points are available.

For both pure and SAM tones, it has been reported that low-SR fibers tend to phase lock with greater precision than medium-SR fibers, which, in turn, phase lock with more precision than high-SR fibers (pure tones: Johnson 1980; SAM tones: Joris and Yin 1992; Joris et al. 1994). Spontaneous activity adds a DC offset to the period histogram by contributing spikes that are not locked to the stimulus and is thus expected to decrease synchrony. To examine whether phase locking to transposed tones also depends on SR, Fig. 6A shows \( S_{\text{I}_{\text{max}}} \) as a function of \( f_m \) separated according to two SR groups (Liberman 1978): high SR (>18/s) and low/medium SR (<18/s). We did not have data from enough low-SR fibers to analyze them separately. For all three stimuli, there is a clear trend for responses from low/medium-SR fibers to have greater \( S_{\text{I}_{\text{max}}} \) than responses from high-SR fibers. This observation is confirmed by two-way ANOVAs, with \( f_m \) and SR group as factors, which reveal highly significant main effects of SR group on \( S_{\text{I}_{\text{max}}} \) for all three stimuli [pure tones: \( F(1,117) = 32.4, P < 0.001 \); transposed tones: \( F(1,58) = 37.9, P < 0.001 \); SAM tones: \( F(1,58) = 31.7, P < 0.001 \)].

Whereas the instantaneous firing rate in response to a low-frequency pure tone falls below the SR during one half of each stimulus cycle (Johnson 1980), this is not expected to be the case for high-frequency modulated sounds such as SAM and transposed tones, neglecting possible effects of adaptation (see DISCUSSION). Responses to transposed tones and pure tones would therefore be expected to become less similar with higher spontaneous activity. To further analyze the interaction between SR and stimulus type, we ran a two-way ANOVA on \( S_{\text{I}_{\text{max}}} \) with SR group and stimulus type (pure or transposed tone) as factors. To minimize the confounding effect of frequency, the analysis included pure-tone data only for frequencies <800 Hz and transposed-tone data for \( f_m \leq 250 \text{ Hz} \). As expected, the analysis showed significant main effects of SR group and stimulus type (both \( P < 0.001 \)). Post hoc multiple comparisons using Bonferroni corrections show that \( S_{\text{I}_{\text{max}}} \) to pure tones is significantly greater than \( S_{\text{I}_{\text{max}}} \) to transposed tones for the high-SR group (\( P < 0.001 \)), but not for the low/medium-SR group (\( P > 0.05 \)). Thus temporal discharge patterns to transposed tones are similar to pure-tone responses only for low/medium-SR fibers, and only at low stimulus levels and low modulation frequencies where the phase locking to transposed tones is maximum.

**Off-CF responses to SAM and transposed tones**

Thus far, we have described phase locking of ANF responses to SAM and transposed tones when the carrier frequency was at the fiber’s CF. However, these stimuli will excite fibers over a range of CFs, particularly at higher stimulus levels where the cochlear excitation patterns become broad. If most of the fibers with CFs near the carrier frequency are saturated, so that phase locking to the envelope becomes weak, temporal information about the modulation frequency may be conveyed primarily by fibers with CFs far from the frequency band where the stimulus has the most energy, i.e., far from the carrier frequency. Therefore it is important to characterize phase locking when \( f_c \) is presented off the CF.

In general, responses to SAM and transposed tones with carrier frequencies both above and below CF broadly resemble on-CF responses. However, some noticeable differences do exist. Figure 7A shows response patterns of a fiber as a function of level to transposed tones with carrier frequencies at the CF (6,920 Hz), below the CF (5,603 Hz), and above the CF (7,490 Hz). For all three carrier frequencies, the period histograms show the same trend in that the fraction of the stimulus cycle occupied by spike discharges increases with stimulus level, implying a degradation in phase locking. Average discharge rates for this low-SR fiber do not saturate completely, even at high levels (Fig. 7C). As expected, phase locking begins to deteriorate at lower levels for the on-CF stimulus than for the off-CF stimuli because the threshold is lower when \( f_c \) is at the CF. The shapes of the period histograms for stimuli below CF resemble those at the CF. However, the period histograms for stimuli above CF clearly show two modes within each stimulus cycle at lower stimulus levels, unlike the on-CF and below-CF histograms. Such bimodal period histograms may result from the sharp transients occurring twice in each stimulus cycle at times when the envelope of the transposed tone shows a slope discontinuity (Fig. 1), which would be expected to induce ringing in the cochlear filters. Despite these complex histogram shapes, Fig. 7B shows that the synchronization index decreases monotonically with the level beyond a maximum for all three carrier frequencies, and the slopes are similar. However, the maximum synchrony is somewhat greater on the CF than either above or below the CF.

Period histograms showing two or more peaks per stimulus cycle were automatically identified from the presence of multiple zero crossings in the numerical derivative of the autocorrelation of the period histogram, which is considerably smoother than the raw period histogram. Multimodal period
histograms were seen in response to transposed tones in six of 22 fibers (27%) for carrier frequencies below the CF and in five of 27 fibers (19%) for carrier frequencies above the CF, but were never observed at the CF. Multiple peaks in responses to SAM tones were less prevalent and occurred in only one of 22 fibers (5%) for carrier frequencies below the CF and in four of 27 fibers (15%) for carriers above the CF. These observations are consistent with oscillations seen at the onset and, sometimes, offsets in response to tone bursts with abrupt onsets (Kiang et al. 1979; Rhode and Smith 1985). Such oscillations, which are observed only when the stimulus is presented in the steep gradients of the tuning curve above and below the CF, have been attributed to the ringing of the cochlear filters. Although ringing of the cochlear filters is characterized by steep gradients of the tuning curve above and below the CF, which are observed only when the stimulus is presented in the steep gradients of the tuning curve above and below the CF, the CF for the entire data set. To facilitate comparisons, stimulus level is expressed relative to the level of maximum synchrony at each carrier frequency. For all three ranges of carrier frequencies, the SI-level curves generally decrease monotonically for levels above the maximum and the slopes are similar. Precise trends, however, are hard to identify in Fig. 8A because of the large variability between fibers. To quantitatively compare the level dependency of SI on and off CF, for each fiber, we computed the difference between each off-CF SI-level curve and the corresponding on-CF curve. The resulting change in SI (ΔSI) level functions (Fig. 8B) are generally flat or just slightly increasing for both SAM and transposed tones. Flat ΔSI-level functions indicate that on- and off-CF SI-level functions have the same slopes, whereas sloping ΔSI-level functions indicate that SI decreases with level at different rates on and off the CF.

These effects were quantitatively analyzed by fitting a regression line to the entire set of ΔSI-level functions separately for each stimulus type (SAM and transposed) and each carrier frequency range (above and below the CF). The slopes and intercepts of the four best-fitting lines are given in Table 1. Because the ΔSI-level functions are plotted with respect to the level maximum, the intercept gives an estimate of the difference.

TABLE 1. Slopes and intercepts of ΔSI-level functions for SAM and transposed tones

<table>
<thead>
<tr>
<th>Stimulus</th>
<th>Carrier Range</th>
<th>Intercept</th>
<th>Slope, dB⁻¹</th>
</tr>
</thead>
<tbody>
<tr>
<td>SAM</td>
<td>( f_c &lt; CF )</td>
<td>0.029</td>
<td>0.0040</td>
</tr>
<tr>
<td>SAM</td>
<td>( f_c &gt; CF )</td>
<td>-0.108*</td>
<td>0.0059*</td>
</tr>
<tr>
<td>Transposed</td>
<td>( f_c &lt; CF )</td>
<td>-0.135*</td>
<td>0.0034</td>
</tr>
<tr>
<td>Transposed</td>
<td>( f_c &gt; CF )</td>
<td>-0.021</td>
<td>0.0005</td>
</tr>
</tbody>
</table>

Slopes and intercepts of the best-fitting lines to the ΔSI-level functions shown in Fig. 8B for each of the two stimuli (SAM and transposed tones) and two carrier frequency ranges (below and above the CF). Asterisks indicate values significantly different from 0 at the 0.05 level.
ence in $S_{\text{max}}$ off and on CF. Statistical analyses ($t$-test) show that the intercepts for SAM tones above CF and transposed tones below CF were significantly negative ($P < 0.05$), indicating a lower $S_{\text{max}}$ for these two conditions compared with when the carrier is at the CF. On the other hand, the intercepts did not significantly differ from zero for SAM tones below CF and for transposed tones above CF, indicating similar $S_{\text{max}}$ on and off CF in these conditions. The slopes of the best-fitting lines to the $\Delta S_{\text{I}}$-level functions did not, in general, differ from zero (Table 1), indicating that the rates of decrease of synchrony with level are similar on and off CF. The one exception is for SAM tones above the CF, where the slope was significantly positive, indicating that synchrony decreases more rapidly with level for SAM tones above CF than for SAM tones at CF. Despite these statistically significant differences, the overall effects are small and the general pattern of results suggests that the dependency of synchrony on level does not greatly differ on and off CF for either stimulus.

Phase-locking analysis with autocorrelation

Although the synchronization index is an appropriate measure of phase locking to a periodic stimulus when the period histogram is unimodal (as was largely the case in our data), it is a poor model of computations performed by the CNS because it necessitates a priori knowledge of the stimulus period. Recently, Louage et al. (2004) proposed alternative, autocorrelation-based measures of phase locking that capture the intrinsic periodicities in the spike responses without requiring prior knowledge of the stimulus. These measures make particular sense in the present context because interaural cross-correlation is a key component of most models for ITD processing. This section compares phase locking, as measured by $S_{\text{I}}$ to autocorrelation-based measures, and examines the extent to which these phase-locking metrics are correlated and can be used interchangeably.

Figure 9 shows the shuffled autocorrelogram (SACs; see METHODS) as a function of stimulus level for the same data that were analyzed with period histograms in Fig. 2. For all three stimuli, the SACs show multiple modes separated by the stimulus period, indicating phase locking to the stimulus. In stimuli, the SACs show multiple modes separated by the stimulus period. For all three stimuli, the SACs were analyzed with period histograms in Fig. 2. For all three stimulsi, the SACs show multiple modes separated by the stimulus period, indicating phase locking to the stimulus. In stimuli, the SACs show multiple modes separated by the stimulus period. For all three stimulsi, the SACs were analyzed with period histograms in Fig. 2. For all three stimulsi, the SACs show multiple modes separated by the stimulus period, indicating phase locking to the stimulus.

**FIG. 9.** $A$: shuffled autocorrelograms (SACs) as a function of stimulus level in response to a pure tone (black squares), SAM tone (red triangles), and a transposed tone (blue circles). Figure is based on the same data as in Fig. 2. $B$: normalized autocorrelation peak height vs. stimulus level with respect to rate threshold for the 3 stimuli. $C$: normalized autocorrelation half-width against sound level with respect to rate threshold for the 3 stimuli.
model \[ F \] performed significantly better than the single-curve data share the same value of parameters was the last one, in which the transposed and SAM variance of the residuals while using the smallest number of pure-tone responses separate. The model that minimized the transposed tone data were grouped together, while keeping the pure-tone responses separate. The model that minimized the parameter \( a \) was fit separately for each stimulus type, or the SAM and \( a \) tested, in which either the same curve (i.e., the same value of \( a \)) was fit to all the data, or a curve (a value of \( a \)) was fit separately for each stimulus type, or the SAM and transposed tone data were grouped together, while keeping the pure-tone responses separate. The model that minimized the variance of the residuals while using the smallest number of parameters was the last one, in which the transposed and SAM data share the same value of \( a \), but not the pure tone data. This model performed significantly better than the single-curve model \([F(1,1088) = 976.0, P < 0.001]\), while not performing significantly worse than the separate-curves model \([F(1,1087) = 3.079, P < 0.080]\). This best model (thick lines in Fig. 10) accounted for \( >98\% \) of the variance in the data, confirming the tight relationship between peak height and synchronization index. The best-fitting parameter \( a \) was 0.316 for pure tones and 0.460 for SAM and transposed tones. Because the relationship between peak height and synchronization index is the same for SAM tones and transposed tones, all conclusions based on the SI remain valid if we use the peak height instead for these two stimuli.

To verify that similar trends hold whether the SAC peak height or the SI is used as the phase-locking metric, Fig. 11 shows the level-maximum peak height (PH\(_{\text{max}}\)) as a function of frequency or \( f_m \) which can be compared with SI\(_{\text{max}}\) in Fig. 4A. We do not show slope data comparable to Fig. 4B for the peak height because the level dependency of peak height could not be fit by a straight line. As observed with the synchronization index metric (Fig. 4A), PH\(_{\text{max}}\) for transposed tones at modulation frequencies \(<250\) Hz is similar to pure-tone PH\(_{\text{max}}\) at 250 Hz and is higher than PH\(_{\text{max}}\) for SAM tones. However, the two metrics differ in that PH\(_{\text{max}}\) for pure tones continues to vary considerably with frequency \(<1,000\) Hz, whereas the SI is stable in that frequency range (see also Louage et al. 2004). The PH\(_{\text{max}}\) curve for pure tones also shows an unexpected dip at 1,000 Hz. In addition, the PH\(_{\text{max}}\) curves for SAM and transposed tones are less parallel to each other than the corresponding SI\(_{\text{max}}\) curves. In general, the PH\(_{\text{max}}\) measure tends to amplify the differences between stimulus conditions relative to SI when phase locking is strong. These differences are likely to reflect the compressive nature of the SI, which cannot exceed unity, whereas peak height can in principle reach arbitrarily large values. Despite these differences, the general trends of the effect of frequency on maximum phase locking across stimulus types hold for both metrics.

Although the SAC peak height measures the extent to which spikes occur in a certain temporal relationship with respect to each other across stimulus presentations, the half-width measures the temporal precision with which spikes occur at these preferred intervals. For periodic stimuli, the two metrics are expected to be negatively correlated because precise phase locking implies both a large peak height and a narrow half-width. However, the two measures might not be perfectly correlated if the relation between the two depended on the stimulus wave shape. Figure 12 shows a scatterplot of peak height against normalized half-width for the same data as in Fig. 10. The figure shows a clear, monotonically decreasing relationship between the two metrics. The data were fit by a hyperbolic function.

**FIG. 10.** Normalized SAC peak height (see METHODS) against SI for all recordings in response to low-frequency pure tones (black), transposed tones (blue), and SAM tones (red). Only pure-tone frequencies \(<1,000\) Hz are included. Best-fitting hyperbolic curves (solid lines) were fit separately to pure-tone data and to combined SAM and transposed tone data.

**FIG. 11.** Maximum SAC peak heights across all levels as a function of frequency or modulation frequency for pure tones (black dotted), transposed tones (blue solid), and SAM tones (red dashed). Error bars represent \( \pm 1 \) SE. Pure-tone responses are binned to the closest frequency shown.

**FIG. 12.** SAC peak height against normalized half-width for all low-frequency pure tone (black circles), transposed tone (blue triangles), and SAM tone (red asterisks) data. Solid line shows the best-fitting hyperbolic function (see RESULTS) for the entire data set.
The best-fitting parameter values for this model were constrained to be the same for all three stimuli. We chose the model in which the responses to all three stimuli are grouped together (i.e., the values of $b$ and $c$ are constrained to be the same for all three stimuli). The best-fitting parameter values for this model were $b = 1.369$ and $c = 0.857$. Although the model with three separate curves fit the data significantly better than the single-curve model $[F(4,1085) = 490.5, P < 0.001]$, we prefer the simpler single-curve model because the fraction of the variance accounted was only slightly greater for the three-curve model than for the single-curve model (93.62% vs. 93.30%) and the parameter estimates were essentially identical for all three curves in the more complex model. Thus the three phase-locking measures (synchronization index, peak height, and peak width) seem to be essentially identical for SAM and transposed tones, and the relationship between peak height and half-width is the same regardless of the stimulus. On the other hand, the relationship between peak height and synchronization index differs somewhat for pure tones compared with the other two stimuli. However, the differences in this relationship are fairly small and do not seem to substantially alter conclusions based on the traditional SI measure (Figs. 10 and 11).

**DISCUSSION**

We have investigated the neural mechanisms underlying ITD-based lateralization at high frequencies by characterizing the precision of phase locking for high-frequency SAM and transposed tones and for low-frequency pure tones at the level of the auditory nerve using both the traditional synchronization index and autocorrelation-based measures. Our results show similar precision of phase locking to pure tones and transposed tones only for a restricted set of conditions: stimulus levels close to thresholds, low modulation frequencies, and in low/medium-SR fibers. Phase locking to transposed and SAM tones fell faster with increasing stimulus level than phase locking to pure tones, although phase locking to transposed tones always exceeded phase locking to SAM tones. Maximum synchrony to transposed tones was similar to pure-tone maximum synchrony for modulation frequencies $<250$ Hz in low/medium-SR fibers, but fell faster than maximum synchrony to pure tones at higher modulation frequencies. The low-pass dependency of maximum synchrony on modulation frequency was similar for transposed and SAM tones. Responses to SAM and transposed tones with carrier frequencies below and above the CF generally showed a similar synchrony-level dependency as on-CF responses when the level was expressed relative to threshold at each frequency.

*Comparison of phase locking to pure and transposed tones*

Transposed tones are intended to produce similar temporal patterns of discharge in high-CF AN fibers as occur in low-CF fibers in response to low-frequency pure tones. Our results show that phase locking to transposed tones resembles phase locking to pure tones in only a restricted set of conditions. The rationale for stimulus transposition is based on a simple model of mechanoelectrical transduction in hair cells consisting of ideal half-wave rectification followed by low-pass filtering (van de Par and Kohlrausch 1997). Although this model is a useful first approximation, there are several differences in the way pure tones and transposed tones are processed in the cochlea, which lead to different auditory nerve discharge patterns. These differences involve 1) mechanoelectrical transduction, 2) cochlear compressions, and 3) cochlear filtering.

For pure tones, phase locking in the auditory nerve ultimately derives from the morphological polarization of the IHC ciliary bundle and resultant asymmetrical modulation of the hair-cell receptor potential (Hudspeth and Corey 1977). Because some of the transducer channels are open at rest (Ashmore 1991; Fettiplace and Fuchs 1999), a sinusoidal displacement of the cilia causes a modulation of the IHC receptor potential around rest, which in turn results in modulation in the release of neurotransmitter by the synapses at the base of the hair cells, and ultimately modulation of the instantaneous firing rate of the afferent neurons around SR in spontaneously active fibers (Johnson 1980). Because the fraction of transducer channels open at rest is $\approx 50\%$, the receptor potentials are asymmetrical (depolarizations are larger than hyperpolarizations) for all but the lowest stimulus levels, and modulations of the instantaneous firing rate are correspondingly asymmetric.

The situation is different for transposed tones because there is no hyperpolarization of the IHC membrane potential and no resulting decrease in the instantaneous firing rate below SR during the half-cycle when the stimulus has zero amplitude (Fig. 1) if possible adaptation effects are neglected (see following text). This lack of negative modulation of the instantaneous rate should result in a lower synchronization index for transposed tones compared with pure tones in spontaneously active fibers, but not in fibers with low spontaneous activity. Consistent with this reasoning, we found that maximum synchrony to pure tones is significantly greater than maximum synchrony to transposed tones in high-SR fibers, but not in low/medium-SR fibers. However, these differences between SR groups are pronounced only at low stimulus levels.

A second, more important, factor underlying differences in responses to pure and transposed tones is the strong compression manifested primarily in the saturation of rate-level functions. Despite rate saturation, phase locking to pure tones remains fairly stable over a wide range of stimulus levels (Fig. 3; Johnson 1980). In contrast, phase locking to the envelope of SAM tones reaches a maximum only a few decibels above threshold and then falls steeply with increasing level (Cooper et al. 1993; Javel 1980; Joris and Yin 1992; Smith and Brachman 1980; Yates 1987). Similar degradations in phase locking have been observed for nonsinusoidal envelope modulations (Delgutte 1980; Wang and Sachs 1993). Our results show that responses to transposed tones behave similarly to responses to SAM tones in this respect, although the fall in synchrony with increasing level is not as steep for transposed tones as for SAM tones, particularly for low modulation frequencies (Figs. 3 and 5). At higher modulation frequencies, the level dependency of synchrony becomes more similar for SAM and transposed tones (Figs. 5 and 4B), consistent with the

\[ HW = \frac{1}{b(PH - 1) + c} \]  

where $HW$ is the normalized peak half-width and $b$ and $c$ are free parameters. As in Fig. 10, different versions of the model were tested by grouping the responses to the three stimuli in various ways. We chose the model in which the responses to all three stimuli are grouped together (i.e., the values of $b$ and $c$ are constrained to be the same for all three stimuli). The best-fitting parameter values for this model were $b = 1.369$ and $c = 0.857$. Although the model with three separate curves fit the data significantly better than the single-curve model $[F(4,1085) = 490.5, P < 0.001]$, we prefer the simpler single-curve model because the fraction of the variance accounted was only slightly greater for the three-curve model than for the single-curve model (93.62% vs. 93.30%) and the parameter estimates were essentially identical for all three curves in the more complex model. Thus the three phase-locking measures (synchronization index, peak height, and peak width) seem to be essentially equivalent for SAM and transposed tones, and the relationship between peak height and half-width is the same regardless of the stimulus. On the other hand, the relationship between peak height and synchronization index differs somewhat for pure tones compared with the other two stimuli. However, the differences in this relationship are fairly small and do not seem to substantially alter conclusions based on the traditional SI measure (Figs. 10 and 11).
idea that the cochlear filters increasingly attenuate the additional side bands of the transposed tones, effectively making the two stimuli more alike.

The degradation in phase locking to the envelope of SAM tones with increasing stimulus level is qualitatively consistent with the saturating character of rate-level functions because a given modulation in stimulus amplitude creates a smaller modulation of the firing rate when the mean intensity is in the saturated part of the rate-level function. At first sight, this explanation does not hold for transposed tones because the output of any instantaneous compression would remain zero regardless of stimulus level during the entire envelope half-cycle for which the stimulus amplitude is zero (the “off period”). However, the slow decay time constant of the cochlear filter (and other filters arising in the hair cell membrane and synaptic transmission) prolongs the response to transposed tones into the stimulus off period. Figure 2 clearly shows this encroachment of responses to transposed tones into the stimulus off period at high stimulus levels for a modulation frequency of 250 Hz. The duration of this encroachment at the highest level (>1 ms) is consistent with the duration of click responses for fibers with similar CFs (Kiang et al. 1965). This prolongation of the responses to each cycle of a transposed tone should be most significant at higher modulation frequencies, where they occupy an increasingly large fraction of the modulation cycle. Consistent with this prediction, the slopes of synchrony-level functions decrease with increasing $f_m$ and, for very low $f_m$ (60 Hz), the degradation in phase locking with level for transposed tones is comparable to that for low-frequency pure tones (Fig. 4B).

Our discussion so far has neglected possible effects of adaptation. It has been argued that rapid adaptation generally enhances the coding of dynamic stimuli and, in particular, accounts for the observation that the maximum synchrony to the envelope of SAM tones is greater, and occurs at higher stimulus levels, than expected based on the static rate-level function (Cooper et al. 1993; Smith and Brachman 1980; Yates 1987). Although we did not quantitatively compare phase locking to transposed tones with predictions based on static rate-level functions, transposed tones are likely to behave similarly to SAM tones in this respect. Adaptation could also decrease the instantaneous firing rate below the SR during the stimulus off period and thereby enhance the coding of SAM and transposed tones in spontaneously active fibers. Although these effects of adaptation are likely to occur, they are apparently too weak to counteract the larger effects of cochlear tuning and compression on responses to transposed tones, with the net result that phase locking to transposed tones generally falls below synchrony to pure tones.

Cochlear frequency selectivity is likely to be responsible for the result that synchrony to SAM and transposed tones falls faster with increasing modulation frequency than synchrony to pure tones falls with frequency (Fig. 4). As modulation frequency increases, the side bands of SAM and transposed tones are increasingly attenuated by the cochlear filters, so the effective modulation in the mechanical drive to the hair cells also decreases. Joris and Yin (1992) argued that the upper frequency limit of phase locking to SAM tones is determined by cochlear filtering for CFs $\leq$10–15 kHz, and by a temporal limitation at higher CFs. Because most (37 of 39 fibers, 66 of 69 responses) of our transposed tone data were from fibers with CFs $<10$ kHz, and because the upper cutoff of phase locking is similar for transposed tones and SAM tones (Fig. 4A), phase locking to transposed tones is likely to be largely limited by cochlear filtering in our data. In contrast, phase locking to pure tones is limited by an inability of synapses to follow fast changes in the hair-cell receptor potential (Weiss and Rose 1988). The different mechanisms for pure and transposed tones partly explain why the upper limit of phase locking is lower for transposed tones than for pure tones (Fig. 4). This difference might be even more pronounced in humans if, as some data suggest (Shera et al. 2002; but see Ruggero and Temchin 2005), cochlear frequency resolution is significantly sharper in humans than in cats.

In short, various cochlear mechanisms including frequency selectivity, hair cell transduction, and synaptic transmission all contribute to the temporal discharge patterns in the auditory nerve for transposed tones differing from those for pure tones in all but a restricted set of conditions. Consequently, physiological and central physiological studies should be cautious about assuming a strict similarity in the peripheral representations of the two stimuli.

Relation to studies of ITD coding in central auditory neurons

The only single-unit study of auditory neurons that used transposed tones is that of Griffin et al. (2005), which compared ITD sensitivity to SAM and transposed tones for high-frequency neurons in the inferior colliculus (IC) of anesthetized guinea pigs. Griffin et al. found a greater proportion of neurons sensitive to ITD for transposed tones than for SAM tones and, among sensitive neurons, a greater modulation of firing rate with ITD for transposed tones. In addition, neural ITD just noticeable differences (JNDS) estimated using signal detection theory (ROC analysis) were smaller for transposed tones than for SAM tones at the same modulation frequency. At low modulation frequencies (<280 Hz), the best neural ITD JNDS for transposed tones were comparable to the JNDS measured by Shackleton et al. (2003) for their pure-tone counterparts. However, ITD sensitivity was too poor to allow estimation of neural JNDS for either SAM or transposed tones with $f_m >280$ Hz, whereas pure-tone neural ITD JNDS improve with increasing frequency $\leq 500$ Hz (Shackleton et al. 2003). The ITD sensitivity of the IC neurons studied by Griffin et al. is thought to be largely inherited from that of neurons in the medial and lateral superior olives (MSO and LSO) that, in turn, ultimately depends on phase locking in theafferent inputs from both ears. Because Griffin et al. used low stimulus levels (about 15 dB above pure-tone thresholds at the carrier frequency), their finding of comparable ITD sensitivity for pure tones and transposed tones at low frequencies is consistent with our observation that maximum synchrony in AN fibers is similar for the two stimuli at low frequencies (Fig. 4). However, our finding that synchrony to transposed tones falls much faster with increasing level than synchrony to pure tones raises the question of how the ITD sensitivity of IC neurons to the two stimuli would compare at higher stimulus levels.

There is scant information on the level dependency of ITD sensitivity in IC neurons to either low-frequency pure tones or high-frequency SAM tones. The few studies that even address the question (Batra et al. 1993; Fitzpatrick et al. 2005; Kuwada and Yin 1983; Yin and Kuwada 1983) are more concerned with
shifts in the best ITD with level rather than with changes in sharpness of ITD tuning, which are more directly relevant to a characterization of ITD sensitivity in terms of neural JNDS. A majority of the examples of pure-tone ITD curves found in the literature (Fig. 9A in Kuwada and Yin 1983; Fig. 10B in Yin and Kuwada 1983; Fig. 10 in Kuwada et al. 1984) show no major changes in sharpness of tuning over up to a 40-dB level range, although one unit (Fig. 12 in Kuwada et al. 1984) does show substantial level-dependent changes in the shapes of ITD curves measured with binaural beats. An unpublished study (DC Fitzpatrick, personal communication) reports a mean increase of 3 μs/dB in the half-widths of composite ITD curves obtained by summing pure-tone ITD curves over a wide range of frequencies. This moderate degradation in ITD tuning appears to be related to a lowering of the frequency, which contributes most to the composite ITD curve, and does not necessarily occur in response to individual tones. Thus it is hard to confidently relate the degradation in composite ITD tuning to the small decrease in synchronization index with level we observed in AN fibers for pure tones (Fig. 3). Based on our results, the degradation in ITD tuning with level would be expected to be more substantial for SAM and transposed tones than for pure tones. Unfortunately, we are not aware of any report on the effect of level on ITD tuning widths for amplitude-modulated (AM) tones. Further studies are needed to systematically characterize the effects of stimulus level on ITD sensitivity for both low-frequency pure tones and, especially, high-frequency AM stimuli, and to determine whether the similarity in ITD tuning between pure tones and transposed tones observed at low stimulus levels by Griffin et al. (2005) also holds at higher levels.

Relation to psychophysical studies using transposed tones

The present study was motivated by the finding that ITD JNDS for transposed tones in human listeners are lower than JNDS for SAM tones and, at low modulation frequencies (≤128 Hz), are comparable to pure-tone JNDS (Bernstein 2001; Bernstein and Trahiotis 2002; Oxenham et al. 2004). Ideal observer (or optimal processor) models of binaural processing, based on auditory-nerve activity (Colburn 1973, 1996), predict that ITD discrimination performance improves with increasing synchronization index given a reasonable mathematical description of the shapes of period histograms of AN fibers. Therefore our characterization of the phase locking of ANFs is relevant to an understanding of the neural mechanisms underlying the psychophysical results of Bernstein and Trahiotis (2002). Their finding that ITD JNDS are lower for transposed tones than for SAM tones at all modulation frequencies is consistent with our finding that synchrony to transposed tones is better than synchrony to SAM tones (Figs. 3, 4, 5, and 11) for all frequencies and levels. However, their finding of similar ITD JNDS for pure and transposed tones is hard to interpret in the context of our physiological results when the effect of level is taken into account. Our results suggest that, at the level (75 dB SPL) where Bernstein and Trahiotis made their measurements, virtually all AN fibers with CFs close to the carrier frequency of transposed tones would show much poorer phase locking than in response to their pure-tone counterparts, and therefore ITD JNDS predicted by ideal-observer models would be considerably poorer for transposed tones than for pure tones.

There are several possibilities for reconciling the neural data with the psychophysics. One is that the binaural processor relies on fibers with CFs far from the carrier frequency of transposed tones for ITD discrimination. We have shown that maximum phase locking to transposed tones is nearly as good off the CF as that on the CF (Fig. 8), so these remote fibers can provide precise ITD information at high stimulus levels. However, contrary to this hypothesis, an unpublished human psychophysical study (Dreyer et al. 2005) found that ITD discrimination for transposed tones remains stable at high stimulus levels even in the presence of band-reject noise that was designed to mask ITD information in all but a narrow band (±20% of f0) of CFs centered at f0. Alternatively, ITD discrimination at high sound levels might be based on the small fraction of high-threshold fibers that would still show good phase locking to transposed tones. The binaural processor would have to somehow focus on this small fraction of informative fibers and ignore the others. In awake animals, the number of informative fibers at high levels might be increased by activation of the olivocochlear efferents, which is known to shift rate-level functions to higher levels (Guinan and Stankovic 1996; Wiederhold and Kiang 1970). However, because the effect of olivocochlear efferent on dynamic range is most obvious in the presence of background noise (May and Sachs 1992), efferents would not be expected to play a large role in the experiments of Bernstein and Trahiotis (2002) because there was no background noise near f0. Finally, the small, but nonzero, synchrony cues available in response to transposed tones at high levels (Fig. 3) may be enhanced in the CNS before binaural interactions. Many cell types in the VCN show a general enhancement in synchrony to the envelope over synchrony seen in the auditory nerve, as well as a smaller decrease in synchrony with level (Frisina et al. 1985, 1990; Joris et al. 2004; Rhode and Greenberg 1994). This synchrony enhancement may be more significant for transposed tones, which produce small synchrony, than for pure tones, for which synchrony is already high in the auditory nerve.

Bernstein and Trahiotis (2002) found that psychophysical ITD JNDS for transposed and SAM tones degrade rapidly for modulation frequencies >128 Hz, whereas pure-tone ITD JNDS continue to improve up to ≥512 Hz. At first sight, this frequency dependency may seem germane to our result that maximum phase locking to SAM and transposed tones begins to decrease between 125 and 250 Hz. However, the degradation in ITD discrimination performance is precipitous (some of Bernstein and Trahiotis’ subjects could not do the task at all at 512 Hz), whereas the degradation in phase locking is more gradual, and there is still significant synchrony at 1,000 Hz. Moreover, we have argued that cochlear filtering is likely to determine the upper limit of phase locking to SAM and transposed tones in our data, whereas Bernstein and Trahiotis provide strong arguments against peripheral filtering being responsible for the degradation in their ITD JNDS. Thus it is likely that the frequency limitation on ITD discrimination based on the envelope is central rather than peripheral. Bernstein and Trahiotis (2002) were able to fit their JND data by introducing a 150-Hz low-pass filter operating on the envelope in their cross-correlation model of binaural processing (Bernstein and Trahiotis 1996). Although such a filter is consistent
with psychophysical results on monaural envelope perception (Kohlrausch et al. 2000), the ordering of the envelope filter and the binaural processor in their model is physiologically problematic. Bernstein and Trahiotis assumed that the envelope filter precedes binaural processing. Yet, temporal modulation transfer functions (tMTFs) of MSO and LSO neurons, the neurons that perform initial processing of ITD, typically have considerably higher upper cutoff frequencies than the 150 Hz postulated in the Bernstein and Trahiotis model (Grothe et al. 1997, 2001; Joris and Yin 1998). The 150-Hz cutoff is more in line with the tMTFs of most IC neurons (Krishna and Semple 2000), but the ITD sensitivity of these neurons is thought to be largely inherited from their MSO and LSO inputs (Ingham and McAlpine 2005). Nevertheless, the possibility that some form of ITD sensitivity arises anew in the IC cannot be ruled out (Malmierca et al. 2005; Oliver 1987). Alternatively, the upper frequency limit on the ability to process ITDs in the envelope of high-frequency stimuli may not originate in brain stem processing per se, but rather in the inability of higher processing stages to make use of the binaural information conveyed by brain stem neurons. Why such a limit would operate on the envelope and not the fine structure is unclear. Thus the contrast in both level and frequency dependency between the psychophysical results of Bernstein and Trahiotis (2002) and the present physiological results raises important questions about the neural mechanisms for processing envelope ITDs.

Transposed tones have also been used to study pitch perception. Oxenham et al. (2004) found that frequency JNDs are considerably poorer for transposed tones with modulation frequencies in the range 55–320 Hz than for their pure-tone counterparts, even though their listeners had good ITD discrimination with the transposed tones for modulation frequencies <150 Hz. Moreover, listeners were unable to form pitch percept for transposed tone complexes consisting of three transposed tones with modulation frequencies corresponding to harmonics 3, 4, and 5 of a common fundamental, whereas harmonic complex tones consisting of three pure tones evoked a strong pitch percept. Oxenham et al. (2004) interpreted their results as evidence against purely temporal models of pitch processing. This interpretation depends on the assumption that transposed tones and their pure tone counterparts produce essentially equivalent temporal discharge patterns in the auditory nerve. However, at the stimulus levels used in their experiments (70 phons for simple tones; 65 dB SPL per component for complex tones), a majority of the auditory-nerve fibers would show considerably poorer phase locking to transposed tones than to pure tones, and this issue would be most severe for the transposed tone complexes because the presence of multiple components would interfere with the spread of excitation to cochlear regions that would otherwise show good phase locking.3

On the other hand, if the degradation in AN phase locking at high stimulus levels is responsible for the poor frequency discrimination performance with transposed tones compared with pure tones, it is hard to understand why ITD discrimination is comparable for the two stimuli at low frequencies. Thus the Oxenham et al. (2004) results pose problems for purely temporal accounts of pitch and binaural processing.

Phase-locking metrics

Traditionally, phase locking to pure tones and SAM tones has been characterized by the synchronization index, or vector strength (Goldberg and Brown 1969; Johnson 1980). In circular statistics, the SI is a general measure of the concentration of the probability distribution around its mean, analogous to the SD for distributions along a line (Mardia and Jupp 2000). Thus this metric is an appropriate measure of the precision of phase locking to the fundamental of periodic stimuli when the period histogram is unimodal, as was usually the case in our data. The synchronization index is also appropriate for characterizing ITD sensitivity because, given reasonable assumptions about the shapes of period histograms, performance of ideal-observer models of ITD processing increase monotonically with the SI of the input neurons (Colburn 1973). However, the synchronization index is a poor model of the computations performed by the CNS because it requires a priori knowledge of the stimulus period, information that is not explicitly available to the central processor. Louage et al. (2004) proposed alternate measures of phase locking that are more appealing from the perspective of central processing because they are based on interspike interval statistics; in addition, they apply to both periodic and aperiodic stimuli such as noise. Specifically, the shuffled autocorrelation (SAC) is useful to characterize phase locking because, by tallying intervals between spikes obtained in response to different presentations of the same stimulus,4 it eliminates the distortions caused by neural refractoriness in the traditional autocorrelation (Louage et al. 2004). The SAC is particularly appropriate for characterizing ITD sensitivity because the computation it performs is equivalent to that of a binaural cross-correlator receiving statistically independent, identically distributed spike train inputs from the two ears, as postulated in many models of binaural processing (Colburn 1973, 1996).

We compared the traditional synchronization index measure of phase locking with two measures based on the SAC for our three stimuli. For all stimuli, the SAC had the same period as the stimulus, indicating phase locking, and each SAC period had a single peak with a symmetric, nearly triangular shape (Fig. 9). For each stimulus, the SAC peak height was monotonically related to the synchronization index and the relationship was nonlinear (expansive), reflecting the upper limit of the synchronization index at unity (Fig. 10). A similar result was previously reported for pure-tone stimuli by Louage et al. (2004).5 The compressive nature of SI is evident in the steeper falloff of phase locking with level seen with SAC than with SI

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3 Reported simulations by Oxenham et al. (2004) of responses to their stimuli using the Meddis and O’Mard (1997) model were run at much lower stimulus levels than those used in the psychophysical experiments, suggesting that the compressions present in the model may have degraded the temporal cues at higher levels, consistent with our physiological data.

4 A related procedure (de Cheveigne’ 1998) first aligns the spikes from all stimulus presentations onto the same time axis and then computes the autocorrelation of the combined spike train. The resulting histogram contains both intervals between spikes from different stimulus presentations and intervals from within the same presentation, i.e., it is the sum of the SAC and the traditional autocorrelation. For large numbers of stimulus presentations, it approaches the SAC because the contribution of the intervals from the same presentation becomes negligible.

5 A quantitative comparison with the data reported in Louage et al. (2004) is difficult because their peak height metric was not based directly on the SAC, but on a more complex (and less physiological) form of correlation, the “difcor,” which combines responses to two stimuli with opposite polarities. Although their metric has the advantage of separating phase locking to the envelope from phase locking to the fine time structure, it was for this very reason not suitable for our purpose of comparing phase locking to the pure-tone waveform with phase locking to the envelopes of SAM and transposed tones.
Previous neurophysiological studies, they also raise fundamental questions about the central neural processing of the amplitude envelope at high sound levels, in particular with respect to the binaural processing of envelope ITDs.

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**References**


ENVELOPE PHASE LOCKING AT HIGH FREQUENCIES


