Neuronal responses to moving targets in monkey frontal eye fields.

Carlos R. Cassanello, Abhay T. Nihalani and Vincent P. Ferrera

Columbia University, Department of Neuroscience, and Keck-Mahoney Center for Mind and Brain, 1051 Riverside Dr., Unit 87, Kolb Research Annex 504, New York, New York 10032, USA

Abbreviated Title: Predictive responses in frontal eye fields.

Corresponding Author:
Dr. Carlos R. Cassanello
Department of Psychology
Australian National University
Canberra, ACT 0200 Australia
Email: Carlos.Cassanello@anu.edu.au

Key words: prediction, anticipation, flash-lag, frontal eye field, saccade target velocity compensation

Acknowledgments: Supported by NIH-MH59244
Abstract

Due to delays in visuo-motor processing, eye movements directed toward moving targets must integrate both target position and velocity to be accurate. It is unknown where and how target velocity information is incorporated into the planning of rapid (saccadic) eye movements. We recorded the activity of neurons in frontal eye fields (FEF) while monkeys made saccades to stationary and moving targets. A substantial fraction of FEF neurons were found to encode not only the initial position of a moving target, but the metrics (amplitude and direction) of the saccade needed to intercept the target. Many neurons also encoded target velocity in a nearly linear manner. The quasi-linear dependence of firing rate on target velocity means that the neuronal response can be directly read-out to compute the future position of a target moving with constant velocity. This is demonstrated using a quantitative model in which saccade amplitude is encoded in the population response of neurons tuned to retinal target position and modulated by target velocity.

Introduction

In a world filled with moving objects, the ability to anticipate where things are headed is crucial for survival. Due to delays in sensory-motor pathways, the position of a moving object as represented in the brain could lag behind the object’s true position (Schlag and Schlag-Rey 2002). The discrepancy between an object’s true location and its neural representation might cause visually-guided reaching and eye movements to be inaccurate. But since real objects tend to move in a predictable manner, the brain can compensate for object motion by incorporating an estimate of target velocity (speed and direction) when planning movements or constructing an internal representation of the target. Rapid eye movements (saccades) are programmed based on a ‘position error’ that
represents the difference between the current and desired eye position. There is evidence that this error signal is sampled approximately 70 to 80 msec before the onset of the saccade (Becker and Jurgens 1979). Because of this delay, saccades based on position error alone should always undershoot a moving target. The size of the undershoot would exceed the radius of the fovea for targets moving at very modest speeds (<10 deg/sec). However, monkeys and humans can make accurate saccades to moving targets, suggesting that they compensate for target velocity during saccade planning (Heywood and Churcher, 1979; Keller and Steen Johnsen 1990; Ron et al. 1989a,b; Guan et al. 2005; Eggert et al 2005; de Brouwer et al. 2001, 2002a,b). One possible explanation for this accuracy is that saccades to moving targets are produced by a system that combines a past measure of the position error with an additional correction based on target velocity (Robinson 1973).

Little is currently known about the neural substrate for saccade target velocity compensation in primates. Patients with neurological disorders such as schizophrenia have an impaired ability to estimate motion (Hooker and Park 2000), suggesting a possible link to frontal lobe function. There is evidence that the accuracy of saccades to moving targets is compromised by lesions to primary visual cortex (V1) and to the middle temporal (MT) motion area, while saccades to stationary targets are not affected (Segraves et al., 1987; Newsome et al. 1985). It has been shown that neurons in the deep layers of the superior colliculus encode the instantaneous position of a moving target but not the saccade needed to intercept the target (Keller et al. 1996). These findings provide support for the hypothesis that saccades made to moving targets are controlled by at least two partially separate pathways, one of which is concerned strictly with correction of a pre-saccadic retinal position error, and another which extrapolates future position based on the velocity of the moving target. The former pathway includes the SC while the latter does not. In this paper we attempt to answer the question of whether the FEF belongs to either or both pathways.
The frontal eye field (FEF) receives robust input from motion processing areas MT and MST (Schall et al. 1995), contains neurons that are selective for motion speed and direction (Xiao et al. 2006), and sends output to the caudate nucleus, superior colliculus, and pons (Stanton et al. 1988), making it a good candidate for providing target velocity signals to the saccade system. We obtained data from 96 neurons in the FEF while monkeys made saccades to stationary or moving targets. We found evidence that FEF neurons code not only the instantaneous position of a moving target, but also the metrics of the saccade required to intercept the target. FEF neurons are also modulated by target speed even when target position and saccade metrics are held constant. Thus, the three variables involved in target velocity compensation (target position, target velocity and saccade metric) are available in FEF, providing evidence that this structure may be involved in extrapolating target motion when planning saccades.

**Methods**

Experiments were performed on four sub-adult male rhesus monkeys (Macaca mulatta) weighing between 5 and 8 kg. All methods were approved by the Institutional Animal Care and Use Committee at Columbia University and the New York State Psychiatric Institute. Monkeys were prepared for experiments by surgical implantation of a post used for head restraint and a recording chamber to give access to the cortex. Eye position was recorded using a monocular scleral search coil. All surgical procedures were performed using aseptic technique and general (isoflurane 1-3%) anesthesia. Monkeys were trained to sit in a primate chair for the duration of the experiment with their heads restrained and perform the saccade tasks. Correct performance of the task was reinforced by liquid reward.

**Visual stimulation**
Visual stimuli were generated and controlled by a Cambridge Research Systems VSG2/3F video frame buffer. The output from the video board was displayed on a calibrated 37 in. color monitor (Mitsubishi) with a 60 Hz non-interlaced refresh rate. The monitor stood at a viewing distance of 24 in. so that the display area subtended roughly 40 deg. horizontally by 30 deg. vertically. The spatial resolution of the display was 1280 pixels by 1024 lines. Fixation targets were small (0.5 deg) yellow squares presented on a uniform black background. The luminance of the fixation target was 65.0 cd/m², while the background was close to 0 cd/m² (below the photometer threshold). The frame buffer was programmed to send out digital pulses (frame sync) for timing purposes at the beginning of each video frame in which a target was turned on or off. These pulses were recorded by the computer using a hardware timer, and stored together with the neuronal and eye movement data.

Neuronal recording and electrical stimulation

Recording chambers (20 mm diameter) were implanted on the skull overlying the arcuate sulcus, positioned at stereotaxic coordinates 25A, 15L. At the start of each recording session, a hydraulic microdrive was mounted on the recording chamber. Recordings were made using platinum-iridium electrodes with impedances of 0.1 - 1 Mohm. Signals from the microelectrode were amplified, filtered and monitored on an oscilloscope and audio monitor. A time-amplitude window discriminator converted extracellular action potentials into digital pulses (TTL), which were sampled by the computer with 0.01 ms time resolution. Units were isolated on the basis of waveform. When a unit was isolated, stimulus parameters such as position and size were adjusted to optimize its response. Neuronal spike trains were collected and stored along with eye position and velocity records. Electrical microstimulation was used to map the region of cortex from which neuronal recordings were obtained in each monkey. Sites in peri-arcuate cortex were stimulated through the same
electrode used to record neuronal activity. The stimulation consisted of a train of 0.2 msec biphasic pulses at a rate of 350 pulses/sec delivered by an optically isolated pulse stimulator (AM Systems). The output of the stimulator was gated by a computer generated TTL level so as to be synchronized with other trial events. The current threshold for evoking saccades was determined by stimulating during a fixation task (Opris et al., 2001). The threshold was defined as the current level at which involuntary saccades were evoked on about half the stimulation trials (Bruce et al., 1985). Recording and stimulation sites were classified on stimulation threshold as being within the low-threshold FEF if the threshold was less than 85 uA (range: 10-85 uA; mean: 43 uA). This classification uses a higher threshold criterion than others have used (Bruce et al., 1985). However, we feel this is warranted as thresholds were measured during a fixation task which results in higher thresholds as compared to stimulation free gaze (Goldberg, Bushnell, & Bruce, 1986).

For all sites, electrically evoked saccades were almost always contraversive and showed a mediolateral gradation of amplitudes (Bruce and Goldberg, 1985). In addition, the evoked saccade direction rotated systematically as the depth of the electrode changed. These features of the saccade amplitude and direction map are characteristic of the FEF.

Eye Movement Recording

Eye position was monitored using a monocular scleral search coil system (CNC Engineering). The eye position signals were then digitally sampled by computer at 1 kHz per channel and digitized with 12-bit resolution, and stored on a disk for offline analysis. Velocity was computed from eye position information using a differentiator filter algorithm. Eye position and velocity were used to estimate saccade parameters. Polar eye velocity (rvel) was constructed combining the magnitudes of the horizontal (hvel) and vertical (vvel) eye velocity. Polar eye velocity was digitally differentiated to
yield polar acceleration (racc). Saccade onset was computed using an acceleration criterion (racc ≥ 500 deg/sec²). Saccade offset was found using the complementary criterion (racc ≤ 500 deg/sec²). This criterion was not always appropriate for small saccades, hence each trial was also checked by visual inspection.

**Behavioral paradigms**

Monkeys were trained to perform various oculomotor tasks during neuronal recording. Once a neuron was isolated, a memory guided saccade task (MEM) was used first to find the preferred direction of the cell. In the MEM task, monkeys made saccades to the remembered location of a visual cue. The cue location varied among eight positions, equally spaced (45 deg) around the clock. At the beginning of each trial the monkey fixated a small red square. A peripheral cue was flashed for 250 ms followed by a variable delay (750-1250ms) during which the fixation target remained on and the monkey maintained fixation within a 2 x 2 deg window. At the end of the delay, the fixation target disappeared and the monkey was allowed up to 600 ms to make a saccade to the remembered location of the cue. After the 600 ms saccade interval, and if the monkey’s memory-saccade was within a 3 x 3 deg window centered on the cue location, the cue re-appeared to provide feedback to the monkey and corrective saccades were generally made at this time. Before commencing data collection, the eccentricity of the peripheral cue was varied to find the optimum eccentricity for each neuron. Data were then recorded with a fixed eccentricity. For analysis each MEM trial was divided in seven time intervals including visual, pre and peri-saccadic intervals. More details on this task have been given elsewhere (Cassanello and Ferrera 2007b).

After collecting data for the memory-guided saccade task, we switched to the tracking task. In this task, the subject was required to make saccades to stationary or moving targets. The following
describes the standard task geometry, which could be scaled and rotated to match the receptive field size and eccentricity of individual neurons. The initial target positions were arranged collinearly (“on-axis”, Fig. 1A,C) or perpendicular (“off-axis”, Fig. 1B,D) to the neuron’s preferred direction (Fig 1. shows only a subset of target positions, to avoid clutter). The on-axis targets were located in the receptive/movement field of the cell at 8 different distances (3, 6, 9, 10, 12, 15, 18 or 21 deg) from the fixation point, which was presented at the center of the display (Fig. 1A). The target either remained stationary, or moved toward or away from the center of the display at 10 or 30 deg/sec. The off-axis trials (Fig. 1B) consisted of saccades to targets with initial positions along a line perpendicular to the preferred direction of the neuron. There were up to 11 off-axis target positions and the spacing between the targets was 3 deg. The eccentricity of the off-axis target nearest to the fixation point was 10 deg. Off-axis targets were stationary or moved with two speeds (10 and 30 deg/sec) in two directions (along an orientation perpendicular to the cell’s preferred direction).

**Data analysis**

The tracking task had 62 different stimulus conditions comprising different combinations of initial target position, speed and direction. All stimulus conditions were presented interleaved randomly within each block.

We used regression analysis to assess the validity of the previously reported relation between saccade amplitude, position error and target velocity (Keller & Steen Johnsen 1990; Eqn 1).

\[
SA = \alpha + \beta_1 \times PE + \beta_2 \times TV
\]

Where SA is saccade amplitude, PE is position error and TV is target velocity\(^1\). One way to think about this regression analysis is that it provides estimates of the weights given to PE and TV in
saccade planning. Ideally, the initial position error would be fully incorporated into the saccade plan \((\beta_1 = 1.0)\), and the target velocity would be weighted according to the time elapsed between the sampling of PE and the onset of the saccade because elapsed time multiplied by target velocity yield the required compensation in deg. Thus \(\beta_2\) should be approximately 0.1 if position error is sampled 100 msec prior to saccade onset \((\beta_2\), has dimensions of seconds, whereas \(\beta_1\) is dimensionless). All of the variables in Eqn 1 are time-dependent, where time is measured relative to saccade onset. In the Results, we explore the effects of using different time points on the parameter estimates.

To accommodate off-axis target motion, Eqn 1 can be expanded to two-dimensions by treating the horizontal \((x)\) and vertical \((y)\) components of each variable independently:

\[
(2a) \quad S_x = \alpha + \beta_{1x} \cdot PE_x + \beta_{2x} \cdot TV_x
\]
\[
(2b) \quad S_y = \alpha_y + \beta_{1y} \cdot PE_y + \beta_{2y} \cdot TV_y
\]

This allows one to perform the analysis described in the preceding paragraph for any target motion, not just radial motion (i.e. target motions lying along a line extending outward from the center of gaze).

For analysis of neural activity, each trial of the static target saccade task and step-ramp saccade task was divided into seven time epochs: (1) fixation interval: 100 ms before the saccade target onset; (2) visual interval: first 100 ms after the onset of the saccade target and prior to any saccade; (3) pre-saccadic interval: 100 ms prior to the onset of the first saccade; (4) peri-saccadic interval: 100 ms window centered on saccade onset; (5) post-saccadic interval: 100 ms after the onset of the saccade; (6) from target onset to saccade onset: variable length; (7) from target onset to 100 ms after saccade onset: variable length. The average firing rate was computed within each time window.

\(^1\) Often-used abbreviations: firing rate (FR), target velocity (TV), saccade amplitude (SA), saccade direction (SD), position error (PE), direction error (DE).
The number of repetitions of each trial condition was typically 5 to 10 with some units recorded over 15 complete blocks.

The pre- and peri-saccadic trial epoch measure neural activity starting 100 or 50 ms, respectively, before saccade onset. If visual input for saccade planning is sampled 100 ms before the saccade, then one might have expected the time windows for neural data analysis to bracket that time point, e.g. 150-50 msec prior to saccade onset. But behavioral estimates of when input is sampled for saccade planning refer to when the input is available at the retina. FEF neurons have visual latencies of approximately 50 msec, hence it is appropriate to shift the time window for analyzing FEF responses by about that amount. On the other hand, movement-related activity in FEF can appear as high-frequency bursts that start about 50 msec prior to saccade onset and continue through saccade initiation. Furthermore, latencies for electrically-evoked saccades in the FEF are in the range of 30-40 msec. These considerations justify looking at FEF activity 50 ms prior to saccade onset.

We selected neurons based on two criteria. First, for each cell we first performed a test to determine whether the response after target onset was significantly modulated relative to activity in the fixation interval. This was accomplished by performing a two-sided t-test on the difference between the mean firing rate of the visual, pre and peri-saccadic intervals and the background/fixation interval. This allowed us to reject the null hypothesis that the neuronal response was unmodulated either by the presence of visual stimulation or by the movement of the eyes. Another exclusion criterion was based on too few trial repetitions. Only data sets with more than three repetitions per stimulus condition were used. These criteria left 96 neurons for further analysis out of 124 total cells that were recorded.

To examine the neuronal responses during saccades to stationary and moving targets we plotted the firing rate (FR) as a function of target velocity (TV), saccade amplitude (SA) defined as
the distance between the position of the eye at the end of the saccade minus the position of the eye at saccade onset, and the position error (PE) defined as the difference between the position of the target and the position of the eye 100 ms before the saccade onset. For each trial condition we computed mean firing rate and standard error of the mean (s.e.m.) within the previously defined trial epochs.

If a neuron encodes position error, then when its firing rate is plotted as a function of PE, the responses to moving targets should overlay the responses to stationary targets. Likewise, if a cell encodes saccade amplitude, then the firing rate vs. SA plots should overlap for stationary and moving targets. To test this, we plotted FR as a function of PE or SA for stationary targets and then interpolated the data to get a smooth curve. We used these FR v. PE and FR v. SA functions to predict the response to moving targets. For each moving target trial, we computed the position error and firing rate (FRM(pe)), and then looked up the firing rate for the same position error when the target was stationary (FRS(pe)). We then computed the correlation between FRM(pe) and FRS(pe). We used the same procedure to determine how much of the variance in firing rate was accounted for by SA. Based on significance of the correlation coefficient, we classified cells as being tuned for PE or SA. A similar method has been used to analyze spatial frames of reference for parietal neurons (Mullette-Gillman et al 2005).

To assess the effect of TV, we plotted recorded FRs (mean values and s.e.m.) vs. the difference between SA and PE. In addition we plotted and evaluated the behavioral correlation between the difference between SA and PE and the TV. This last procedure follows closely the analysis performed by Keller and Steen Johnsen (1990). We then related physiological data to saccade metrics by fitting piecewise linear functions to the plots of FR vs. SA-PE as well as to the plots of FR vs. TV.
To test for significant modulation of TV on the firing rates during the on-axis trials, we ran five one-way ANOVAs with firing rate as the dependent variable and TV, SA, SD, PE, or DE as the explanatory variable. One set comprised all on-axis trials, including both saccades to static and moving targets. The ANOVA was done on the firing rates of each trial epoch.

Running ANOVA over the firing rates using SA/SD or PE/DE as independent variables across all trial conditions (with saccades to static and moving targets) was not possible due to the random variability in SA and PE. To overcome this we binned the values of SA/SD and PE/DE across all trials. Then we performed two-way ANOVAs grouping the trials according to target speed and PE/DE or target speed and SA/SD.

The activity of FEF neurons can be classified as visual, visual-movement, or movement related based on whether it is more strongly associated with a visual stimulus or with a saccadic eye movement (Bruce and Goldberg, 1985). We used a visuomotor index to classify neurons as follows:

$$VMI = (V - M) / (V + M)$$

where V is the average firing rate 100 ms after the appearance of the visual stimulus and M is the average firing rate 100 ms before the saccade onset. This index ranges from –1.0 (pure movement cell) to 1.0 (pure visual cell). This analysis was performed using data from the tracking and memory saccade tasks. In each case, the firing rates were calculated using the trial condition that produced the maximum overall response, i.e. the preferred target location or saccade metric (direction and amplitude).

**Results**

**Saccades to moving targets**

We trained four macaque monkeys to perform saccades to stationary and moving targets as explained in the behavioral tasks section (Fig. 1A-D). If the saccade accurately compensates for target motion,
then saccade amplitude should include a predictive component that is proportional to target velocity (TV). By examining saccades to stationary and moving targets, we were able to dissociate saccade amplitude (SA) from position error (PE) sampled 100 ms prior to saccade onset (Fig. 2A). We used regression analysis to assess the validity of the previously reported relation between saccade amplitude, position error and target velocity (Keller & Steen Johnsen 1990; Eqn 1) for the four monkeys used in our study. This analysis used data from 69 neuronal recording sessions (60 of which resulted in the population of 96 neurons analyzed below). Position error measured 100 ms prior to saccade onset is plotted vs. saccade amplitude for 5 different target velocities (-30, -10, 0, 10, 30 deg/sec) in Fig. 2B for monkey F. The results confirm a nearly perfect linear relationship. The coefficients of Eqn 1 derived from this analysis are given in Table 1 (rows with “PE Time” of 100 ms). The fitted lines have $\beta_1$ near to but generally less than 1.0, and $\beta_2$ greater than 0.1. This indicates that the saccade plan tends to under-compensate position error and over-compensate target velocity.

The question naturally arises as to why the regression analysis was done with position error sampled at a particular time (100 ms) prior to saccade onset. To determine the sensitivity of the analysis to this time point, we repeated the analysis using position errors sampled at 100, 80, 60, 40, 20, and 0 ms before the onset of the saccade. For all six time points, the regression showed a clear linear dependence between saccade amplitude and both position error and target velocity with high correlation coefficients (Table 1 shows regression parameters for 100, 40, 20 and 0 ms). We did not observe a large variation in the correlation coefficient when using a position error taken closer to the saccade onset. In all animals $r^2$ was larger than 0.93 with the exception of monkey C. The coefficient of the target velocity term ($\beta_2$) changes in a manner consistent with a linear dependence on the time to the saccade onset, i.e. it gets smaller as the time at which position error is sampled gets closer to
saccade onset. This is expected because the difference between position error and saccade amplitude becomes smaller and, hence, less velocity compensation is required. These results are consistent with previous studies (Keller and Steen Johnsen 1990). The only difference is that our $\beta_2$ coefficients are somewhat larger, but this could be a consequence of our including saccades in all directions. However, our analysis further shows that there is nothing special about 100 ms as the time at which position error is sampled. It suggests that rather than sampling position error at a particular time and compensating for target motion at that instant, the brain may actually sample position error continuously to compute the necessary velocity compensation at any given moment. This would allow the oculomotor system some flexibility in deciding when to initiate the movement without sacrificing accuracy.

To examine more closely how target velocity is used in saccade programming, we looked at the relationship between the difference (or residual), SA-PE, and TV. This residual can be thought of as the extra amount of saccade amplitude or direction that is due to target velocity. The regression analysis shown in Fig. 2B is largely determined by the dependence of saccade amplitude on position error. The residual, SA-PE, largely removes the effect of position error and therefore provides a more robust estimate of the effect of target velocity on saccade metrics. Eqn 1 suggests that the relationship between the residual and target velocity should also be linear, and in fact a linear function accounted for at least 80% of the variance for all four monkeys when PE was sampled 100 ms before saccade onset. Again, to determine if this result was sensitive to the particular time at which position error was sampled, we iterated the analysis for time points ranging from 0 to 200 ms before saccade onset, sampling position error every 10 ms. The correlation of SA-PE($t$) vs. TV is shown in Fig. 2C as a function of $t$ (time before saccade). The influence of target velocity on SA-PE decreased substantially with time before saccade onset, but there was still a significant correlation within a few milliseconds.
before saccade onset. This again suggests that PE and TV are not sampled at a discrete point in time, but are continuously integrated into an updated estimate of saccade amplitude. This result helps to justify, the use of measures of neural activity in different time intervals between target onset and saccade onset, some of which may include activity only 50 ms prior to the saccade.

Eqn 1. can be generalized to two dimensions by replacing SA, PE and TV with 2D vectors representing the x and y components of saccade displacement, position error and target velocity, respectively (see Methods Eqn 2a,b). Then the preceding analysis can be done for off-axis target motions as well as on-axis. Specifically, linear functions can be fit independently to the x and y components of each variable. This analysis was done for trials with off-axis target motion and the results turned out to be nearly indistinguishable from those for on-axis target motion shown in Fig. 2C.

**Neuronal Responses in FEF**

We recorded 124 cells in the frontal eye fields of four monkeys. Of these cells, 96 (19 from monkey C, 16 from monkey D, 27 from monkey E and 34 from monkey F) were retained for further analysis based on criteria described in Methods. The behavioral results above confirm that target motion dissociates saccade amplitude from position error by an amount proportional to target velocity. The following analyses explore 1) the statistical significance of the effect of target velocity, retinal error (target position and direction) and saccade metrics (amplitude and direction) on firing rate, 2) neuronal sensitivity to retinal error and saccade metrics, 3) neuronal sensitivity to target velocity, and 4) the relationship between target velocity sensitivity and visual-movement index.
Statistical significance of target velocity, retinal error, and saccade metrics on firing rate

Analyses of variance (ANOVA) were run to determine the explanatory power of target velocity (TV), saccade amplitude/direction (SA/SD) and position/direction error (PE/DE) on firing rates in different trial epochs (fixation, visual, pre-saccadic and peri-saccadic) across all neurons sampled. Each explanatory variable was first considered individually (Table 2). As expected, ANOVA found few neurons with significant modulation of firing rate by any explanatory variable in the fixation interval. There is a progressive increase in the number of cells showing significant effects in the visual, pre-saccadic and peri-saccadic trial epochs, suggesting that neural signals related to TV, PE, DE, SA and SD evolved over time from the onset of the target through the execution of the movement. However, the number of significant cells was comparable across all five explanatory variables. These trends were similar for both the p<0.05 and p<0.01 significance levels. In general, the numbers of cells with significant effects ranges from 2 to 60 times the number that would be expected by chance.

Two- and three-way ANOVAs were also run using combinations of the explanatory variables. All of these analyses produced results in qualitative agreement with the one-way ANOVAs. The explanatory power of TV, SA/SD and PE/DE increased across the visual, pre-, and peri-saccadic trial epochs, but there were no clear differences between these variables. This is what one would expect if neuronal activity in FEF were coupled to target velocity compensation because, behaviorally, TV, PE/DE and SA/SD are linearly related, as shown in Fig. 2. Therefore, neural circuitry that is involved in computing SA/SD based on PE/DE and TV should be correlated with all of these variables. This appears to be the case for FEF.
**Effects of retinal error and saccade metrics on firing rate**

Figure 3 shows examples of two individual cells with average firing rate plotted against position error (PE, Fig. 3A,C) or saccade amplitude (SA, Fig. 3B,D). Firing rate was computed during the peri-saccadic time interval, which includes the 50 msec just before saccade onset. In Fig. 3A, activity prior to saccades to moving targets (colored symbols) is similar to activity when saccades are made to stationary targets (black symbols) when activity is plotted as a function of position error. However, the peak response of the neuron shifted systematically when plotted as a function of saccade amplitude (Fig. 3B). Fig. 3C,D shows the activity of a different cell whose activity was more consistent when described in terms of saccade amplitude (Fig. 3D) than position error (Fig. 3C). The cell in Fig. 3A,C could be described as encoding position error better than saccade amplitude in the sense that there was generally less variability in firing rate for a given value of position error than for a given value of saccade amplitude. The activity of the cell in Fig. 3C,D was better described by saccade amplitude as the explanatory variable.

Although position/direction error and saccade amplitude/direction are correlated, it is clear that for some cells, one accounts for more variability in firing rate than the other. There are many ways one might quantify this. We chose to use a metric for which the response to stationary targets was used to predict the response to moving targets. To do this, we first had to fit smooth functions to the data for stationary targets. These functions are shown as the solid black lines in Fig. 3. These smooth curves comprise the predicted firing rate, while the responses to moving targets on a trial-by-trial basis (not the averages plotted in Fig. 3) comprise the observed firing rates. We then computed a simple correlation between the observed and predicted rates. The results are shown as correlation coefficients (r) and their attendant significance levels (p) in each panel of Fig. 3. For the cell in Fig.
3A,B, the correlation was more robust (larger r, smaller p) for position error than for saccade amplitude. The cell in Fig. 3C,D showed the complementary result.

This analysis was carried out across the population of neurons and for 3 distinct (but overlapping) 100 msec time windows starting at a) target onset (visual), b) 100 msec before saccade onset (pre-saccadic), or c) 50 msec before saccade onset (peri-saccadic). Across the time intervals (Fig. 4), the number of cells that were significantly correlated with either SA/SD or PE/DE nearly doubled, indicating that tuning for both parameters improved during the span between target onset and saccade. During the visual interval, hardly any cells with significant tuning (filled circles in Fig. 4A,D) showed a stronger correlation with SA/SD than with PE/DE, suggesting that the cells were mainly driven by target position. But, in the pre- and peri-saccadic intervals, there emerged cells whose tuning was better correlated with SA/SD. This is consistent with the idea that SA/SD tuned cells encode a predictive component derived by extrapolating target velocity, which presumably requires some time to compute.

Across all trial epochs, the proportion of cells that were significantly correlated with either SA/SD or PE/DE varied from about one-quarter to one-half of the population. The total population of cells is the same for all epochs. Hence some cells that had no significant correlations during the visual epoch became significantly correlated during the pre- and peri-saccadic epochs. However, the significant correlations are modest, mostly in the range $r = [0.2 \ 0.4]$. Part of this is due to presumably random trial-to-trial variability in firing and the fact that the time window for averaging was only 100 msec. However, part of the variability could be due to the fact that FEF neurons are sensitive not only to target position and saccade metrics, but to target velocity (direction and speed) as well. This will be explored next.
Modulation of responses by target velocity

Do FEF neurons represent only target position and saccade metrics? If so, they might be considered as simply visual or movement neurons, leaving unclear the issue of whether FEF encodes a predictive saccade component derived by extrapolating target velocity. Evidence that FEF neurons are modulated by target velocity would help support the notion that FEF is involved in the computations underlying target velocity compensation as opposed to representing the inputs and outputs of that computation. The ANOVA results reported above provide some evidence that FEF activity is modulated by target velocity when target position and saccade metrics are included as explanatory variables. However, added support could be provided by showing that FEF activity is modulated by target velocity when retinal error and saccade metrics are constant. Figure 5 A,B show the pre-saccadic activity of an example FEF neuron as a function of position error (Fig. 5A) or saccade amplitude (Fig. 5B) for off-axis trials. Notice that the curves for different target speeds do not superimpose when plotted either as a function of PE or SA. There is clear modulation of firing rate even when PE and SA are constant across different target velocities. For example, when saccade amplitude is 10 deg, the response to a target moving at 30 deg/sec is about 4 times stronger than the response to -30 deg/sec.

To quantify the effect of target velocity across the population, we found the preferred and non-preferred speed for each cell – i.e. the speeds that produced the highest and lowest mean response during the pre-saccadic interval, averaged across all other conditions. Then, for those two velocities, we selected only trials with overlapping saccade amplitudes, i.e. the range of saccade amplitudes that was common to both velocities. We then recomputed the mean response to the preferred and non-preferred target velocity using only the trials with overlapping saccade amplitudes. The results are shown in Fig. 5C (circles). The filled circles represent cells for which the preferred – non-preferred
difference was statistically significant (unpaired t-test, p < 0.05; n = 35 cells, 36% of the population). The analysis was repeated substituting position error for saccade amplitude (Fig. 5C squares), and also for off-axis trials (Fig. 5D) with saccade direction (circles) and direction error (squares). In each case, at least 36% of the cells show a significant effect of target velocity for trials with overlapping target position or saccade metrics.

Target velocity is linearly related to the compensatory or “predictive” component of the saccade. The relationship described by Eqn 1 can be re-arranged to express the difference between saccade amplitude and position error as a function of target velocity (SA-PE = a + b * TV, or the equivalent for SD and DE). The difference, SA-PE or SD-DE, can be referred to as “the residual.” The residual is plotted for two recording sessions in Fig. 6A,D. The relationship is highly linear. It is likewise possible to plot the firing rate of the neuron during the pre-saccadic time interval as a function of the residual. When this is done, a clear relationship is seen (Fig. 6B,E). Each group of colored symbols in Fig. 6 represents a different target velocity. Hence, the relationship seen in Fig 6B,E is due to the neurons’ sensitivity to target velocity. This is confirmed by plotting firing rate vs. target velocity in Fig. 6C,F.

The scatter in the data within each speed group in Fig. 6B,E is due to variability in target position (i.e., each speed group includes a range of initial target positions). Target velocity is reliably encoded despite this variation. The encoding is not linear over the entire range of residuals, but it is nearly linear for each half of the residual axis. The finding that individual cells changed their firing more for positive than for negative target velocity (or vice-versa) suggests that the cells were direction selective. Previous work from our lab using patches of moving random dots found that about half the neurons in FEF were significantly modulated by direction of motion (Xiao et al. 2006). However, in the current study, direction selectivity is somewhat conflated with target position because the targets
changed position as they moved, and therefore the current data are not proof of direction selectivity. But some degree of directionality likely contributes to the asymmetry in response to the different target directions.

As an estimate of velocity sensitivity, we fit the data (firing rate vs. target velocity) for each cell with a piecewise linear function and calculated the correlation between the fits and the data (as shown in Fig. 6C,F). This was done separately for both the visual and pre-saccadic time intervals. The results are shown in Fig. 7. Sensitivity to target velocity was much stronger in the pre-saccadic interval than in the visual interval for both on- and off-axis trials.

**Relationship between target velocity sensitivity and visual-movement index**

FEF neurons can be indexed according to whether their response is more closely tied to the visual stimulus or to the oculomotor response. This classification is believed to reflect the flow of information through FEF. It is therefore of interest to investigate whether a measure of target velocity compensation correlates with the classification of cells as “visual”, “visual-movement”, or “movement”-related. We used Eqn 3 (Methods) to calculate a visuo-movement index (VMI) for each neuron. This index has a value of –1.0 for pure movements cells, and 1.0 for purely visual cells. For the population of neurons in this study, the mean VMI was –0.26, indicating that, for most cells, pre-saccadic firing rates were higher than firing rates during the visual trial epoch. The raw firing rates for the visual and pre-saccadic intervals are shown in Fig. 8A and it is apparent that nearly every cell was more active during the later trial epoch.

As a measure of target velocity compensation, we used the correlation between firing rate and the residual (SA-PE or SD-DE), which we will refer to as the “FR-residual correlation”. This correlation is a reflection of the fidelity with which each neuron encodes the portion of the saccade
that depends on target velocity. Fig. 6 shows how the FR-residual correlation is computed and Fig. 7 compares the correlation when it is based on visual activity versus presaccadic activity. Fig. 8B,C shows how the FR-residual correlation varies with VMI. In Fig. 8B, VMI is plotted against the FR-residual correlation where “FR” refers to activity during the visual epoch. The results are plotted for both on- and off-axis target motions and there is no significant relationship between VMI and the FR-residual correlation in either case. Fig. 8C plots the same quantities except that “FR” now refers to pre-saccadic activity. The more negative VMI’s (which correspond to stronger movement-related activity) tend weakly to correlate with the FR-residual correlation. Thus, cells whose activity is more movement-related tend also to compensate more for target velocity.

**Model for computing saccade amplitude based on the responses of velocity-modulated neurons**

The data presented above provide evidence that FEF neurons represent initial retinal target position, target velocity and saccade amplitude. Here we present a quantitative model, consistent with the data, that computes saccade amplitude from the responses of neurons that are tuned to retinal target position, but are modulated by target velocity. The principles of this model are very similar to eye position gain field models that have been used to represent head-centered target position using neurons sensitive to retinal target position and eye position (Cassanello & Ferrera, 2007a,b; Keith & Crawford 2008; Siegel, 1998; Zipser & Andersen, 1988; Xing & Andersen, 2000; Salinas & Abbott, 1995, Pouget & Sejnowski, 1997; White & Snyder, 2004).

The model comprised 101 neurons. The firing rate of each neuron was determined by the product of a retinal position sensitivity function \(R(x)\) and a target velocity sensitivity function \(G(y)\):

\[
FR(x,y) = R(x) \cdot G(y)
\]

(4)

Retinal sensitivity was modeled as a Gaussian:
(5) \[ R(x) = A \cdot \exp\left[-(x - \rho)^2 / \sigma^2\right] \]

with \( x \) representing retinal target position, \( \rho \) determining the retinal location of peak sensitivity (receptive field center), and \( \sigma \) determining the tuning width (receptive field size). These parameters varied across the population of neurons to provide coverage of the entire visual field. Examples of retinal sensitivity functions for six model neurons are shown in Fig. 9A. Target velocity sensitivity was modeled as a rectified linear function:

(6) \[ G(y) = [\alpha \cdot y + \beta]^+ \]

where \( y \) is target velocity and the (+) indicates that values below zero are made equal to zero. The parameter \( \alpha \) represents the slope of the function and varied across the population of model neurons to provide a range of velocity sensitivities. The parameter \( \beta \) represents the y-axis intercept and was fixed for all neurons. Examples of target velocity functions for six model neurons are shown in Fig. 9B.

Fig. 9C illustrates how retinal position and target velocity sensitivities interact for a single model neuron. This neuron had a large value of \( \rho \), resulting in an “open” receptive field. The amplitude of response increases with increasing target velocity. This is similar to the response of the FEF neuron shown in Fig. 5A.

Saccade amplitude is read-out as the peak of the population response. For a stationary target, the peak of the population response is identical to retinal target position. However, for a moving target, responses are modulated by target velocity and this causes the population peak to shift in the direction of the target. The magnitude of the shift can be calibrated by adjusting the slopes of the target velocity functions.

The performance of the model over a range of target positions and velocities is shown in Fig. 9D. Each point shows saccade amplitude, as determined by the peak of the population response, for a
particular target position and velocity. The different colors represent different target velocities as in Fig. 9C. The model was simulated with a delay of 500 msec. In other words, we assumed that the saccade was initiated 500 msec after target position was sampled. This is obviously unrealistic, but was done so that the magnitude of velocity compensation would be sizeable relative to the range of target positions. In this case, perfect compensation would be 0.5 • TV, or 15.0 deg for a 30 deg/sec target. Ideal compensation is shown as dashed lines in Fig. 9D. The average error of the model relative to ideal performance across all velocities and positions was 0.54 deg. Without compensation, the average error would have been 4.5 deg. For a more realistic delay of 100 msec, perfect compensation would be 0.1 • TV, with a maximum of 1.5 deg. This condition was modeled simply by reducing the slopes of the target velocity sensitivity functions for all neurons. When simulations were run for a 100 msec delay, the average error was 0.19 deg.

Discussion

To make accurate saccades to moving targets, the oculomotor system may take advantage of information about both target position and velocity. The primate frontal eye field is a region in prefrontal cortex that receives visual input and is involved in programming eye movements. We have verified behaviorally that saccades to moving targets include a compensatory component that is proportional to target velocity. FEF neurons are sensitive to target velocity and this sensitivity increases during the time between the appearance of a moving visual target and the initiation of an eye movement to foveate that target. FEF neurons are also sensitive not only to the position of a moving target, but to the metrics of the saccade required to intercept that target, and this sensitivity also evolves over time. The sensitivity to saccade metrics may therefore arise from computations that predict future target location based on target velocity. This study shows that FEF neurons encode
position/direction error, saccade amplitude/direction and target velocity, thereby establishing FEF as a likely site for the computation of future target position.

The neurons in our sample tended to have firing rates that were higher just prior to saccade onset than during the initial visual response. Hence, most neurons would be classified as visual-movement or movement related and few were purely visual. Neurons that were toward the movement end of the visual-movement spectrum tended to show a greater degree of target velocity compensation than neurons with stronger visual activity. This trend suggests that target velocity compensation emerges during the visual-motor transformation in FEF.

We developed a quantitative model to show how a population of velocity-modulated neurons can accurately encode saccade amplitude for moving targets. In the model, neurons are tuned for retinal position and their responses are multiplicatively scaled by target velocity. Scaling the responses of neurons with fixed receptive fields causes the peak of the population response to shift in the direction of target motion. The model matches several features of the FEF data. First, model neurons are tuned to retinal target position, consistent with the activity of position or direction error neurons found in the FEF (e.g. Fig. 3A). Second, model neurons are linearly modulated by target velocity, as are many FEF neurons (e.g. Fig. 6). The output of the model is saccade amplitude, consistent with the observation that some FEF neurons encode saccade amplitude or saccade direction (Fig. 3B). The performance of the model for realistic saccade latencies was, on average, within 0.2 deg of ideal target velocity compensation. The model is formally similar to eye position gain field models, except that target velocity modulates the neuronal response rather than eye position. This suggests that similar computations may underlie compensation for both target velocity as well as eye movements.
Relation to previous work

We previously reported evidence of direction and speed selectivity in FEF for moving random dot stimuli presented while monkeys maintained stable fixation (Xiao et al. 2006). In that study, 52% of the neurons were significantly tuned for direction and 40% for speed (two-way ANOVA, p<0.05). However, the stimulus was presented for 500 msec, and for different cells, the tuning emerged at different times within that epoch. The current report extends these observations by showing that there is selectivity for target velocity when monkeys performed visually guided saccades and that this selectivity was present in neural activity occurring between target onset and saccade initiation. Furthermore, velocity tuning evolved over time. Only 17% of cells were selective for target velocity in the first 100 msec after saccade target onset, while 54% were selective in the 100 msec prior to saccade initiation (one-way ANOVA, p<0.05). These results suggest that the timing of target velocity signals in FEF is appropriate for controlling saccades to moving targets. While it is true that target velocity, saccade amplitude and position error are all linearly related, and therefore difficult to disentangle, we believe that it is the cells’ sensitivity to target velocity that allows them to encode the compensatory movement. Shi et al. (1995) also examined FEF responses to moving targets and appear to have obtained results compatible with the current study, but this work has only appeared in abstract form.

Previous work in our lab has documented signals of predictive value that are present in FEF when monkeys make saccades to invisible moving targets (Barborica and Ferrera 2003; Xiao et al. 2007). The current report complements these observations by extending the notion that FEF is involved in motion extrapolation to the case of visible moving targets. It may be the case that an internal representation of invisible target motion is learned by generalizing the predictive response to
visible moving targets. In this case, we would expect that the same neurons are involved in representing both visible and invisible moving targets.

The current results from FEF are quite different than those of a similar study in the superior colliculus. Keller et al (1996) reported that during saccades to moving targets, neurons from the deeper layers of the SC encode retinal position error sampled at about 90 msec before the onset of the saccade, but do not encode saccade amplitude. This is consistent with reports that SC neurons are not selective for stimulus velocity unless monkeys are specifically trained to link motion with saccade direction (Horwitz and Newsome 2001; Horwitz et al. 2004). It appears that, although SC has reciprocal connections with FEF, it must not receive strong input from those FEF neurons that are sensitive to target velocity or that encode saccade amplitude for moving targets. The suggestion then is that FEF neurons that compensate for target motion provide input to saccade-generating circuitry via an extra-collicular pathway.

Further evidence that target velocity compensation for saccades depends on cortical pathways comes from lesion and stimulation studies. Segraves et al (1987) found that lesions of primary visual cortex impaired the ability of monkeys to make accurate saccades to moving targets. It is likely that V1 is the source of motion signals in extrastriate cortex (Movshon and Newsome 1996) that are then relayed to FEF (Schall et al. 1995). Visual area MT is likely to be part of this pathway as lesions of MT also cause deficits in saccades to moving targets (Newsome et al 1985) while microstimulation of direction columns in MT has systematic effects on saccade target velocity compensation (Groh et al. 1997). Overall, the evidence points to a V1-MT-FEF-brainstem pathway as playing a role in target velocity compensation for saccades.
Tables

**Table 1.** Results from multi-regression analysis on the on-axis saccades of the four monkeys tested.

The regression includes static and step-ramp saccades. Behavioral data from 69 recording sessions have been included in this analysis, including 9 sessions from which no neuronal data was kept for analysis. All directions have been included, not just horizontal saccades. For the first three monkeys the four rows show the regression coefficients obtained with four different values of PE taken at 0, 20, 40 and 100 ms respectively before the saccade onset.

<table>
<thead>
<tr>
<th>Animal</th>
<th>PE Time</th>
<th>N</th>
<th>α</th>
<th>β₁</th>
<th>β₂</th>
<th>r²</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>0 ms</td>
<td>2260</td>
<td>0.4156</td>
<td>0.9051</td>
<td>0.0722</td>
<td>0.8810</td>
</tr>
<tr>
<td>C</td>
<td>20 ms</td>
<td>2260</td>
<td>0.3567</td>
<td>0.9042</td>
<td>0.0879</td>
<td>0.8803</td>
</tr>
<tr>
<td>C</td>
<td>40 ms</td>
<td>2260</td>
<td>0.3403</td>
<td>0.9043</td>
<td>0.1038</td>
<td>0.8797</td>
</tr>
<tr>
<td>C</td>
<td>100 ms</td>
<td>2260</td>
<td>0.2940</td>
<td>0.9034</td>
<td>0.1536</td>
<td>0.8729</td>
</tr>
<tr>
<td>D</td>
<td>0 ms</td>
<td>1750</td>
<td>-0.1822</td>
<td>1.0326</td>
<td>0.0552</td>
<td>0.9592</td>
</tr>
<tr>
<td>D</td>
<td>20 ms</td>
<td>1750</td>
<td>-0.3675</td>
<td>1.0364</td>
<td>0.0672</td>
<td>0.9584</td>
</tr>
<tr>
<td>D</td>
<td>40 ms</td>
<td>1750</td>
<td>-0.4298</td>
<td>1.0372</td>
<td>0.0824</td>
<td>0.9578</td>
</tr>
<tr>
<td>D</td>
<td>100 ms</td>
<td>1750</td>
<td>-0.4953</td>
<td>1.0377</td>
<td>0.1402</td>
<td>0.9546</td>
</tr>
<tr>
<td>E</td>
<td>0 ms</td>
<td>2763</td>
<td>0.5110</td>
<td>0.9091</td>
<td>0.0604</td>
<td>0.9383</td>
</tr>
<tr>
<td>E</td>
<td>20 ms</td>
<td>2763</td>
<td>0.4113</td>
<td>0.9102</td>
<td>0.0763</td>
<td>0.9383</td>
</tr>
<tr>
<td>E</td>
<td>40 ms</td>
<td>2763</td>
<td>0.4053</td>
<td>0.9098</td>
<td>0.0931</td>
<td>0.9383</td>
</tr>
<tr>
<td>E</td>
<td>100 ms</td>
<td>2763</td>
<td>0.4250</td>
<td>0.9074</td>
<td>0.1462</td>
<td>0.9380</td>
</tr>
<tr>
<td>F</td>
<td>0 ms</td>
<td>7909</td>
<td>0.2872</td>
<td>0.9484</td>
<td>0.0661</td>
<td>0.9753</td>
</tr>
<tr>
<td>F</td>
<td>20 ms</td>
<td>7909</td>
<td>0.2572</td>
<td>0.9464</td>
<td>0.0821</td>
<td>0.9754</td>
</tr>
<tr>
<td>F</td>
<td>40 ms</td>
<td>7909</td>
<td>0.2722</td>
<td>0.9445</td>
<td>0.0993</td>
<td>0.9757</td>
</tr>
<tr>
<td>F</td>
<td>100 ms</td>
<td>7909</td>
<td>0.2996</td>
<td>0.9418</td>
<td>0.1550</td>
<td>0.9752</td>
</tr>
</tbody>
</table>
Table 2: Results of one-way ANOVA with explanatory variables TV, SA, PE, SD, DE on all trials (on-axis and off-axis targets). Number of cells with significant effect at p < 0.05 (or p<0.01 in parentheses). Total neurons n = 96.

<table>
<thead>
<tr>
<th>Explanatory Variable</th>
<th>Fixation</th>
<th>Visual</th>
<th>Presacc</th>
<th>Perisacc</th>
</tr>
</thead>
<tbody>
<tr>
<td>Target velocity</td>
<td>3 (0)</td>
<td>16 (11)</td>
<td>52 (38)</td>
<td>67 (61)</td>
</tr>
<tr>
<td>Position error</td>
<td>8 (1)</td>
<td>22 (15)</td>
<td>34 (27)</td>
<td>44 (36)</td>
</tr>
<tr>
<td>Direction error</td>
<td>5 (1)</td>
<td>30 (23)</td>
<td>54 (44)</td>
<td>56 (45)</td>
</tr>
<tr>
<td>Saccade amplitude</td>
<td>5 (2)</td>
<td>11 (5)</td>
<td>40 (35)</td>
<td>40 (26)</td>
</tr>
<tr>
<td>Saccade direction</td>
<td>4 (0)</td>
<td>25 (13)</td>
<td>53 (43)</td>
<td>58 (46)</td>
</tr>
</tbody>
</table>

Figure Legends

Figure 1. Tracking task used to measure responses to stationary and moving targets. A) Initial target positions for on-axis trials (black diamonds) relative to the receptive/movement field (gray patch). On any given trial, there was only one target. The line along which the targets were positioned varied depending on the RF of the neuron being recorded. B) Initial target positions for off-axis trials. Same format as A. C) Sequence of events for on-axis trials. Black squares represent fixation or saccade targets. Dashed circles represents desired eye position. Gray arrow represents target motion. Black arrow represents eye movements. D) Sequence of events for off-axis trials. Same conventions as C.

Figure 2. Metrics of saccades to moving and stationary targets for one monkey. A) Example of a step-ramp on-axis trial with purely horizontal target motion. Target horizontal position is shown in
blue. Horizontal eye position is in red. Position error (PE) and saccade amplitude (SA) are indicated as well as the times of target onset (TO), saccade onset (SO) and saccade end (SE). PE in this case is taken as the difference between target and eye position 100 ms before SO. B) Scatter plot of PE vs. SA for all on-axis trials (n = 7909) recorded from monkey F. Target velocity (TV) is color coded as indicated in the figure. The correlation coefficients (r) for each target velocity are shown in the upper left inset. C) Correlation between SA-PE(t) and TV with PE sampled at different times before saccade onset (t=0).

**Figure 3.** Example neuronal responses as a function of position or direction error and saccade amplitude or direction. A) Average firing rate around the time of the saccade as a function of position error measured 100 ms before saccade onset. Only data for on-axis trials are shown. Black symbols represent responses to stationary targets. Colored symbols represent targets moving with different speeds either toward or away from the initial fixation position according to the legend. Solid lines represent a smooth functions fit to the data (curves may have a different range than symbols because the symbols represent averages grouped according to trial type whereas the curves are constructed without grouping). Correlation coefficients (r) and attendant p-values are shown for the correlation between responses to stationary and moving targets. B) Same neuron and time interval as A, but plotted as a function of saccade amplitude. C) Data for a second neuron recorded during on-axis trials plotted as a function of direction error. D) Same data as C plotted as a function of saccade direction.

**Figure 4.** Correlation coefficients as computed in Fig. 3 across the population of neurons. A) Correlation for position error vs. correlation for saccade amplitude for on-axis trials and activity recorded during the first 100 msec after target onset. Text in the upper-left corner indicates total number of cells (n), number with significant correlation (p<0.05) for either PE or SA (filled symbols),
and number for which the correlation with PE was larger than that with SA. Open symbols are cells for which neither correlation was significant. B) Same as A, but for activity 100 msec prior to saccade onset. C) Same as A, but for activity 50 msec before to 50 msec after saccade onset. D,E,F) Same as A,B, and C, but for off-axis trials.

**Figure 5.** Modulation of pre-saccadic activity by target velocity.  A) Activity as a function of position error for five target velocities (see legend). B) Activity as a function of saccade amplitude for five target velocities. C) Response to best speed vs. worst speed for on-axis trials for all cells. For each cell, responses were limited to trials with the same range of saccade amplitudes (circles) or position errors (squares) for both speeds. Filled symbols (black or gray) represent cells with a statistically significant difference between responses to preferred and null speeds (unpaired t-test, p<0.05). Dashed line is x=y. D) Same format as C for off-axis trials. Each data point represents the response to preferred and non-preferred target velocities using only trials with overlapping saccade direction (circles) or direction error (squares). Filled symbols represents cells with significantly different responses to the preferred and non-preferred target velocities.

**Figure 6.** Two example recordings showing dependence of saccade metrics and firing rate on target velocity. A) Residual (SA-PE) vs. target velocity. Text gives correlation coefficient (r) and p-value (p). B) Dependence of firing rate on residual (SA-PE). Data were fit with a piecewise linear function. Text shows correlation (r, p) between the piecewise linear fit and the data. C) Firing rate vs. target velocity. Same conventions as B. D,E,F) Same as A,B, and C but for a second neuron/recording session.
**Figure 7.** Correlation between firing rate and residual (SA-PE or SD-DE). PE and DE were sampled at 100 msec before the onset of the saccade. A) Correlation coefficients as computed in Fig. 5 for visual vs. pre-saccadic firing rate. Filled symbols indicate that either correlation coefficient was significant (p<0.05). B) Same as A but for off-axis trials.

**Figure 8.** Visuomovement index and target velocity compensation. A) Firing rate during visual vs. pre-saccadic trial epoch. These are the rates that were used to compute the visuomotor index for each cell. B) Velocity compensation metric (FR vs. SA-PE) vs. visuomovement index. Firing rate (FR) for velocity compensation was measured during the visual trial epoch. Filled circles and solid regression line are for on-axis motion trials, open circles and dashed line are off-axis trials (hence, each cell is represented by two data points). Correlation coefficient (r) and significance level (p) are given in the legend. Note that “SA-PE” is valid for on-axis trials and should be replaced by “SD-DE” for off-axis. C) Same format at B except that the firing rate for the velocity compensation metric was taken from the pre-saccadic trial epoch.

**Figure 9.** Quantitative model for predicting saccade amplitude based on velocity-modulated neurons. A) Spatial selectivity of a subset of model neurons. B) Velocity selectivity for the same model neurons shown in A. C) Responses of a single model neuron as a function of initial retinal target position computed by multiplying its spatial and velocity sensitivities. Different colors represent different target velocities (see legend). D) Saccade amplitude predicted by the model for a range of initial target positions and velocities. The colors represent different target velocities as in C. The filled circles represent saccade amplitudes generated by the model. The dashed lines represent ideal velocity compensation.
References


A

B

C

Position error (deg)

Saccade amplitude (deg)

Correlation: SA−PE(t) vs. TV

Intervals:

- TO (Target Onset)
- SO (Saccade Onset)
- SE (Saccade End)

Correlation values:

- Monkey F: r = 0.994
- Monkey C: r = 0.989
- Monkey D: r = 0.999
- Monkey E: r = 0.998
- Monkey F: r = 0.972

Graphs show data for saccade amplitudes and position errors over time before saccade onset, with correlation coefficients indicating the strength of the relationship between saccadic eye movements and the target location.
A  

-30 deg/sec  
-10 deg/sec  
0 deg/sec  
10 deg/sec  
30 deg/sec

B  

C  

D  

r = 0.657 p = 0.000  
r = 0.199 p = 0.017  
r = 0.057 p = 0.422  
r = 0.600 p = 0.000
**A** Visual

- $n = 96$
- 25 significant
- $n(PE > SA) = 18$

**B** Pre-saccadic

- $n = 96$
- 40 significant
- $n(PE > SA) = 18$

**C** Peri-saccadic

- $n = 96$
- 52 significant
- $n(PE > SA) = 25$

**D** Visual

- $n = 92$
- 28 significant
- $n(DE > SD) = 24$

**E** Pre-saccadic

- $n = 92$
- 50 significant
- $n(DE > SD) = 29$

**F** Peri-saccadic

- $n = 92$
- 54 significant
- $n(DE > SD) = 25$
On-axis Trials

Off-axis Trials

Pref Response (sp/sec)

Non-pref Response (sp/sec)

Pref Response (sp/sec)

Saccade Amplitude (deg)

Position Error (deg)

Firing Rate (sp/sec)

total = 96

SA sig (p<0.05) = 35

PE sig (p<0.05) = 38

total = 92

SD sig (p<0.05) = 50

DE sig (p<0.05) = 38

Firing Rate (sp/sec)

Position Error (deg)

Saccade Amplitude (deg)
FR visual (sp/sec)
FR pre-saccadic (sp/sec)

A

Correlation (FR vs. SA−PE)
Visuomovement index
Visual interval

B

on-axis (r = −0.04, p = 0.68)
off-axis (r = −0.05, p = 0.61)

C

Correlation (FR vs. SA−PE)
Visuomovement index
Pre-saccadic interval

on-axis (r = −0.23, p = 0.03)
off-axis (r = −0.20, p = 0.05)
**Figure A**

![Graph 1](image1.png)

**Figure B**

![Graph 2](image2.png)

**Figure C**

![Graph 3](image3.png)

**Figure D**

Avg error = 0.54 deg.