Neuronal Variability in Orbitofrontal Cortex During Economic Decisions

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ABSTRACT

Neuroeconomic models assume that economic decisions are based on the activity of offer value cells in the orbitofrontal cortex (OFC), but testing this assertion has proven difficult. In principle, the decision made on a given trial should correlate with the stochastic fluctuations of these cells. However, this correlation, measured as a choice probability (CP), is small. Importantly, a neuron's CP reflects not only its individual contribution to the decision (termed read-out weight), but also the intensity and the structure of correlated variability across the neuronal population (termed noise correlation). A precise mathematical relation between CPs, noise correlations and read-out weights was recently derived by Haefner and colleagues (2013) for a linear decision model. In this framework, concurrent measurements of noise correlations and CPs can provide quantitative information on how a population of cells contributes to a decision. Here we examined neuronal variability in the OFC of rhesus monkeys during economic decisions. Noise correlations had similar structure but considerably lower strength compared to those typically measured in sensory areas during perceptual decisions. In contrast, variability in the activity of individual cells was high and comparable to that recorded in other cortical regions. Simulation analyses based on Haefner's equation showed that noise correlations measured in the OFC combined with a plausible read-out of offer value cells reproduced the experimental measures of CPs. In other words, the results obtained for noise correlations and those obtained for CPs taken together support the hypothesis that economic decisions are primarily based on the activity of offer value cells.
The discharges of individual neurons in cortical and subcortical areas are highly variable, but fluctuations in the activity of different cells within a given area are often correlated (Cohen and Maunsell 2009; Jeanne et al. 2013; Lee et al. 1998; Liu et al. 2013; Poort and Roelfsema 2009; Romo et al. 2003; Shadlen and Newsome 1998; Smith and Kohn 2008; Smith and Sommer 2013; Zohary et al. 1994). This phenomenon, termed noise correlation, can provide deep insights into the functions of a particular brain region (Cohen and Maunsell 2009; Jeanne et al. 2013). The analysis of noise correlations is particularly informative in the context of decision making because certain patterns of correlated variability can induce a systematic relation between the fluctuations in the activity of individual cells and the decision made by the subject. This relation is quantified as a choice probability (CP), which is the probability with which an ideal observer would correctly predict the upcoming decision based on the activity of one cell (Britten et al. 1992; Britten et al. 1996). In studies of perceptual decisions, significant CPs have historically been interpreted as evidence that a particular sensory area participates in the decision process (Britten et al. 1996; Cohen and Newsome 2009; Liu et al. 2013; Nienborg and Cumming 2014; 2006; Romo et al. 2002), although CPs can also be produced by top-down feed-back (Nienborg and Cumming 2009). Importantly, a neuron's CP reflects not only its individual contribution to the decision (termed read-out weight), but also the intensity and the structure of noise correlations within the entire network (Britten et al. 1996; Cohen and Newsome 2009; Nienborg and Cumming 2009; Shadlen and Newsome 1998). A precise mathematical relation between CPs, noise correlations and read-out weights was recently derived by Haefner and colleagues for a linear decision model (Haefner et al. 2013). Within this framework, concurrent measurements of noise correlations and CPs can provide quantitative information on how a population of cells contributes to a decision. These principles – originally developed for perceptual decisions – were applied here to the domain of economic choice.

An individual executing an economic choice assigns a subjective value to each of the available offers and then makes a decision by comparing values. This behavior is selectively disrupted by lesions of the orbitofrontal cortex (OFC) (Camille et al. 2011; Gallagher et al. 1999; Gremel and Costa 2013; Rudebeck et al. 2013). Furthermore, neural activity in this area encodes the values subjects assign to offered and chosen goods while choosing between them (Padoa-Schioppa
Current models posit that economic decisions are based on values computed in the OFC (Kable and Glimcher 2009; Padoa-Schioppa 2011; Rangel and Hare 2010; Rushworth et al. 2012). In previous work, we examined the neuronal activity of monkeys choosing between different juices. We identified three groups of neurons: offer value cells encoding the value of one of the two juices, chosen value cells encoding the value of the chosen juice, and chosen juice cells encoding the choice outcome in a binary way (Padoa-Schioppa and Assad 2006; 2008). Thus according to current views, offer value cells would provide the primary input to the decision process. Testing this hypothesis, however, has proven difficult. Furthermore, we recently found that CPs of offer value cells are substantially lower (Padoa-Schioppa 2013) than normally measured in sensory areas during perceptual decisions (Britten et al. 1996; Nienborg and Cumming 2014; 2006; Romo et al. 2002). One possible explanation for this result is that offer value cells influence decisions less than previously thought. Alternatively, CPs of offer value cells may be low because noise correlations in the OFC are low, or perhaps because noise correlations are "balanced" (i.e., independent of whether two offer value cells are associated to the same good or to different goods) (Haefner et al. 2013; Nienborg et al. 2012).

To address these issues, we examined noise correlations in the primate OFC during a juice-choice task. Noise correlations had similar structure but considerably lower strength compared to those typically reported for sensory areas. Applying Haefner's mathematical framework, we found that CPs measured in the OFC arise from the distribution of noise correlations given a plausible linear read-out of offer value cells. Specifically, the empirical mean(CP) fell between the values predicted by a uniform-pooling model and that predicted by an optimal linear decoder.

MATERIALS & METHODS

Data set

We analyzed neuronal data from two experiments previously described in detail (Padoa-Schioppa and Assad 2006; 2008). All experimental procedures adhered to the NIH Guide for the Care and Use of Laboratory Animals and were approved by the Harvard Medical School Standing Committee on Animals. In both experiments, two rhesus monkeys (one male, one female) chose between juices offered in
varying amounts. The two experiments differed only in the number of juices available in each session. In experiment 1, two juices were offered in each session (A and B). In experiment 2, three juices were offered in each session (A, B and C), two juices were offered in each trial, and trials with the three juice pairs were presented in pseudo-random order. In both experiments, an "offer type" was defined by two offers (e.g. [1A:2B]) and a "trial type" was defined by an offer type and a choice (e.g. [1A:2B,A]). The spatial contingencies (left/right) were counterbalanced across trials and different offer types were pseudo-randomly interleaved. Each offer type was usually presented ≥20 times. Neuronal recordings were performed from orbitofrontal cortex (OFC) and four electrodes were typically used in each session.

All analyses were conducted in Matlab (MathWorks, Inc). The neuronal classification was described in previous studies. Briefly, we defined seven time windows: pre-offer (0.5 s before the offer), post-offer (0.5 s after the offer), delay (0.1-1 s after the offer), pre-go (0.5 s before the go cue), reaction time (RT; from the go to the saccade onset), pre-juice (0.5 s before juice delivery) and post-juice (0.5 s after juice delivery). A "neuronal response" was defined as the activity of one cell in one time window as a function of the trial type. Task-related responses were identified by a 1-way ANOVA (factor [trial type]; p<0.001). In preliminary analyses, we tested the neuronal population against a large number of variables. Procedures of variable selection identified offer value, chosen value and chosen juice as the three variables encoded by the neuronal population (Padoa-Schioppa and Assad 2006). The encoding of these variables was categorical and generally consistent across time windows, indicating that neurons formed three distinct groups (Padoa-Schioppa 2013). A variable was said to explain a response if a linear regression of the response onto that variable had a non-zero slope (p<0.05). For each neuron, the group was identified by the variable that provided the highest sum R² across all seven time windows. Cells whose responses were not explained by any of these variables were defined as null. The data set thus included 252 offer value cells, 288 chosen value cells, 252 chosen juice cells and 692 null cells. Table 1 indicates the number of cell pairs recorded for each pair type.

Analysis of single cell variability

For each cell, we analyzed the power-law relation between the mean spike count (μ) and its standard deviation (σ). In essence, we performed the regression log(σ) = α log(μ) + β, where
each data point represented one trial type. Our analysis relied on systematic changes in $\mu$ with the
trial type and was thus carried out only on time windows in which the neuron was tuned (i.e.,
when the neuronal response was explained by the encoded variable). The analysis presupposed a
monotonic relationship between $\mu$ and $\sigma$. Thus we excluded neuronal responses that did not
present any correlation between these measures across trial types ($p > 0.1$; 10% of time windows
excluded). Also, to minimize the effects of measurement noise, we restricted the analysis to trial
types with $\geq 10$ trials (~4% of trials excluded). These criteria reduced the number of extreme
values in the analysis, but did not substantially alter the median values obtained for $\alpha$ and $\beta$
across the population.

For each neuronal response, we determined the values of $\alpha$ and $\beta$ using Deming's regression
(Glaister 2001). Simple linear regressions assume that the x-variable is measured exactly and that
only the y-variable is affected by error. In contrast, Deming's regression finds the best linear fit
for the case when both x and y are measured with error and the ratio between error in x and error
in y is known. Error in $\log(\mu)$ and $\log(\sigma)$ were derived by propagation of uncertainty from the
standard error of the mean (SEM) and the standard error of the standard deviation (SESD). We
used an approximation of SESD (Ahn and Fessler 2003) that is highly accurate (within 3%) for
$n > 10$ observations:

$$\text{SESD} \approx \frac{\sigma}{\sqrt{2(n-1)}}$$

From here, we calculated the ratio of error ($\lambda$) for each trial type in a time window.

$$\lambda = \frac{2(n-1)\mu^2}{n \sigma^2}$$

We used the mean $\lambda$ across trial types to obtain $\alpha_w$ and $\beta_w$ for each time window. Values of $\alpha_w$
and $\beta_w$ were then averaged across time windows to obtain overall values of $\alpha$ and $\beta$ for each cell.

The Fano factor and coefficient of variation were measured separately for each cell, each time
window and each trial type. Measures were then averaged across trial types. The time course of
individual-cell variability was calculated using a 200 ms sliding window with 25 ms intervals.
Analysis of noise correlations

Noise correlation ($r_{\text{noise}}$) was defined as Pearson's correlation between the trial-to-trial activity of two simultaneously recorded neurons. For each cell, trial type and time window, we computed the mean firing rate and standard deviation (SD) across trials. We z-scored the firing rate in each trial accordingly and obtained a normalized activity fluctuation. To minimize the effect of outliers, we removed trials for which either neuron's firing rate was $>3$ SD away from the mean for that trial type (Smith and Kohn 2008), although this procedure did not have a measurable impact on the results. We then computed Pearson's correlation between normalized activity fluctuations for every pair of simultaneously recorded cells.

All statistical comparisons of noise correlations across pair types based on tuning, distance and time window were done after applying Fisher's r-to-z transformation. The significance of individual noise correlations was tested by computing correlations on trial-shuffled data. This method captures the range of correlations expected by chance for a pair of cells with given activity profiles. The trial order was randomly permuted for one of the two cells in a pair and Pearson's correlation was calculated on permuted data. This procedure was repeated 1,000 times for each pair and used to generate a confidence interval. Pairs with $r_{\text{noise}}$ outside of their 95% confidence interval were considered statistically significant.

For the sliding time window analysis, we calculated $r_{\text{noise}}$ around the offer, go signal and juice delivery using 200 ms sliding time windows with 25 ms increments. For all other analyses, separate values of $r_{\text{noise}}$ were obtained for the seven time windows throughout the trial. The overall $r_{\text{noise}}$ for a cell pair was defined as the average $r_{\text{noise}}$ across time windows. All time windows were 500 ms long except RT (typically 250-400 ms). Restricting the analysis to time windows in which both neurons were tuned ($p<0.1$) did not measurably alter the effects of distance, timing, cell type, or polarity described in the main text. Similarly, repeating calculations with shorter time windows slightly reduced $r_{\text{noise}}$ but did not alter the effects of distance, timing, or cell type.

For certain analyses, we introduced the concept of neuronal polarity. In offer value cells, the encoded juice and the slope sign were always unambiguous. However, in chosen juice cells, the
design of experiment 1 made it impossible to distinguish between a cell encoding juice A with a positive slope and a cell encoding juice B with a negative slope (in both cases, the firing rate would be high/low for choices of juice A/B). We thus developed the concept of neuron polarity, which combined juice association and slope sign. The polarity was always +1 or -1. For experiment 1, the polarity was +1 when a higher firing rate of the cell corresponded to a higher probability of choosing juice A. By this convention, cells that encoded juice A with a positive slope (A+ cells) and cells that encoded juice B with a negative slope (B- cells) both had polarity = +1. In contrast, A- cells and B+ cells both had polarity = -1. The same convention held for experiment 2, except that cells encoding juice C were relabeled as encoding juice A (juice B) when paired with a cell encoding juice B (juice A). The definition of polarity applied to offer value and chosen juice cells; for chosen value cells, the polarity reduced to the sign of the encoding.

**Computing choice probabilities and neuronal sensitivity**

The methods used to calculate empirical CPs in offer value cells have been described previously (Padoa-Schioppa 2013), and were carried out here with minor alterations. Briefly, we focused on offer types in which the animal split its choices between the two juices, imposing that each juice be chosen in ≥3 trials. For each offer type, trials were divided based on the animal's choice. The two resulting distributions of firing rates were compared with a receiver operating characteristic analysis, from which we obtained the area under the curve (AUC). The CP for each cell was obtained averaging the AUC across offer types. By definition, an offer value cell presents CP>0.5 if, for given offers, the firing rate is higher in trials in which the animal chooses the juice encoded by the neuron. Thus an offer value cell with positive encoding presents CP>0.5 if its activity provides a direct contribution to the decision. Conversely, an offer value cell with negative encoding presents CP<0.5 if its activity provides a direct contribution to the decision (because the cell is less active when the animal chooses the juice encoded by the neuron). To compute an overall mean(CP) across the population, we thus rectified CPs for cells with negative encoding by defining CP as 1-AUC for these neurons. This convention allowed us to pool cells with positive and negative encoding.
We examined the relation between neuronal sensitivity (d’) and CP. This analysis focused on
offered value cells and on the post-offer time window. For each neuronal response, we computed
the standard deviation for each trial type and we averaged the result across trial types. The
neuronal sensitivity was calculated dividing the tuning slope by the average standard deviation.
Note that cells with negative encoding also have negative neuronal sensitivity. Thus to examine
the relation between CP and d’ we pooled offered value A cells and offered value B but we did not
rectify CPs.

Unless otherwise indicated, all the CPs described in this study were calculated in the 500 ms
after the offer (the same time window used to compute noise correlations). However, the
simulation analyses on the relation between CPs and noise correlations (see below) were
repeated using a shorter time window, 150-400 ms after the offer, as in a previous study (Padoa-
Schioppa 2013). As illustrated in Fig.7cd, the results obtained with the two procedures were
essentially identical.

Reconstructing choice probabilities from noise correlations

In a linear decision model, a binary decision between options X and Y is a linear read-out of a
neural population. In formulas,

\[ D = \sum_{i=1}^{n} \omega_i \phi_i \]  

(1)

where \( \phi_i \) is the activity of neuron \( i \) and \( \omega_i \) is the weight given to that neuron in the decision. By
convention, \( D > 0 \) corresponds to choosing X and \( D < 0 \) corresponds to choosing Y. Thus neurons
with \( \omega_i > 0 \) support choosing X, while those with \( \omega_i < 0 \) support choosing Y. Haefner et al (2013)
showed that the relationship between CPs, neuronal covariances and read-out weights is well
approximated by the equation

\[ CP_k = 0.5 + \frac{\sqrt{2}}{\pi} \frac{(X\omega)_k}{\sqrt{X_{kk} \omega^T X \omega}} \]  

(2)

where \( CP_k \) is the choice probability of cell \( k \), \( X \) is the covariance matrix for the network, \( X_{kk} \) is
the variance of cell \( k \), and \( \omega \) is the vector of read-out weights. Generally the covariance matrix
for a cortical circuit is not fully known. However, it is still possible to calculate CP by using the
overall trends in correlation data to construct \( X \). Using Eq.2, we conducted a series of
simulations to assess whether noise correlations measured in the OFC, taken together with a plausible read-out scheme of *offer value* cells, would induce a distribution of CPs close to that measured empirically. Specifically, we simulated CPs for a population of 10,000 *offer value* units. One half of the units had positive polarity (representing positive encoding of juice A or negative encoding of juice B) and the other half had negative polarity (representing negative encoding of juice A or positive encoding of juice B). Noise correlations used in the simulations were computed from the empirical data. Randomly sampling pairwise correlations does not generally produce a viable (positive definite) correlation matrix. In order to reconstruct CPs, we thus generated a viable and realistic correlation matrix from empirical data as follows.

First, we defined the constant $c$ as the difference in mean($r_{\text{noise}}$) for pairs of *offer value* cells with the same vs. opposite polarity based on data from the relevant time window. For "long-distance" simulations, $c$ was computed using only pairs of neurons recorded from different electrodes. For "mixed-distance" simulations, $c$ was calculated separately for same-electrode pairs ($c_{\text{same}}$) and different-electrode pairs ($c_{\text{different}}$), and the final value was defined as $c = 0.9 \ c_{\text{different}} + 0.1 \ c_{\text{same}}$. This weighting of $c_{\text{different}}$ and $c_{\text{same}}$ corresponds to a scenario in which neurons from the same electrode are representative of 10% of all cell pairs in the OFC. This scenario likely overestimates average noise correlations, since it assumes that correlations remain high for inter-neuronal distances up to 1 mm. Thus long-distance and mixed-distance simulations effectively provided a lower bound and an upper bound for mean(CP).

Second, we constructed a simplified correlation matrix $C$, where $C_{ij} = 1$ when $i = j$; $C_{ij} = c$ when $i \neq j$ and polarity($i$) = polarity($j$); and $C_{ij} = 0$ when polarity($i$) $\neq$ polarity($j$). To emulate the heterogeneity observed in empirical noise correlations, we added variability to the matrix using the method described by Hardin et al. (2013), in which the realistic correlation matrix $S$ is:

$$S_{ij} = C_{ij} + \varepsilon u_i^T u_j, \quad i \neq j; \quad \text{otherwise} \quad S_{ij} = C_{ij}$$

In this equation, $\varepsilon$ is the maximum possible noise (defined so that $0 < S_{ij} < 1$ for all $i,j$) and $u_i$ are random $M$-dimensional unit vectors. In the simulations, we used $\varepsilon = 0.9$ and $M = 100$. We thus obtained a realistic (positive definite) correlation matrix such that the variances of its elements were comparable to variances calculated from the empirical distribution of $r_{\text{noise}}$. For the uniform
condition, this random factor does not affect the outcome, as CPs depend exclusively on the mean difference in correlation between pairs in the same pool vs. competing pools (Haefner et al. 2013). For the optimal condition, changing the parameters of the correlation matrix affects CP, but if $C, M$ and $\varepsilon$ are kept constant, values of CP are consistent across simulations. To verify this point, we repeated each simulation 30 times and found that mean(CP) varied by $<10^{-3}$.

In addition to an entry in the correlation matrix, each unit in the simulation was also assigned a standard deviation, which was drawn from the empirical distribution for offer value cells. The covariance matrix was computed from the noise correlation matrix and the standard deviations. For simulations based on Fisher's optimal read-out weights (Xanthopoulos et al. 2013), each unit was also assigned a slope, indicating how much its response changed with a small shift in offer value. Each slope was always paired with the same standard deviation, as these two parameters are empirically related in our data.

In the case of uniform read-out, weights were set equal to +1 or -1 based on the polarity of each unit. In the calculation of CP, weights are normalized (see Eq.2). Thus the specific value of the uniform weight did not matter, as long as the absolute value was the same for all units. For simulations based on optimal read-out, weights were determined by Fisher's linear discriminant analysis (Xanthopoulos et al. 2013). Certain simulations included two "fictive" hysteresis units (one positive and one negative), meant to account for the effects of choice hysteresis (see below). These units were assigned weights equal to 0.161 times the total weight of the offer value pool. Their variance was defined as $\text{var}_{\text{hyst}} = p(1-p)\phi^2$, where $\phi$ is the mean firing rate modulation of offer value cells (see below). Positive and negative hysteresis units were uncorrelated with offer value units and perfectly anti-correlated with each other.

Derivation of read-out weights for hysteresis units

We previously quantified the effect of choice hysteresis with a logistic analysis (Padoa-Schioppa 2013). Briefly, we constructed a model:

\[
\text{choice } B = \frac{1}{1 + \exp(-X)}
\]

\[
X = a_0 + a_1 \log(\#B/\#A) + a_2 (\delta_{n-1,B} - \delta_{n-1,A})
\]  (3)
The variable choice B was equal to 1 if the animal chose juice B and 0 otherwise. \#A and \#B were, respectively, the quantities of juices A and B offered to the animal. The current trial was labeled as trial n. The variable \( \delta_{n-1,J} \) was equal to 1 if the animal received juice J in the previous trial and 0 otherwise. Notably, the difference \( \left( \delta_{n-1,B} - \delta_{n-1,A} \right) \) was equal to 1, -1 or 0 depending on whether the previous trial ended with receipt of juice B, juice A or otherwise (for example with receipt of the third juice in experiment 2). The logistic regression provided an estimate for \( a_0, a_1 \) and \( a_2 \). By construction, \( a_1 > 0 \). In the simplified model with \( a_2 = 0 \), \( a_1 \) was the inverse temperature and a measure of choice variability, while the indifference point was provided by \( \exp(-a_0/a_1) \). Choice hysteresis corresponded to \( a_2 > 0 \). Eq.3 may be re-written as follows:

\[
X = a_0 + a_1 \left( \log \frac{\#B}{\#A} + a_2/a_1 \left( \delta_{n-1,B} - \delta_{n-1,A} \right) \right)
\]

In the last passage, we defined \( \varepsilon \) such that \( \exp(a_2/a_1) = 1 + \varepsilon \) and we used the relation:

\[
\exp((a_2/a_1) \delta_{n-1,B}) = 1 + \delta_{n-1,B} \left( \exp((a_2/a_1)) - 1 \right) = 1 + \varepsilon \delta_{n-1,B} \tag{5}
\]

The final formulation indicates that the effect of choosing juice B (juice A) in the previous trial is equivalent to that of multiplying the quantity of juice B (juice A) by a factor \( 1 + \varepsilon = \exp(a_2/a_1) \). The logistic regression was performed for each session in the data set. Averaging across sessions, we obtained \( \text{mean}(\exp(a_2/a_1)) = 1.161 \), and thus \( \text{mean}(\varepsilon) = 0.161 \).

Consider this result in the context of a linear decision model. In the absence of hysteresis:

\[
D = \sum_{i=1}^{2K} \omega_i \phi_i \quad \text{if } D > 0 \text{ choose } A; \text{ if } D < 0 \text{ choose } B \tag{6}
\]
Here, $2k$ is the total number of offer value cells, $\omega_i$ is the read-out weight of neuron $i$ and $\phi_i$ is its firing rate modulation (i.e., the firing rate minus the intercept corresponding to zero value). Offer value cells do not reflect choice hysteresis, but they encode value in a linear way. Thus choice hysteresis can be modeled as if it affected the firing rates of offer value cells. More precisely, the effect of choosing juice B (juice A) in the previous trial is equivalent to that of multiplying the firing rate of offer value B cells (offer value A cells) by a factor $1 + \varepsilon$. In formulas:

$$D = D_A + D_B = \sum_{i=1}^{k} \omega_i^A \phi_i^A + \sum_{i=1}^{k} \omega_i^B \phi_i^B$$

$$D_A = \sum_{i=1}^{k} \omega_i^A \phi_i^A (1 + \varepsilon \delta_{n-1,A}) \tag{7}$$

$$D_B = \sum_{i=1}^{k} \omega_i^A \phi_i^A + \sum_{i=1}^{k} \omega_i^A \phi_i^A \varepsilon \delta_{n-1,A}$$

We now consider only cases in which, $\omega_i^A = 1/k$ and $\omega_i^B = -1/k$ (uniform weights). If so,

$$D_A = \sum_{i=1}^{k} \omega_i^A \phi_i^A + \varepsilon \delta_{n-1,A} \frac{1}{k} \sum_{i=1}^{k} \phi_i^A \tag{8}$$

$$D_B = \sum_{i=1}^{k} \omega_i^A \phi_i^A + \varepsilon \delta_{n-1,A} \overline{\phi_i^A}$$

The first term is the simple contribution of the first pool of neurons independent of choice hysteresis. The second term can now be interpreted as one additional unit with firing rate equal to the average firing rate of offer value A cells and read-out weight of $\varepsilon$. The same holds for $D_B$ except that the read-out weight for the additional unit has a minus sign.

Elements of the covariance matrix related to the two hysteresis units are computed as follows. First, the two hysteresis units are perfectly anti-correlated with each other. Second, since trial-by-trial fluctuations in the activity of offer value cells are independent of choice hysteresis, the correlation between the hysteresis units and other offer value cells equals zero. Third, with respect to the variance of the hysteresis units, we note that $\overline{\phi_i^A}$ in Eq.8 is an average across cells, not across trials. However, since trial-by-trial fluctuations in the activity of offer value cells are independent of choice hysteresis, $\overline{\phi_i^A}$ does not fluctuate across trials and only depends on the
mean activity of offer value cells for given offer. Therefore, if \( p \) is the proportion of trials in which the animal chooses juice J, the variance of the hysteresis unit is:

\[
\text{var}_{hyst}^J \approx p (1 - p) \left( \phi^J \right)^2
\]

For the simulations, we calculated \( \phi^J \) based on the activity of offer value cells that were tuned during the post-offer time window (\( N = 144 \)). For each cell, we identified offer types for which the animal split its choices between juices A and B (i.e., the offer types for which CPs were defined) and we averaged the spike count modulation across trials. Values of \( p \) were determined separately for each session. We thus computed \( \text{var}_{hyst} \) separately for each cell. The variance of the hysteresis units in the simulation was then computed by averaging \( \text{var}_{hyst} \) across offer value cells. Numerically, we found mean(\( \text{var}_{hyst} \)) = 3.96 (sp/s)^2.

RESULTS

The purpose of this study was to quantify noise correlations in OFC and to examine the relation between noise correlations and CPs measured in this area during economic decisions. The Results are organized as follows. In the first section, we describe the neuronal variability measured for individual cells. In the following three sections, we describe the correlation in neuronal variability for pairs of cells (a.k.a., noise correlation), its time course during a trial, and its dependence on the variables encoded by the two neurons. In the last two sections, we summarize the empirical results obtained for CPs, and we examine the relation between noise correlations and CPs in the framework of a linear decision model. The latter analysis is based on a series of computer simulations.

Firing rates of individual neurons are highly variable

In the experiments, two animals chose between different juices offered in varying quantity (Fig.1a). We recorded and analyzed the activity of 1,484 cells in seven time windows (see Materials & Methods). Preliminary analyses identified three distinct groups of cells, namely offer value cells (\( N = 252 \); Fig.1bc), chosen value cells (\( N = 288 \); Fig.1d) and chosen juice cells (\( N = \)
For each group, the encoding could be positive (increasing firing rate for increasing values) or negative (decreasing firing rate for increasing values). Cells in these three groups were collectively referred to as "tuned" cells. Other neurons, whose activity was not modulated by the offers and/or was not explained by any of the three variables, were referred to as null cells (N = 692).

We first examined the variability in the firing rate of individual neurons across trials. For each cell, we analyzed the relation between the mean spike count (μ) and its standard deviation (σ). We began with the general assumption that σ and μ are related by a power law:

\[ \sigma = \beta \cdot \mu^\alpha \]  
\[ \log(\sigma) = \alpha \log(\mu) + \log(\beta) \]

where α and β are constants. To estimate α and β, we took advantage of the fact that neuronal responses in OFC vary depending on the trial type. We computed μ and σ for each tuned cell, each time window, and each trial type. For each cell and each time window, we fit Eq.10 using Deming's regression (see Materials & Methods) and we obtained \( \alpha_w \) and \( \beta_w \) (Fig.2a). We then averaged \( \alpha_w \) and \( \beta_w \) across time windows to obtain an overall value of α and β for each cell.

Across the population we found mean(α) = 0.679 ± 0.008 (Fig.2b) and mean(β) = 1.12 ± 0.01. The measures of α and β were significantly correlated (Fig.2c) and comparable to findings in visual cortex (Dean 1981; Vogels et al. 1989).

One important metric for individual cells is provided by the relation between neuronal variability and firing rate. As apparent in Eq.10, both α and β contribute to the variability, and both parameters are only defined for tuned cells. Therefore, to quantify this relation in all cells (including null cells), we analyzed the Fano factor and the coefficient of variation in relation to the baseline firing rate (pre-offer time window). Population analyses revealed that the Fano factor varied only mildly with the baseline firing rate (Fig.2d), whereas the coefficient of variation had a strong inverse relationship with the baseline firing rate (Fig.2e).

Finally, we analyzed the time course of neuronal variability. We computed the Fano factor in 200 ms sliding time windows and averaged it across the entire population (Fig.2f). The Fano
factor dropped shortly after the offer and returned to baseline in the next 500-700 ms. It
decreased again and more modestly after the go signal, remained depressed around juice
delivery, and returned to baseline gradually in the 1 s following juice delivery. An analysis of the
coefficient of variation provided a similar picture (not shown). This result resonates with
previous reports (Churchland et al. 2010), although neuronal variability in the OFC was
previously found to drop only after juice delivery, whereas we observed the largest effect shortly
after the offer. This discrepancy presumably reflects the fact that previous work focused on
classical conditioning whereas our monkeys were engaged in a choice task.

In summary, the firing rate of individual neurons in OFC was highly variable, and this variability
was comparable to that typically measured in sensory areas.

**Noise correlations in orbitofrontal cortex are low**

Our data set included 3,439 pairs of cells recorded simultaneously. Of these, 863 pairs were
recorded from the same electrode and 2,576 pairs were recorded from different electrodes placed
at ≥1 mm distance. We computed the noise correlation ($r_{noise}$) for each of cell pair. Across the
population, $r_{noise}$ ranged from -0.59 to 0.87, with mean($r_{noise}$) = 0.019 ± 0.001 (average computed
pooling time windows; Fig.3a). Noise correlation strongly depended on inter-neuronal distance
(p<10^{-10}, 1-way ANOVA). Pairs recorded from the same electrode had mean($r_{noise}$) = 0.054 ±
0.004, while pairs at ≥1 mm distance had mean($r_{noise}$) = 0.008 ± 0.001. To look at the effects of
distance more closely, we binned pairs into five groups based on distance (Fig.3b). Pairs
recorded from the same electrode had significantly higher noise correlations than pairs at any of
the greater distances (all p<10^{-10}, Tukey-Kramer test). Noise correlations did not decrease further
at higher distances (all p>0.05, Tukey-Kramer test). Importantly, mean($r_{noise}$) was significantly
above zero in each time window, both at short distance (same electrode) and at long distance
(different electrodes; all p<10^{-3}, t test).

Notably, our measures of noise correlations were substantially smaller than those found in many
previous studies of sensory and motor areas (Fig.3a) (Gutnisky and Dragoi 2008; Kohn and
Smith 2005; Lee et al. 1998; Liu et al. 2013; Nienborg and Cumming 2006; Poort and Roelfsema
2009; Smith and Kohn 2008; Smith and Sommer 2013; Zohary et al. 1994) but see (Averbeck
and Lee 2003; Ecker et al. 2014; Ecker et al. 2010; Mitchell et al. 2009; Miura et al. 2012). We thus examined several factors that might have artificially biased our estimates of noise correlation. First, since correlated activity may have variable timing, it is possible to underestimate noise correlations if the time windows for calculations are too small. However, the time windows used here (200-500 ms) were comparable to those used in many other studies and would capture the majority of correlated activity even if the timing of spikes varied stochastically over ~100 ms (Cohen and Kohn 2011). For an additional control, we doubled the size of the time windows to 1 s and found that $r_{\text{noise}}$ increased only by 15%. Second, imperfect spike sorting can bias measurements of $r_{\text{noise}}$. Specifically, when multiple cells are recorded on the same electrode, mis-assignment of spikes can create spurious correlations. However, this type of error would only apply to cells from the same electrode, and it would tend to inflate rather than reduce $r_{\text{noise}}$. Conversely, discarding meaningful spikes or mistakenly splitting spikes from one cell into several clusters could artificially lower $r_{\text{noise}}$. However, in order to decrease $r_{\text{noise}}$ from 0.1 to the levels we observed in OFC, it would be necessary to discard >75% of spikes or to mis-identify a single neuron as more than six separate cells (Cohen and Kohn 2011), which seems implausible.

Third, firing rates in OFC are lower than in many other cortical areas (see below), and noise correlations tend to increase with firing rate (de la Rocha et al. 2007). Thus one possibility is that the discrepancy in $r_{\text{noise}}$ reflected a genuine difference between areas, but was entirely due to the properties of individual cells as opposed to the network organization. However, additional analyses cast doubts on this view. Indeed, values of $r_{\text{noise}}$ were comparable for pairs of tuned and null cells, despite the fact that null cells had lower firing rates throughout the trial. Furthermore, although the geometric mean of the firing rates was significantly related to $r_{\text{noise}}$ in our dataset, this correlation was weak (Fig.3c). Finally, our results can be compared to the predictions of a model relating noise correlation to firing rate (Cohen and Kohn 2011). The model predicts $r_{\text{noise}} > 0.15$ when both neurons have a firing rate of 1 sp/s. In our dataset, 90% of pairs had a baseline firing rate >1 sp/s for both neurons, while only 5% of pairs had $r_{\text{noise}} > 0.15$. In conclusion, differences in firing rates between OFC and sensory areas cannot fully explain the lower noise correlations found in OFC.
Time course of noise correlations

We next examined how noise correlations varied over the course of a trial. A first analysis was based on seven large time windows. A repeated-measures ANOVA revealed that the strength of noise correlations varied systematically across time windows ($p<10^{-5}$; Fig.3b). A post-hoc analysis indicated that $r_{\text{noise}}$ was significantly lower during the post-offer time window compared to the pre-offer, delay and pre-go time windows ($p<0.005$; Tukey-Kramer test). Intermediate $r_{\text{noise}}$ occurred during RT, pre-juice and post-juice time windows.

To analyze the time course of $r_{\text{noise}}$ at higher resolution, we calculated $r_{\text{noise}}$ in 200 ms sliding time windows. As illustrated in Fig.4a, the mean($r_{\text{noise}}$) dropped immediately after the offer presentation and returned to baseline levels ~700 ms after the offer. It dropped again, but to a lesser extent, after the go signal, remained depressed until juice delivery, and returned to baseline gradually in the subsequent 1 s. Interestingly, the time profile measured for the correlated variability (Fig.4a) closely resembled that measured for the variability of individual cells (Fig.2e) and was inversely related to neuronal firing rate over the course of the trial (Fig.4b). One concern might be whether transient decreases in noise correlation are caused by increases in firing rates. To address this issue, we restricted the analysis to cells whose firing rate decreased after the offer, and found that mean($r_{\text{noise}}$) dropped after the offer even for these cells. Thus the drop in $r_{\text{noise}}$ observed in Fig.4a was not simply a byproduct of higher firing rates.

We next examined the time course of noise correlations as a function of the variables encoded by the two cells. Neurons in our data set fell into four groups – offer value, chosen value, chosen juice and null. These groups led to ten pair types (Table 1). Fig.5a summarizes the values of $r_{\text{noise}}$ observed for every pair type and time window. The time course of noise correlations was roughly consistent across pair types. In almost all cases, $r_{\text{noise}}$ decreased in the post-offer time window compared to baseline, increased in the delay and pre-go time windows, decreased again after the go signal and remained stable for the rest of the trial. Pairs of chosen juice neurons (pair type 3) presented an exception to this pattern. For these pairs, $r_{\text{noise}}$ was lowest in the pre-offer time window, with a non-significant increase after the offers were presented. This time course reflects a distinct feature of chosen juice neurons. Unlike other groups of neurons, chosen juice cells show in the pre-offer time window a tail activity related to the outcome of the previous trial.
(Padoa-Schioppa 2013). Thus if two chosen juice cells have opposite juice preference, the tail activity introduces a negative correlation in the pre-offer time window. This point can be observed in Fig.5b (far right), where pairs of chosen juice cells were divided based on whether they encoded the same juice (same polarity) or different juices (opposite polarity). Note that for pairs of chosen juice cells with the same polarity, the time course across time windows is similar to that observed for other pair types.

**Noise correlations depend on the variables encoded by the two cells**

A primary goal of the study was to assess how noise correlations depend on the variables encoded by the two cells. To examine this issue, we first pooled data across time windows for each pair type (see Fig.5a) and examined the entire population. A 1-way ANOVA showed a significant effect of the pair type ($p<10^{-3}$). Mean($r_{noise}$) was generally highest when two cells encoded the same variable (pair types 1-3) or were both null (pair type 10). However, $r_{noise}$ was also relatively high for pairs of [offer value, chosen value] cells (pair type 4). We then broke down cell pairs depending on the distance between the two neurons (Fig.5c). In these conditions, the pair type had a significant effect on $r_{noise}$ when cells were from the same electrode (1-way ANOVA, $p<0.01$). For cell pairs recorded on different electrodes, there was no significant effect of pair type (1-way ANOVA, $p=0.7$). This finding suggests that the systematic pattern seen in Fig.5a was influenced by the spatial distribution of cells. Indeed, the proportion of pairs found on the same electrode was about twice as high for pair types 1-4 and pair type 10 than it was for pair types 6-9 (see Table 1), leading to greater mean($r_{noise}$) in these pair types.

We further analyzed noise correlations between cells in the same group (offer value, chosen value, chosen juice). Specifically, we examined how $r_{noise}$ depended on whether the two cells encoded the same juice or different juices, and how $r_{noise}$ depended on the slope signs (positive or negative encoding). For offer value cells, the encoded juice and the slope sign were always unambiguous. For chosen juice cells, the design of experiment 1 made it impossible to distinguish between a cell encoding juice A with a positive slope and a cell encoding juice B with a negative slope (in both cases, the firing rate would be high/low for choices of juice A/B). We thus developed the concept of neuron polarity, which combined juice association and slope sign (see Materials & Methods). In essence, two cells had the same/opposite polarity if they
"supported" the same/opposite decision. Our analyses showed that noise correlations were generally higher when two cells in the same group had the same polarity (Fig.5b, Fig.6ab). This pattern could be observed in both pairs from the same electrode and pairs from different electrodes (same electrode, p<10^{-4}; different electrode, p<0.003; separate two-way ANOVAs with factors [pair type x polarity]).

In the most granular analysis, we divided pairs of offer value cells in eight pools depending on whether the cells were recorded from the same or different electrodes, on whether the cells encoded the same juice or different juices, and on whether the sign of the encoding (positive or negative) was the same or different (Fig.6cd). Although there were no statistical differences between groups (t test, all p > 0.05), it is interesting to note that noise correlations were highest when the two cells encoded the same juice with the same sign and progressively lower when the two cells encoded different juices with opposite signs, different juices with the same sign, and the same juice with opposite signs.

When two offer value cells encoded the same variable (same juice, same sign) and were recorded from the same electrode, mean(r_{noise}) was comparable to values seen in many sensory areas (Cohen and Kohn 2011). However, unlike neurons in sensory regions, offer value cells did not appear to cluster based on the encoded variable. Such a clustering would make it more likely to encounter pairs of offer value cells encoding the same variable (same juice, same sign) when two neurons are recorded from the same electrode compared to when two neurons are recorded ≥1 mm apart. In contrast, considering all pairs of offer value cells, 15/40 (38%) encoded the same variable when the two neurons were recorded from the same electrode, while 26/73 (34%) encoded the same variable when the two neurons were recorded from different electrodes (Fig.6cd).

We do not know how sharply r_{noise} decays with distance, but it appears clear that the decay fully occurs within 1 mm (Fig.3b). Since the area of OFC examined in our studies is relatively large (10-20 mm² of cortex), most pairs of offer value cells are ≥1 mm apart. Hence, the results shown in Fig.6d likely represent the typical r_{noise} for the majority of offer value cell pairs. Among these pairs, mean(r_{noise}) was highest when neurons encoded the same juice with the same sign. This gives rise to the difference in juice polarity seen in Fig.6ab and is particularly important for the
remainder of the paper. If noise correlations within and between pools of *offer value* cells were balanced, stochastic fluctuations in different pools of neurons would be equal on average and their effects onto the decision would cancel. As a consequence, CPs would be at chance (Haefner et al. 2013; Nienborg et al. 2012). Thus the extent to which CPs of *offer value* cells differ from chance level is tightly related to the differences between the values shown in Fig. 6d.

*Choice probabilities in orbitofrontal cortex*

Current models posit that economic decisions are based on values computed in the OFC. In other words, *offer value* cells would provide the primary input to the decision. Consider a neuron that contributes to a decision process. In principle, stochastic fluctuations in the activity of the cell might be correlated with the decision made on any given trial. This correlation is quantified as a choice probability (CP), which is essentially the probability with which an ideal observer would infer the decision outcome based only on the activity of the cell (Britten et al. 1996). At chance, CP = 0.5 and by convention CP > 0.5 (CP < 0.5) for neurons with positive (negative) encoding. We thus examined CP for *offer value* cells. To obtain an overall estimate for the population, we pooled neurons associated with the two juices (A and B) and we rectified the CP of *offer value* cells with negative encoding (see Materials & Methods). The distribution of CPs measured in the 500 ms after the offer was broad, with mean(CP) = 0.513 ± 0.007 (Fig. 7a). This value was higher than, but not statistically different from 0.5 (p = 0.08; t test). Importantly, CPs may be partly or fully explained by post-decision feed-back. In principle, feed-forward and feed-back components of CPs can be disentangled based on a precise estimate of the decision time, which can be obtained in perceptual decisions using dynamic stimuli (Nienborg and Cumming 2009). However, economic decisions are not equally amenable to this approach because "stimuli" (i.e., offers) are entirely and unambiguously revealed as soon as they appear on the monitor.

Importantly, when we quantified CPs focusing on an earlier and shorter time window (150-400 ms after the offer, as in a previous study (Padoa-Schioppa 2013)), we obtained a measure that was smaller but still >0.5 (mean(CP) = 0.507 ± 0.007).

All *offer value* cells associated to a given juice carry the same signal (they encode the same variable). But from a decoding perspective, it would make sense if neurons with higher signal-to-noise ratio (higher neuronal sensitivity) had greater influence on the decision (higher CP).
Indeed, a correlation between CP and neuronal sensitivity has been observed in sensory areas during perceptual decisions (Britten et al. 1996; Liu et al. 2013). We thus examined the relation between the CP and the neuronal sensitivity of individual cells across the population (Fig. 7b).

For each *offer value* cell, the neuronal sensitivity was calculated dividing the tuning slope by the average standard deviation. In this analysis, we pooled cells associated with the two juices (A and B), but we did not rectify cells with negative encoding (neuronal sensitivity < 0). CP and neuronal sensitivity were significantly correlated ($r = 0.20$, $p<0.003$, Spearman rank correlation).

We further quantified the relation between CP and sensitivity with a linear fit ($y = a_0 + a_1 x$; Fig. 7b, red line), which provided a linear term significantly greater than zero ($a_1 = 0.14$; 95% confidence interval = [0.06, 0.21]). To assess distortions from linearity, we also performed a fit using a third order polynomial ($y = a_0 + a_1 x + a_2 x^2 + a_3 x^3$; Fig. 7b, blue line). We found that terms $a_0$ and $a_1$ were significantly greater than zero (95% confidence interval) while terms $a_2$ and $a_3$ were statistically indistinguishable from zero (95% confidence interval). For a control, we repeated these analyses based on polarity (i.e., separating neurons associated with the two juices) and we obtained similar results. These analyses essentially fulfill the optimality test of Haefner et al (2013). The results indicate that the read-out of *offer value* cells does not differ significantly from an optimal scheme.

As previously noted (Padoa-Schioppa 2013), mean(CP) measured for *offer value* cells was substantially lower than the equivalent measure obtained for neurons in the middle temporal (MT) area during perceptual decisions (Britten et al. 1996; Cohen and Newsome 2009). At the same time, noise correlations between pairs of *offer value* cells were 5-10 times smaller than those measured in area MT under comparable conditions (Fig. 6cd). Importantly, a precise mathematical relation links noise correlations, CPs and the read-out weights of individual cells in a population. Within this computational framework, concurrent measures of noise correlations and CPs gave us the opportunity to investigate quantitatively the contribution of *offer value* cells to economic decisions.

*Reconstructing choice probabilities from noise correlations*

Using Haefner's equation (Eq. 2), we conducted a series of simulations to assess whether noise correlations measured in the OFC, taken together with a plausible read-out scheme of *offer value* cells...
cells, would induce a distribution of CPs close to that measured empirically. Specifically, we simulated CPs for a population of 10,000 \textit{offer value} units. One half of the units had positive polarity (representing positive encoding of juice A or negative encoding of juice B) and the other half had negative polarity (representing negative encoding of juice A or positive encoding of juice B). Noise correlations used in the simulations were computed from the empirical distributions measured for pairs of \textit{offer value} cells during the post-offer time window (see Materials & Methods). We examined several read-out schemes (see below). For each scheme, we considered two noise correlation matrices, referred to as "long-distance" and "mixed-distance", which effectively provided a lower bound and an upper bound for mean(CP) (see Materials & Methods).

Fig.7c summarizes the results of six simulations. First, we considered the simple case in which all units have equal magnitude weights (all $\omega_i = \pm 1$). CPs obtained from these simulations (long-distance mean(CP) = 0.528; mixed-distance mean(CP) = 0.542) were clearly above the empirical measure. Importantly, these simulations ignored a known source of choice variability, namely choice hysteresis (Padoa-Schioppa 2013). In essence, when two offers have similar values, monkeys were mildly biased towards the juice they chose in the previous trial. Choice hysteresis was quantified using a logistic analysis and its effect was equivalent to multiplying the quantity of the previously chosen juice by 1.161. Most importantly, choice hysteresis was not reflected in the activity of \textit{offer value} cells (Padoa-Schioppa 2013) and could thus be interpreted as an independent input to the decision. To account for choice hysteresis in the simulation, we incorporated two "fictive" units, one positive and one negative, corresponding to a previous choice of juice A or juice B, respectively. The relative weight of the two hysteresis units was derived mathematically starting from the estimate obtained from the logistic analysis, and was equal to $\pm 0.161$ times the cumulative weight of \textit{offer value} units (see Materials & Methods). CPs obtained from these simulations (long-distance mean(CP) = 0.519; mixed-distance mean(CP) = 0.534; Fig.7c) were closer to, but still above, the empirical measure.

Imposing uniform read-out weights may be overly simplistic, since the brain could certainly take advantage of the heterogeneity in neuronal responses encoding a given offer value (Ecker et al. 2011). Indeed, the linear relation between CP and neuronal sensitivity across the population (Fig.7b) suggests that the read-out of \textit{offer value} cells is close to optimal (Haefner et al. 2013).
Thus to complement our simulation analyses, we calculated the mean(CP) for a population of
offer value units under the assumption of an optimal linear read-out. Optimal read-out weights
were computed using Fisher’s linear discriminant analysis, which finds the set of weights that
best separates two conditions – in this case, choice A versus choice B. These weights took into
account the slope of the encoding measured for each neuron, as well as the response covariance
measured across neurons. We thus computed the optimal read-out weights for the population of
offer value cells. CPs obtained from these simulations (long-distance mean(CP) = 0.502; mixed-
distance mean(CP) = 0.502; Fig.7c) were essentially at chance level and well below the empirical
measure.

We repeated these analyses using a shorter and earlier time window (150-400ms after offer
onset) (Fig.7d). Noise correlations, empirical CPs and simulated CPs were all lower in this time
window. Most importantly, the empirical measure of mean(CP) was very close to that obtained
from the simulation using uniform weights and accounting for choice hysteresis (empirical =
0.507, simulated = 0.506).

To summarize, the CPs of offer value cells were lower than those typically measured in sensory
areas during perceptual decisions. However, CPs were quantitatively as expected given the
structure and the strength of noise correlations measured for pairs of offer value cells in OFC.
The results obtained focusing on an earlier and shorter time window strengthen this conclusion.

DISCUSSION

Noise correlations in orbitofrontal cortex are low

Noise correlations in the OFC were on the order of 0.01. This measure is substantially lower than
those reported for many cortical regions. Specifically, work in V1 (Gutnisky and Dragoi 2008;
Kohn and Smith 2005; Nienborg and Cumming 2006) but see (Ecker et al. 2010), V2 (Nienborg
and Cumming 2006), MT (Cohen and Newsome 2009; Zohary et al. 1994), somatosensory area
S2 (Romo et al. 2003) and primary motor cortex (Lee et al. 1998) have found noise correlations
ranging 0.1-0.25. Studies in V4 (Cohen and Maunsell 2009; Mitchell et al. 2009) have reported
intermediate levels of correlation \( r_{\text{noise}} \approx 0.03-0.07 \), which are closer to but still slightly higher than those observed here for OFC. In lateral prefrontal cortex, noise correlations were smaller, but about twice the size of those found here (Constantinidis and Goldman-Rakic 2002). Importantly, many of these measures were obtained in awake behaving monkeys (Cohen and Newsome 2009; Gutnisky and Dragoi 2008; Nienborg and Cumming 2014; 2006; Poort and Roelfsema 2009; Zohary et al. 1994). Notable exceptions are the studies of Ecker and colleagues, who recently reported measures of \( r_{\text{noise}} \) in V1 comparable to those described here, and raised the hypothesis that high noise correlations measured in earlier studies may reflect factors such as spatial attention or task strategy (Ecker et al. 2014; Ecker et al. 2010) see also (Gawne et al. 1996; Gawne and Richmond 1993). In this respect, it is worth emphasizing that our animals were actively engaged in a choice task. Moreover, since neurons in the OFC are not spatially tuned or associated with specific actions, factors such as spatial attention, action planning or minor stimulus variability are unlikely to affect \( r_{\text{noise}} \). Thus noise correlations in the OFC seem genuinely lower than those measured in sensory areas under comparable conditions. How can we explain this discrepancy?

Possibly important is the fact that our offers were always unequivocally defined. In contrast, studies of perceptual decisions often used stochastic stimuli (Liu et al. 2013; Nienborg and Cumming 2006; Poort and Roelfsema 2009; Zohary et al. 1994). In principle, specific realizations of a stochastic stimulus could elicit systematic neuronal responses (Bair and Koch 1996), which could result in over-estimates of noise correlations (because noise correlations could partly reflect signal correlations). Independently of this consideration, at least two features distinguish OFC structurally and functionally from sensory areas. First, OFC lacks a clear position in a feed-forward processing stream and, instead, integrates converging inputs from multiple sensory and limbic regions (Ongur and Price 2000). In contrast, sensory systems typically present hierarchical processing streams and are, by definition, predominantly unimodal. Theoretical analysis has suggested that correlations arise naturally across sequential stages of feed-forward processing (Rosenbaum et al. 2010) and that hierarchical organization in itself may contribute to \( r_{\text{noise}} \) in many sensory areas. Consistent with this view, noise correlations in perirhinal cortex (Erickson et al. 2000) and in the supplemental motor area (SMA) (Averbeck and Lee 2003), both of which lack a clear hierarchical position, are low and comparable to those
measured here. Second, aside from hierarchy, it remains unclear whether OFC has any topographic organization. As noted above, pairs of offer value cells encoding the same variable (same juice, same sign) were equally prevalent at short and long distances (Fig. 6cd), indicating that any clustering is loose at best. At the same time, significant CPs are almost exclusively observed when the choice-relevant variable is topographically organized within a cortical area (Nienborg and Cumming 2014), suggesting that the circuit organization associated with a topographic map is a necessary condition to observe the patterns of noise correlation that induce high CPs. Interestingly, the rodent anterior piriform cortex (Miura et al. 2012), which also lacks any clear topography, is one of the few areas where $r_{\text{noise}}$ is comparable to that measured here. Conversely, noise correlations in SMA – an area with a clear topography – are low (Averbeck and Lee 2003), indicating that topography is necessary but not sufficient to induce high noise correlations.

Despite differences in strength, noise correlations measured in the OFC presented several traits that clearly resembled those observed in other brain regions. First, $r_{\text{noise}}$ was strongly affected by distance, falling off within 1 mm. A similar effect of distance was found in other cortical areas, although the decay was less sharp in V1 (Smith and Kohn 2008) and V4 (Smith and Sommer 2013). Second, as observed in sensory areas (Cohen and Newsome 2008; Liu et al. 2013; Smith and Kohn 2008), $r_{\text{noise}}$ in OFC was highest when two neurons had similar tuning (i.e., when they encoded the same juice with the same sign). Notably, it is the "differential" component of noise correlations that ultimately limits the information encoded by a neuronal population (Abbott and Dayan 1999; Moreno-Bote et al. 2014; Shadlen et al. 1996). Third, the time course of noise correlations within a trial – specifically the fact that $r_{\text{noise}}$ drops immediately after presentation of a relevant stimulus – is a common phenomenon (Carnevale et al. 2012; Churchland et al. 2010; Kohn and Smith 2005). In conclusion, it appears that noise correlations measured in OFC differ in strength, but not in structure from those measured in other brain regions.

*Noise correlations, choice probabilities and the read-out of offer value cells*

Current neuroeconomic models assume that decisions are based on subjective values computed in the OFC (Kable and Glimcher 2009; Padoa-Schioppa 2011; Rangel and Hare 2010; Rushworth et al. 2012). In the formalism of a linear decision model (Eq. 1), this means that the
normalized read-out weights of offer value cells should add to 1. Taking into account choice hysteresis, which provides a smaller but independent contribution to the decision, this proposition can be amended stating that normalized read-out weights of each offer value pool should add to ~0.839. To test this hypothesis, one would ideally measure read-out weights directly, but this is not practically feasible. However, read-out weights are quantitatively related to noise correlations and CPs, both of which can be measured. Based on this theoretical framework, we showed that the distribution of CPs measured for offer value cells can be reconstructed from concurrent measures of noise correlations assuming a plausible scheme of read-out weights. More specifically, the empirical measure for mean(CP) fell between the values obtained with a uniform and with an optimal read-out.

Our results provide a plausibility argument in favor of the hypothesis that offer value cells provide the primary input to economic decisions. Importantly, additional factors most likely affect the decision process. For example, previous results indicated that decisions are partly biased by the initial state of the neural assembly, reflected in the "predictive activity" of chosen juice cells (Padoa-Schioppa 2013). This predictive activity is largely a tail activity from the previous trial and is thus related to the behavioral phenomenon of choice hysteresis. Thus the "fictive" units in our simulations accounted for this source of choice variability. Conversely, our simulations did not include other possible sources of variability such as residual fluctuations in the initial state of the decision circuit, trial-by-trial fluctuations in the relative value of the goods (Padoa-Schioppa 2013) or downstream noise (Haefner et al. 2013). Most importantly, since any of those factors would reduce CPs, simulation analyses that accounted for any of them would effectively strengthen our current conclusions. The extent and implications of non-linearities in the decoder remain to be examined. Exploring the fine structure and the mechanisms of the neural circuit that generates value-based decisions is a major goal for future research.
FIGURE LEGENDS

Figure 1. Behavioral task and cell groups. a. Juice choice task. At the beginning of each trial, the animal fixated on the center of a screen. Two sets of colored squares, representing the two offers, appeared after 0.5 s. For each offer, the color indicated the juice identity and the number of squares indicated the juice quantity. The animal maintained center fixation for a randomly variable delay (1-2 s), after which the fixation point disappeared and two saccade targets appeared by the offers (go cue). The animal indicated its choice with a saccade and maintained peripheral fixation for 0.75 s before juice delivery. b. Neuron encoding the offer value A. The x-axis represents different offer types ranked by the ratio #B: #A. Black symbols represent the percent of "B" choices. Red symbols represent the neuronal firing rate (diamonds and circles indicate, respectively, choices of juice A and juice B). To highlight the variability in firing rates, thinner error bars here indicate the SD and thicker error bars indicate the SEM. c. Neuron encoding the offer value B. d. Neuron encoding the chosen value. e. Neuron encoding the chosen juice. All conventions in panels cde are as in panel b.

Figure 2. Neuronal variability in the OFC. a. Relation between mean firing rate (μ) and variance (σ) for one representative offer value cell (post-offer time window). Data are plotted in log scale and each data point represents one trial type. The line is obtained from Deming's regression. For this response, αw = 1.0 and βw = -0.99. For each tuned cell (763 cells total), α and β were obtained averaging αw and βw across time windows. b. Distribution of α. Across the population, mean(α) = 0.679 ± 0.008 (± SEM). c. Relation between α and β. Each data point represents one neuron and the two quantities are strongly anti-correlated. One outlier (0.1%) fell outside the range shown. d. Relation between the Fano factor and the baseline activity. Baseline activity was defined as the firing rate in the pre-offer time window. Each data point represents one neuron. Across the population, mean(Fano factor) = 1.8. e. Relation between coefficient of variation (cv) and baseline activity. The two quantities are strongly anti-correlated. Across the population, mean(cv) = 1.0. f. Time course of neuronal variability. Dark lines and shaded regions represent, respectively, the mean Fano factor and the corresponding SEM (in sp/s). The Fano factor was calculated in 200 ms sliding windows. Neuronal variability dropped sharply shortly after the offer onset; it returned to the initial levels 500-700 ms after the offer; it decreased again and
more mildly following the go signal and remained depressed until the trial end. The coefficient of variation presented a similar time course (not shown).

**Figure 3.** Noise correlation ($r_{\text{noise}}$) between pairs of neurons in OFC. **a.** Overall distribution of $r_{\text{noise}}$. In this plot, we pooled all cell pairs and all time windows. Cell pairs with significant $r_{\text{noise}}$ are indicated in dark. The $r_{\text{noise}}$ differed significantly from zero for 1,592/3,439 (46%) cell pairs ($p<0.05$; bootstrap analysis; see Materials & Methods). The black triangle below the x-axis marks the population average. For comparison, we indicate measures of noise correlation previously reported for MT (Zohary et al. 1994), parietal areas 2/5 (Lee et al. 1998), M1 (Lee et al. 1998), V4 (Mitchell et al. 2009) and V1. For V1, the higher data point shown here is from (Poort and Roelfsema 2009) and comparable measures were reported in (Gutnisky and Dragoi 2008; Kohn and Smith 2005; Nienborg and Cumming 2006; Smith and Kohn 2008); the lower data point is from (Ecker et al. 2010) and a comparable measure was reported in (Ecker et al. 2014). **b.** Values of $r_{\text{noise}}$ grouped by inter-electrode distance. The x-axis represents different time windows (see Materials & Methods). For all time windows, $r_{\text{noise}}$ was significantly higher when the two cells were recorded from the same electrode. Notably, $r_{\text{noise}}$ did not decrease beyond values measured at 1 mm distance. Error bars indicate SEM. **c.** Noise correlation as a function of the geometric mean of baseline firing rates. The geometric mean averaged across the population was $5.85 \pm 0.09$ sp/s (mean ± SEM). Across the population, noise correlations were weakly but significantly correlated with the geometric mean of baseline firing rates ($r = 0.05$, $p<0.005$; Spearman rank correlation). **d.** Noise correlation as a function of the geometric mean of standard deviations. Population mean ± SEM = $4.20 \pm 0.04$ sp/s. **e.** Noise correlation as a function of the geometric mean of the coefficients of variation. Population mean ± SEM = $1.048 \pm 0.009$. Data for panels cde were taken from the pre-offer time window. Note that values of $r_{\text{noise}}$ for individual cell pairs fluctuate throughout the course of the trial and are negatively correlated with firing rate across time windows (see Fig.4).

**Figure 4.** Time course of noise correlation and firing rate. **a.** Noise correlation. Values of $r_{\text{noise}}$ were computed in 200 ms time windows slid by 25 ms intervals around offer presentation (left panel), go signal (middle panel) and juice delivery (right panel). In the figure, each data point is placed on the x-axis in the center of the corresponding time window. Dark lines and shaded regions indicate mean($r_{\text{noise}}$) and SEM, respectively. Noise correlations dropped sharply and
transiently after the offer. This effect, most evident when neurons were recorded from the same electrode, was also observed when neurons were recorded from different electrodes. A second and more modest decrease in $r_{\text{noise}}$ occurred after the go signal. This second drop was pronounced only in same-electrode pairs. Noise correlations gradually returned to baseline levels after juice delivery. The figure includes all cell pairs in the data set (863 same-electrode pairs, dark gray; 2,576 different-electrode pairs, light gray). b. Firing rate. The figure illustrates the firing rate averaged across all tuned cells (763 cells). All conventions as in panel a.

**Figure 5.** Noise correlations for different pair types. a. Mean $r_{\text{noise}}$ recorded for ten pair types and seven time windows. The number of pairs for each pair type is indicated in Table 1 and colors indicate different time windows. Pooling time windows, $r_{\text{noise}}$ varied significantly across pair type ($p<10^{-3}$, 1-way ANOVA). Post-hoc tests found several significant differences in $r_{\text{noise}}$: type 1 > types 6-10, type 2 > types 7-9, type 3 > types 6-8, type 4 > types 7-9, and type 10 > types 7-8 (all $p<0.05$, Tukey’s LSD). We also observed consistent trends across time windows. Starting from the pre-offer time window (baseline), $r_{\text{noise}}$ decreased in the post-offer time window. It then increased in the delay and pre-go time windows compared to the post-offer. It decreased again in the RT time window and remained roughly stable for the rest of the trial. These trends were observed for all pair types (with the exception of pair type 10 in the pre-offer time window; see main text.) b. Mean $r_{\text{noise}}$ for pair types 1-3, divided by juice polarity (see Materials & Methods). Pairs of neurons with the same polarity are on the left of each panel, while those with opposite polarities are on the right. For chosen juice pairs with opposite polarity, residual activity from the previous trial leads to negative noise correlations in the pre-offer time window. c. Mean $r_{\text{noise}}$ by pair type. Data from different time windows are averaged separately for cell pairs recorded from the same electrode (top) and from different electrodes (bottom). All error bars indicate SEM.

**Figure 6.** Noise correlations depend on the polarity of the two cells. Top (bottom) panels refer to cell pairs from the same electrode (different electrodes). ab. Noise correlations between cells in the same group (offer value, chosen value and chosen juice). Black (white) bars refer to pairs of cells with the same (opposite) polarity. For each cell group, $r_{\text{noise}}$ was higher when the two neurons had the same polarity. This observation was true both at short and long distance. cd. Noise correlations between pairs of offer value cells. Pairs were divided in 8 pools depending on whether the two cells were recorded from the same or different electrode (top, bottom), on
whether the two neurons encoded the same juice or different juices (left, right), and on whether
the sign of the encoding for the two cells was the same or different (dark gray, light gray). In
general, $r_{noise}$ was highest when two cells encoded the same juice with the same sign. Values of
$r_{noise}$ show the average across all time windows. Numbers in parentheses indicate the number of
neurons in each pool. All error bars indicate SEM.

**Figure 7.** Choice probabilities and noise correlations. **a.** Empirical distribution of CPs measured
in the 500 ms after offer onset (N = 229 cells). Cells with positive and negative encoding were
pooled (see Materials & Methods). Across the population, mean(CP) = 0.513 ± 0.007 (± SEM).

**b.** Relation between choice probability and neuronal sensitivity. Each data point in the figure
represents one *offer value* cell. For each neuron, the neuronal sensitivity was calculated dividing
the tuning slope by the average standard deviation. Cells encoding the two juices (A and B) were
pooled, but cells with a negative encoding were not rectified here (sensitivity < 0). Color lines
indicate the result of a linear fit ($a_0 + a_1 x$; red line) and the result of a fit based on a third-order
polynomial ($a_0 + a_1 x + a_2 x^2 + a_3 x^3$; blue line). In the latter, terms $a_0$ and $a_1$ were significantly
>0, while terms $a_2$ and $a_3$ were indistinguishable from 0, indicating that the read-out of *offer
value* cells was close to optimal (Haefner et al. 2013). Two outliers (gray dots) were not included
in the regressions, but adding them to the data set did not alter any of the significance results. **cd.**

Reconstructing choice probabilities from noise correlations. Each data point represents the
mean(CP) obtained empirically or from a simulation (see Results). The error bars shown for the
empirical measure indicate SEM. For each read-out scheme, long-distance and mixed-distance
simulations provided, respectively, a lower bound and an upper bound for mean(CP) (see
Materials & Methods). Empirical and simulated CP were calculated during the post-offer time
window (**c**) and the window 150-400ms following offer onset (**d**).
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Table 1. Number of simultaneously recorded cell pairs. Pair types are labeled as follows: (1) [offer value, offer value]; (2) [chosen value, chosen value]; (3) [chosen juice, chosen juice]; (4) [offer value, chosen value]; (5) [offer value, chosen juice]; (6) [chosen value, chosen juice]; (7) [offer value, null]; (8) [chosen value, null]; (9) [chosen juice, null]; (10) [null, null]. See also Fig.5a. For pair types 1-3, cell pairs are further broken down depending on whether the two neurons had the same polarity or different polarity (see main text).


Rushworth MF, Kolling N, Sallet J, and Mars RB. Valuation and decision-making in frontal cortex: one or many serial or parallel systems? *Curr Opin Neurobiol* 2012.


Figure 2

(a) $y = 1.0x - 0.99$

(b) Number of Cells

(c) beta

(d) Fano Factor

(e) Coefficient of Variation

(f) Fano Factor

Offer Go Juice
Figure 3

(a) Histogram showing the distribution of noise correlation with percent of pairs. The histogram includes data from 3,439 pairs.

(b) Graphs showing noise correlation across different conditions. The conditions include 'pre-offer', 'post-offer', 'delay', 'pre-go', 'RT', 'pre-juce', and 'post-juce'. The data is divided into three groups: same electrode (n = 853), 1-2 mm (n = 909), and 2-3 mm (n = 739), with > 3 mm (n = 928).

(c) Scatter plot showing the relationship between noise correlation and preoffer firing rate. The correlation coefficient (r) is 0.05 and the p-value is 0.004.

(d) Scatter plot showing the relationship between noise correlation and standard deviation. The correlation coefficient (r) is 0.068 and the p-value is 10^-4.

(e) Scatter plot showing the relationship between noise correlation and coefficient of variation. The correlation coefficient (r) is -0.019 and the p-value is 0.26.
Figure 4

(a) Noise Correlation

(b) Firing Rate (sp/s)

- Offer
- Go
- Juice

- Same electrode
- Different electrodes
Figure 5

(a) Noise Correlation

(b) Offer Value, Chosen Value, Chosen Juice vs. Polarity

(c) Same electrode vs. Different electrodes
Figure 6

(a) **Same Electrode**
- Noise Correlation
- Same polarity vs. opposite polarity
- Offer Value vs. Chosen Value vs. Chosen Juice

(b) **Different Electrodes**
- Noise Correlation
- Offer Value vs. Chosen Value vs. Chosen Juice

(c) **Same Juice**
- Noise Correlation
- Same sign vs. opposite sign
- Offer Value Pairs

(d) **Different Juice**
- Noise Correlation
- Offer Value Pairs
Figure 7

(a) Distribution of choice probability among cells.

(b) Correlation between neuronal sensitivity and choice probability.

(c, d) Comparison of different modeling approaches for choice probability.